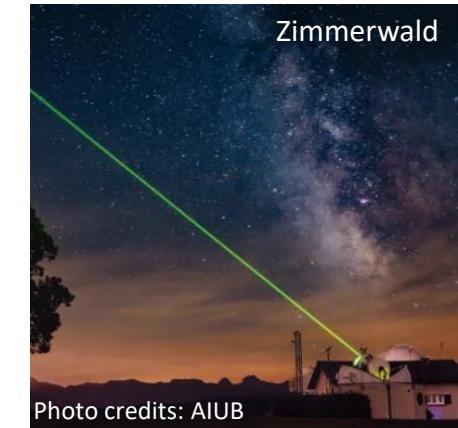
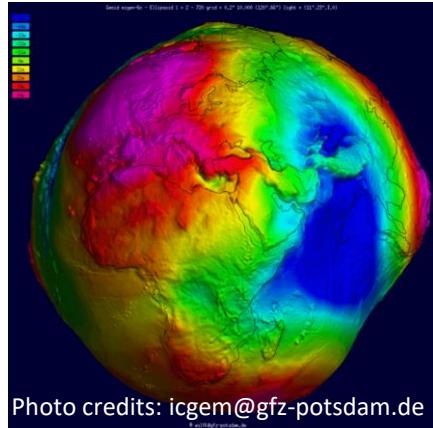


Impact of a Priori Gravity Field Models on SLR Data Processing



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IUGG Berlin 2023, 28th GENERAL ASSEMBLY, 17 July 2023

Outline

- Parametrization and background models used in the SLR processing
 - A priori gravity field models
 - Results of multi-satellite SLR combinations using LAGEOS-1/2, LARES and Starlette SLR observations
 - Summary & Outlook

LAGEOS-1/2 + LARES: Parametrization + Models

Outline:

- Parametrization + Models
- A priori Gravity fields
- Results
- Summary & Outlook

• Parametrization

Satellites	LAGEOS-1/2	LARES
Parametrization	1.0	0.45
Osculating elements	$a, e, i, \Omega, \omega, u_0$	1 set per 7 days
Constant and once-per-revolution accelerations	S_0, S_S, S_C, W_S, W_C	1 set per 7 days
Pseudo-stochastic pulses	no pulses	in along-track (twice per day)
Earth Rotation Parameters	$X_P, Y_P, UT1 - UTC$	piecewise-linear
Geocenter coordinates	1 set per 7 days	free geocenter
Station coordinates	1 set per 7 days	NNR and NNT
Range biases	1 set per 7 days for selected stations	all stations

• Background models

Models	Description
Reference frame	SLRF2014
ERP	IERS-14-C04
Nutation model	IAU2000 (Mathews et al. 2002)
Subdaily pole model	DESAI: IERS 2010
Ocean tide model	FES2014b: d/o 30 (Lyard et al. 2021) + admittances
Earth Tides	Solid earth tides, Pole tides and Ocean pole tides: IERS 2010
Loading corrections	Ocean tidal loading: FES2014 Atmospheric tidal loading: Ray and Ponte (Ray and Ponte 2003)
De-aliasing products	Atmosphere + Ocean RL06: d/o 30 incl. S1- and S2-atmosphere tides (Dobslaw et al. 2017)
Earth gravity field	GGM05S, COST-G, ? : d/o 90

Study the impact of a priori gravity field models on the estimation of geodetic parameters!

A priori gravity field models

Outline:

- Parametrization + Models
- **A priori Gravity fields**
- Results
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- GGM05S (static field)
- GGM05S + time-variable coefficients for the zonals $C_{20}/C_{30}/C_{40}/C_{50}/C_{60}$ and C_{21}/S_{21} provided by the ILRS («semi» time-variable field)
- COST-G (time-variable field)

S_{22}	S_{21}	C_{20}	C_{21}	C_{22}
S_{33}	S_{32}	S_{31}	C_{30}	C_{31}
S_{44}	S_{43}	S_{42}	S_{41}	C_{40}
S_{55}	S_{54}	S_{53}	S_{52}	S_{51}
S_{66}	S_{65}	S_{64}	S_{63}	S_{62}

Static

S_{22}	S_{21}	C_{20}	C_{21}	C_{22}
S_{33}	S_{32}	S_{31}	C_{30}	C_{31}
S_{44}	S_{43}	S_{42}	S_{41}	C_{40}
S_{55}	S_{54}	S_{53}	S_{52}	S_{51}
S_{66}	S_{65}	S_{64}	S_{63}	S_{62}

Time-var. ILRS

S_{22}	S_{21}	C_{20}	C_{21}	C_{22}
S_{33}	S_{32}	S_{31}	C_{30}	C_{31}
S_{44}	S_{43}	S_{42}	S_{41}	C_{40}
S_{55}	S_{54}	S_{53}	S_{52}	S_{51}
S_{66}	S_{65}	S_{64}	S_{63}	S_{62}

COST-G

Further option: replace C_{21}/S_{21} according to the IERS2010 conventions

Outline:

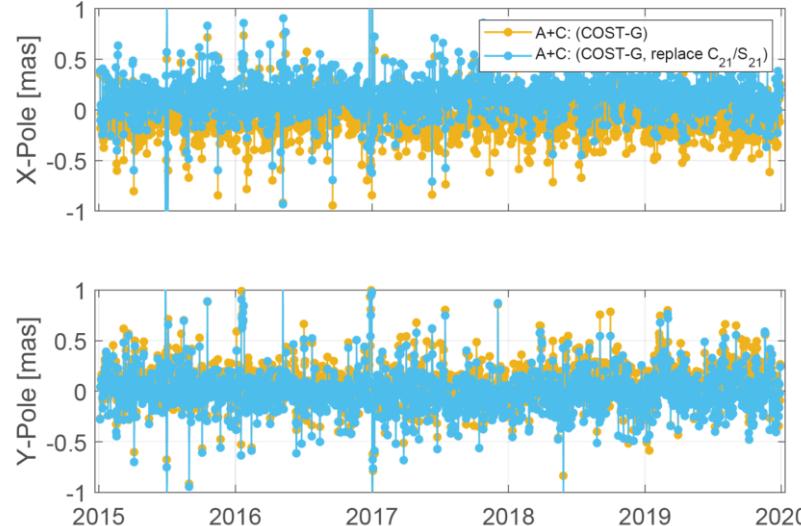
- Parametrization + Models
- A priori Gravity fields
- Results
 - LAGEOS-1/2 + LARES
 - LAGEOS-1/2 + LARES + Starlette
- Summary & Outlook

Glossary:

- A: LAGEOS-1/2
- C: LARES

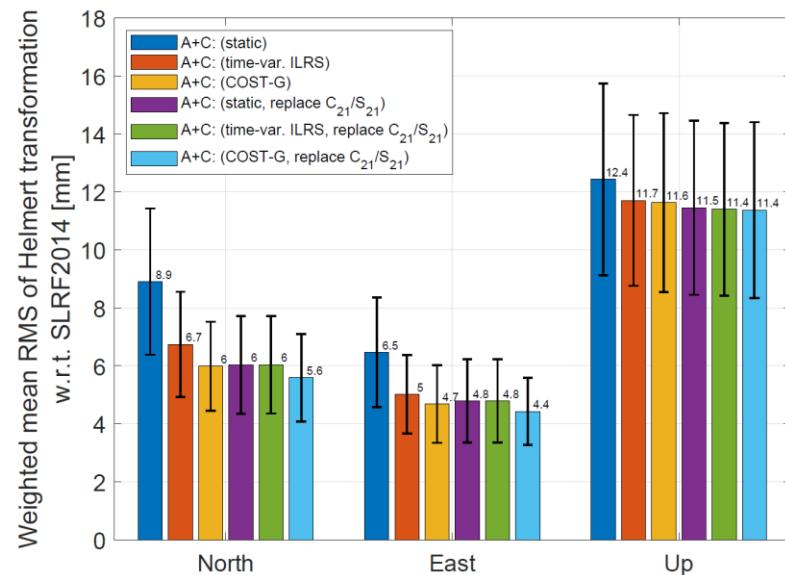
LAGEOS-1/2 + LARES: Results

• Earth Rotation Parameters (ERPs)



	Replace C_{21}/S_{21}	X pole [μas]		Y pole [μas]		UT1-UTC [μs]	
		Bias	WRMS	Bias	WRMS	Bias	WRMS
Static	✗	-295.1	350.8	-12.5	158.7	-36.2	133.7
Static	✓	22.6	132.2	-9.8	116.9	-13.4	83.5
Time-var. ILRS	✗	-86.8	166.5	38.3	146.1	-16.3	87.0
Time-var. ILRS	✓	21.1	130.6	-11.9	115.3	-12.6	81.4
COST-G	✗	-74.8	148.7	60.4	136.8	-8.9	79.1
COST-G	✓	126.6	177.3	-16.0	117.6	-10.2	75.2

• Station coordinates



LAGEOS-1/2 + LARES: Results

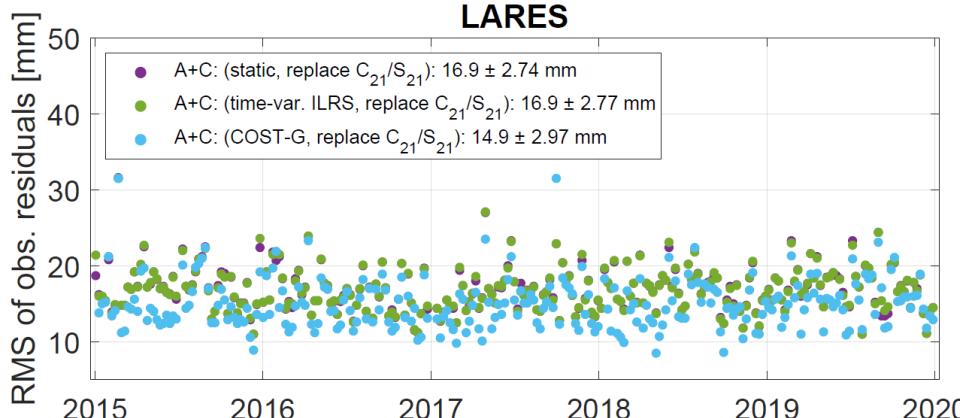
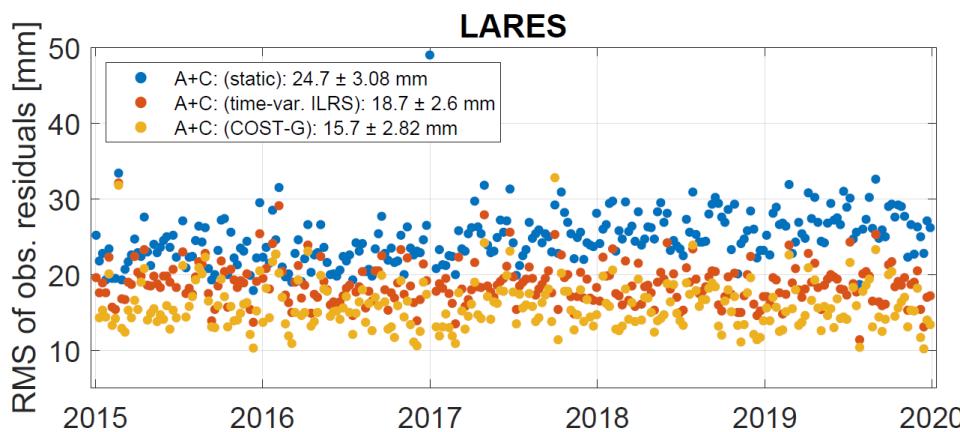
Outline:

- Parametrization + Models
- A priori Gravity fields
- Results
 - LAGEOS-1/2 + LARES
 - LAGEOS-1/2 + LARES + Starlette
- Summary & Outlook

Glossary:

- A: LAGEOS-1/2
- C: LARES

• Observation residuals



• Conclusions

- The replacement of C_{21}/S_{21} (according to the IERS2010 conventions)
 - improves the geodetic parameters: ERPs (except for X-pole if COST-G model is used), station coordinates,
 - reduces the observation residuals, independent of the used a priori gravity field model.
- The use of the gravity field model provided by COST-G
 - improves some ERPs and the station coordinates,
 - reduces the observation residuals of LARES.

LAGEOS-1/2 + LARES + Starlette: Parametrization

Outline:

- Parametrization + Models
- A priori Gravity fields
- Results
 - LAGEOS-1/2 + LARES
 - LAGEOS-1/2 + LARES + Starlette
- Summary & Outlook

Glossary:

- A: LAGEOS-1/2
- C: LARES
- D: Starlette

References:

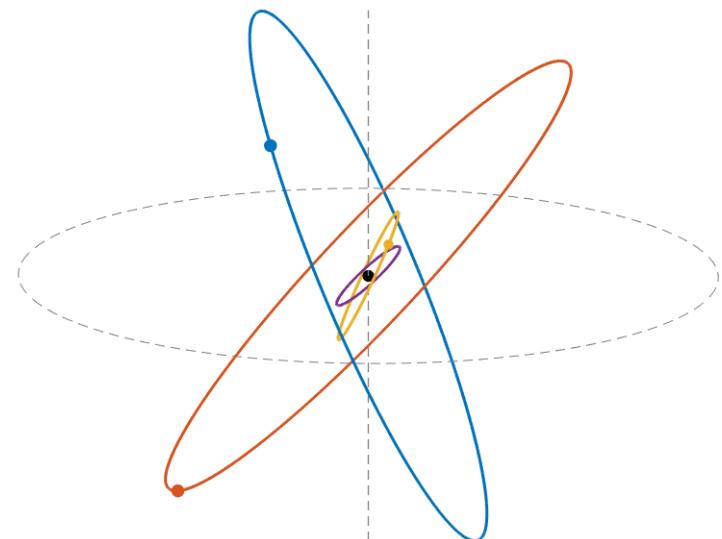
[1] <https://ilrs.gsfc.nasa.gov>

Parametrization

VCE

Satellites	LAGEOS-1/2	LARES	Starlette
Parametrization			
Osculating elements			
$a, e, i, \Omega, \omega, u_0$			
1 set per 7 days			
Constant and once-per-revolution accelerations			
S_0, S_S, S_C, W_S, W_C			
1 set per 7 days			
Pseudo-stochastic pulses			
no pulses		in along-track (twice per day)	in along-track (twelve per day)
Earth Rotation Parameters			
$X_P, Y_P, UT1 - UTC$			
piecewise-linear			
Geocenter coordinates			
1 set per 7 days			
free geocenter			
Station coordinates			
1 set per 7 days			
NNR and NNT			
Range biases			
1 set per 7 days for			
selected stations		all stations	

Orbital planes



	LAGEOS-1	LAGEOS-2	LARES	Starlette	[1]
Diameter [m]	0.60	0.60	0.36	0.24	
Weight [kg]	407.0	405.4	386.6	47.5	
Altitude [km]	5860	5620	1450	812	
Inclination [°]	109.8	52.6	69.5	48.8	

LAGEOS-1/2 + LARES + Starlette: Results

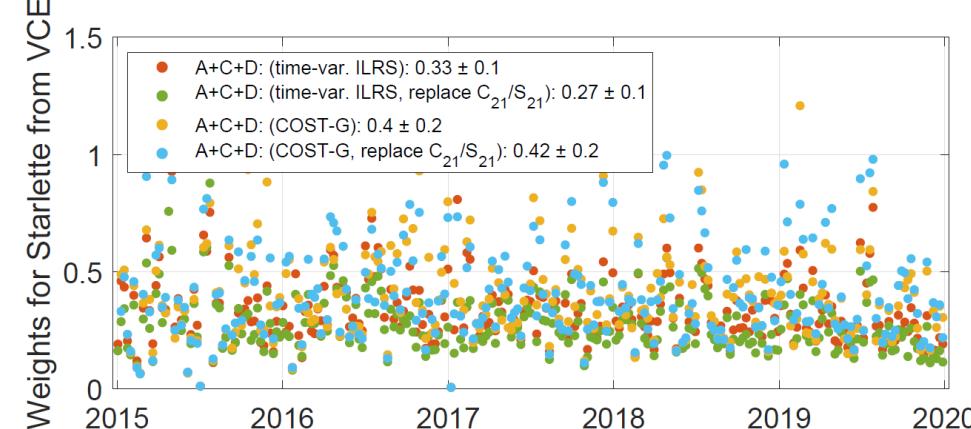
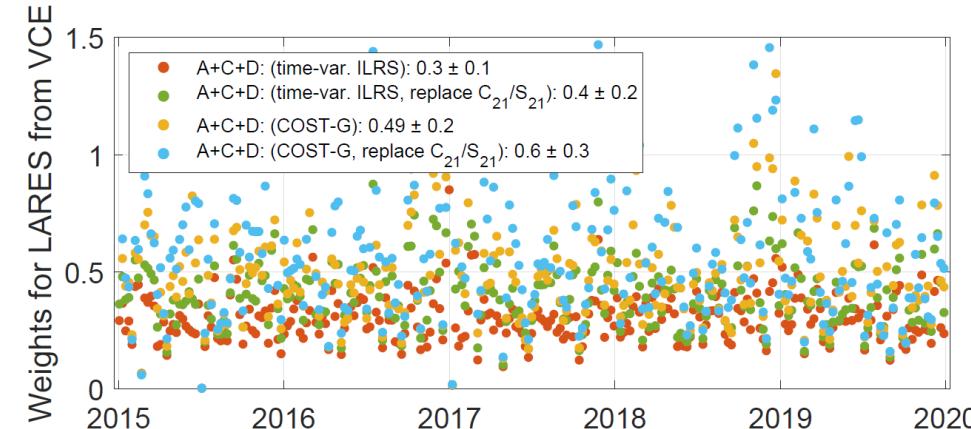
Outline:

- Parametrization + Models
- A priori Gravity fields
- **Results**
 - LAGEOS-1/2 + LARES
 - LAGEOS-1/2 + LARES + Starlette
- Summary & Outlook

Glossary:

- A: LAGEOS-1/2
- C: LARES
- D: Starlette

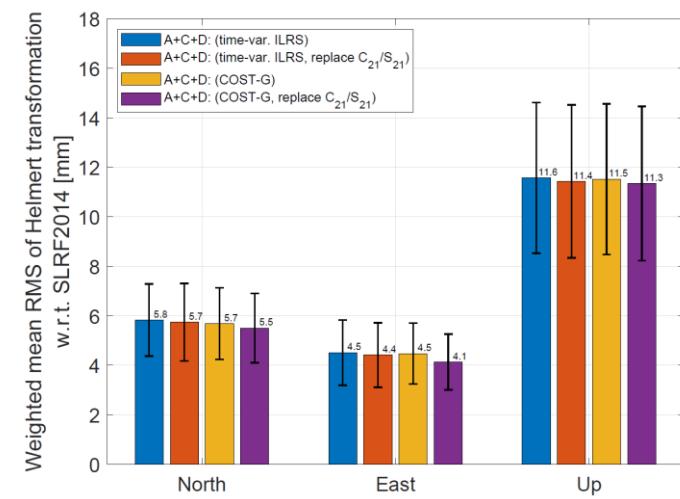
Weights per satellite



Earth Rotation Parameters

	Replace C_{21}/S_{21}	X pole [μas]		Y pole [μas]		UT1-UTC [μs]	
		Bias	WRMS	Bias	WRMS	Bias	WRMS
Time-var. ILRS	✗	19.8	128.0	47.7	134.3	-8.3	73.2
Time-var. ILRS	✓	89.1	150.0	0.5	112.5	-9.5	73.1
COST-G	✗	-70.8	150.5	59.7	143.9	-11.1	80.1
COST-G	✓	145.3	193.3	-33.0	129.8	-6.0	71.7

Station coordinates



LAGEOS-1/2 + LARES + STARLETTE: RESULTS

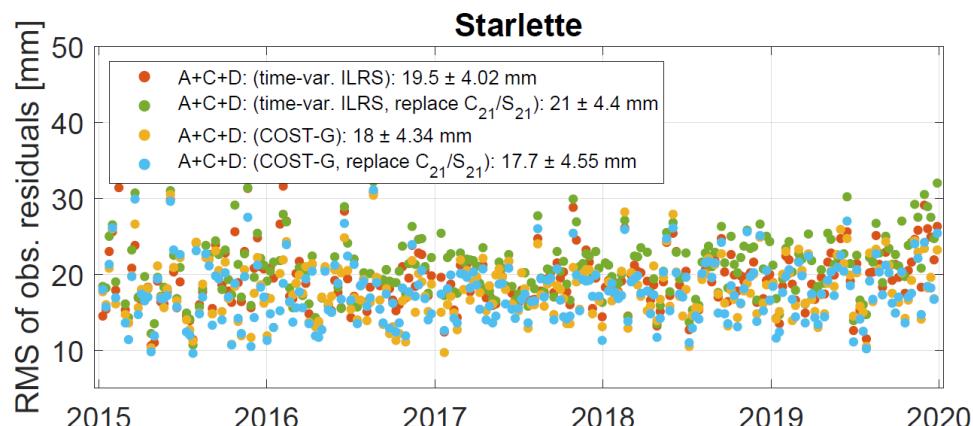
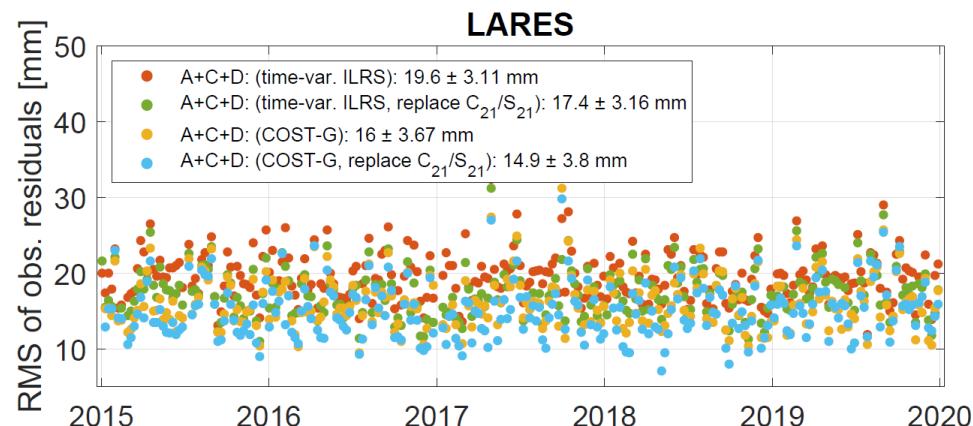
Outline:

- Parametrization + Models
- A priori Gravity fields
- Results
 - LAGEOS-1/2 + LARES
 - LAGEOS-1/2 + LARES + Starlette
- Summary & Outlook

Glossary:

- A: LAGEOS-1/2
- C: LARES
- D: Starlette

• Observation residuals



• Conclusions

- LARES and Starlette receive from the VCE the highest weights if the COST-G model is used.
- The replacement of C_{21}/S_{21} (according to the IERS2010 conventions)
 - has a major impact on the weights of LARES,
 - downgrades the X-pole, while the Y-pole is improved

independent of the used a priori gravity field model.

SUMMARY & OUTLOOK

Outline:

- Parametrization
 - + Models
- A priori Gravity fields
- Results
 - LAGEOS-1/2 + LARES
 - LAGEOS-1/2 + LARES + Starlette
- Summary & Outlook

- **Summary:**
 - The a priori gravity field model has an impact on the estimated geodetic parameters of SLR analyses.
 - The COST-G model can (should) also be used in the SLR processings.
- **Outlook:**
 - Study the impact of the a priori gravity field model when the low-degrees are co-estimated.

SUMMARY & OUTLOOK

Outline:

- Parametrization + Models
- A priori Gravity fields
- Results
 - LAGEOS-1/2 + LARES
 - LAGEOS-1/2 + LARES + Starlette
- Summary & Outlook

Thank you for your attention!