

# Evaluation of xTRF2014 Solutions

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Unified Analysis Workshop 2017  
10–12. July 2017, Paris, France

# Overview

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Introduction and motivation

Description of the processing scheme

Comparison of station coordinates

Comparison of orbits with SLR measurements

Comparing satellite antenna offsets

Comparing polar motion results

- **DTRF2014**

Deutsches Geodätisches Forschungsinstitut at TU Munich  
(DGFI-TUM, Germany; Seitz et al. 2016)

**positions+linear velocities**

# xTRF2014 Solutions

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- **DTRF2014** and **DTRF2014L**

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**positions + linear velocities + NT loading corrections**

# xTRF2014 Solutions

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**positions+linear velocities + NT loading corrections**

- **ITRF2014**

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**positions+linear velocities+PSD corr.**

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**positions+linear velocities+PSD corr. + periodic functions**

- **JTRF2014**

Jet Propulsion Laboratory (JPL, USA; Wu et al. 2015)

**positions every week**

# Description of the processing scheme



**GNSS Reprocessing in 2015:**



European Gravity Service for Improved Emergency Management

## Product availability:

GNSS satellite orbits:

GPS

GLONASS

since 1994

since 2002

GNSS satellite clock corrections:

sampling 30 s:

since 2000

since 2008

sampling 5 s:

since 2003

since 2010

# Description of the processing scheme

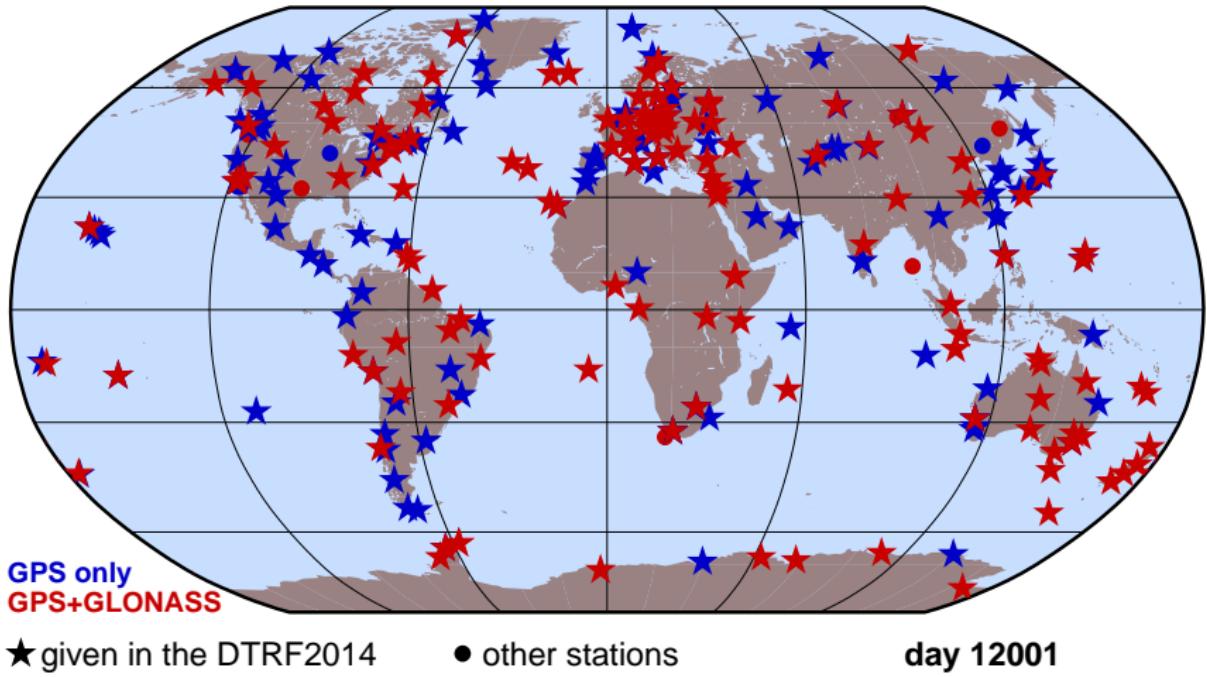


## Product availability:

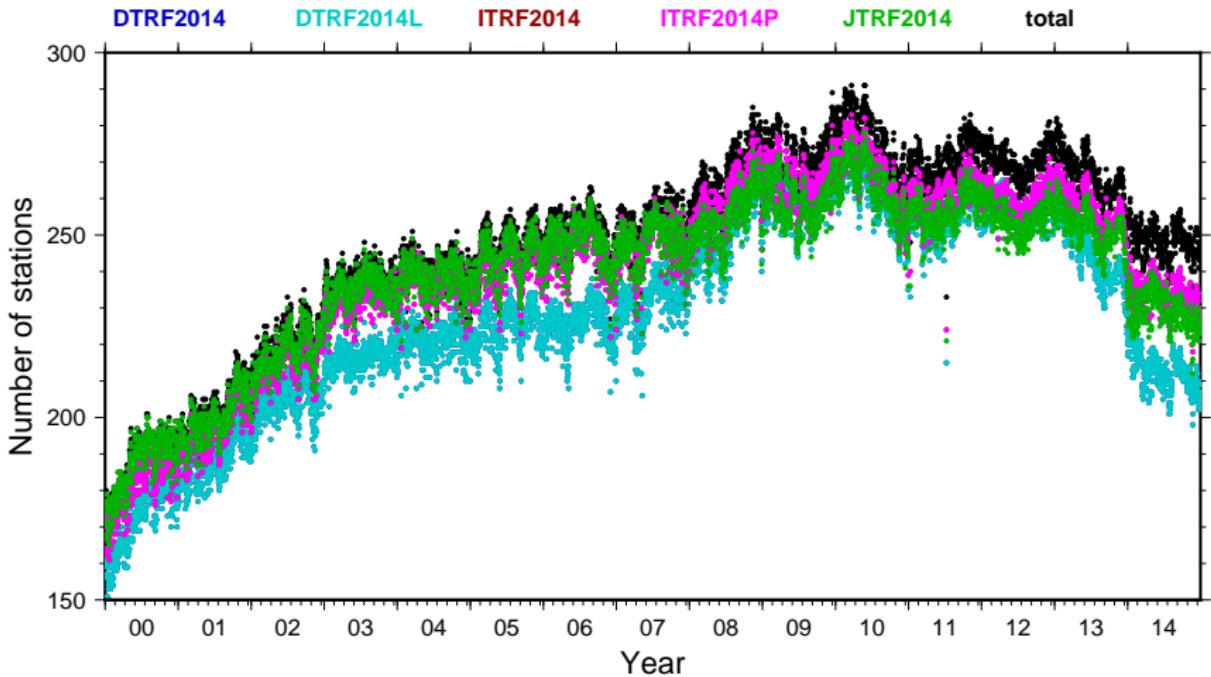
	GPS	GLONASS
GNSS satellite orbits:	since 1994	since 2002
GNSS satellite clock corrections:		
sampling 30 s:	since 2000	since 2008
sampling 5 s:	since 2003	since 2010

- EGSIEM-repro considers the ECOM2 orbit model.
- The solution is consistent with repro2:
  - [IGb08/IGS08.ATX](#)
  - same station selection.

# The station network

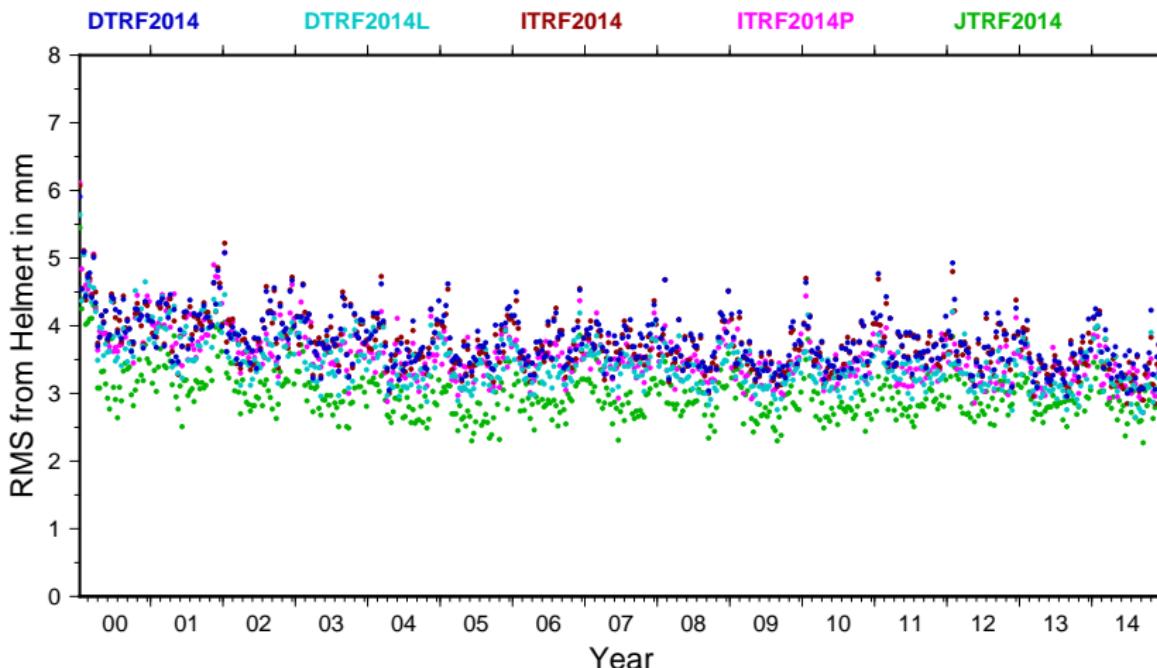


# The station network



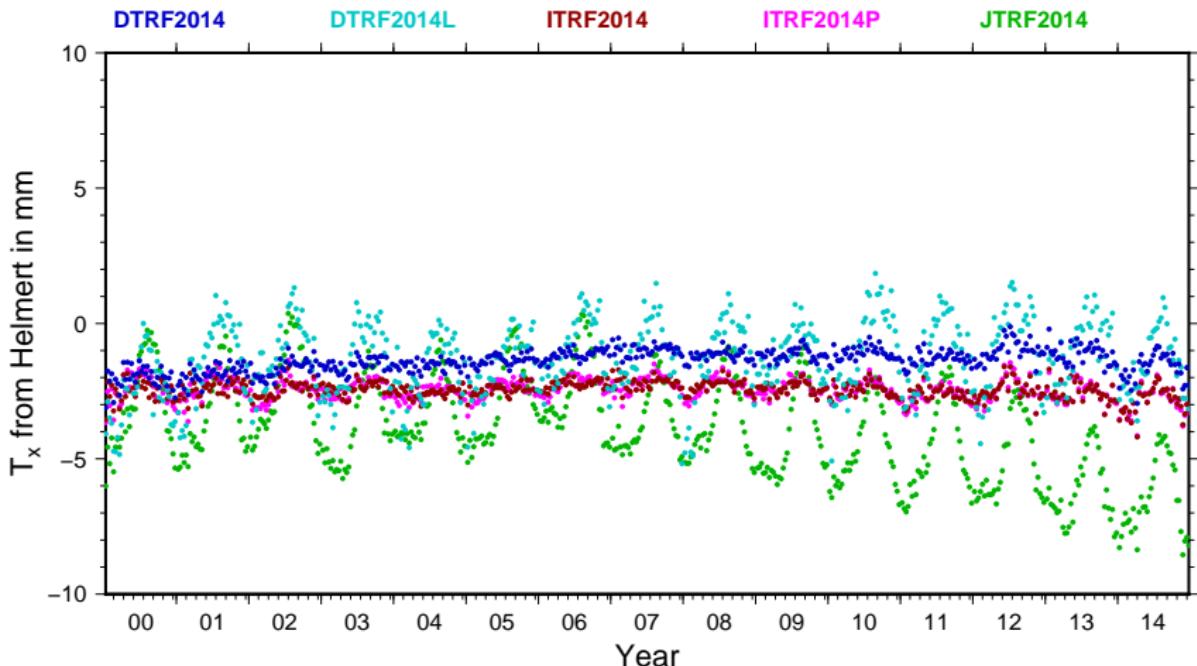
# Comparison of EGIEM solution (IGb08)

RMS (consistency) from a Helmert Transformation



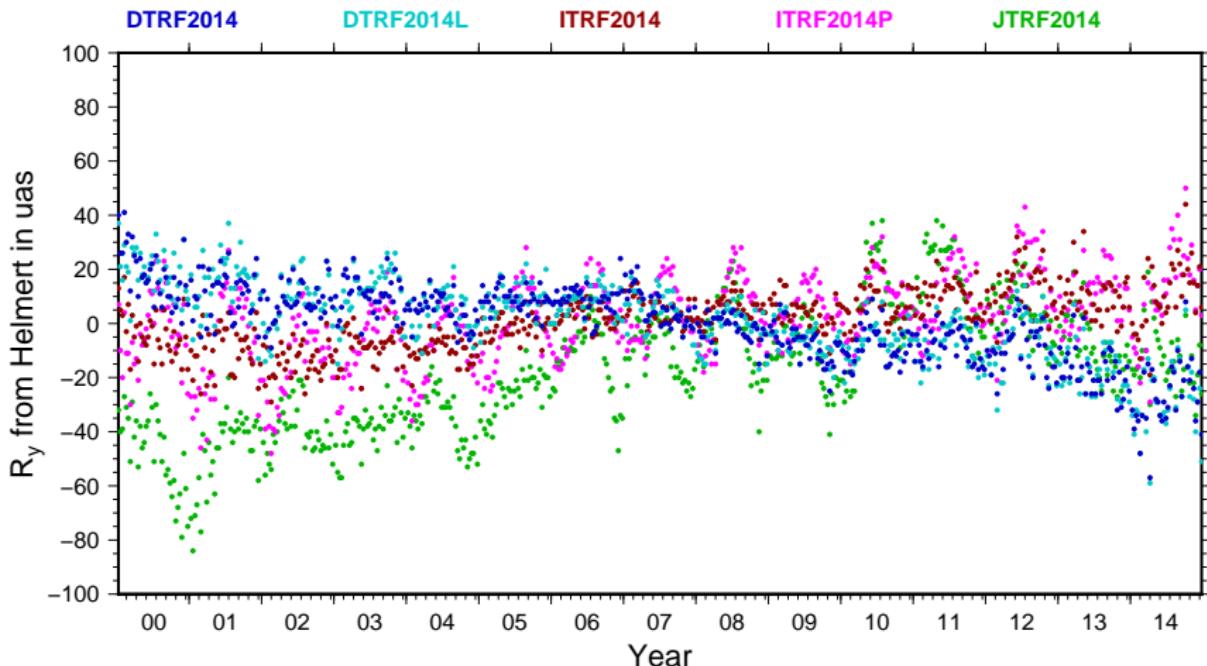
# Comparison of EGIEM solution (IGb08)

Translations in X from a Helmert Transformation



# Comparison of EGIEM solution (IGb08)

Rotations in Y from a Helmert Transformation



# The following parameters are estimated:

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- station coordinates with a minimum constraint solution applying a NNR and NNT condition (no-net-rotation and no-net-translation) to all stations with given coordinates in the particular reference frame,

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- Earth rotation parameters (X- and Y-pole offset and rate as well as LOD; 1st UT-values taken from the C04 product), and
- GNSS satellite orbits with 7 dynamical orbit parameters according to the ECOM2 description and three empirical velocity changes of the satellites every 12 hours.

# Comparison of station coordinates

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- The resulting coordinates are confronted with the datum-free solution (where the GCC was estimated).

# Comparison of station coordinates

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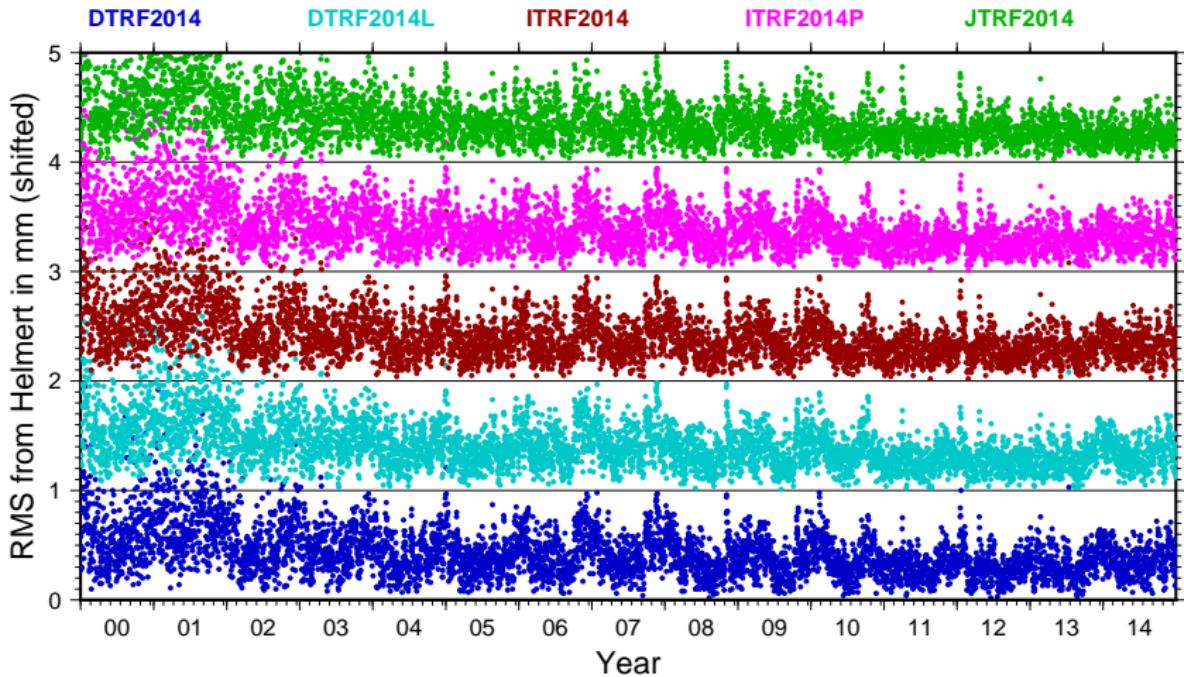
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- The resulting coordinates are confronted with the datum-free solution (where the GCC was estimated).
- The transformation and rotation parameters are reflecting the GCC estimates and the orientation from the datum-free solution and are therefore not of interest regarding the consistency between all five reference frame solutions.
- The RMS of the residuals are more interesting because they can be seen as a measure for the distortion of the network geometry introduced by forcing the center of mass into the origin.

# Comparison of station coordinates



# Comparison of orbits with SLR measurements

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- Station coordinates for the SLR tracking stations have been derived from the five reference frame solutions.

# Comparison of orbits with SLR measurements

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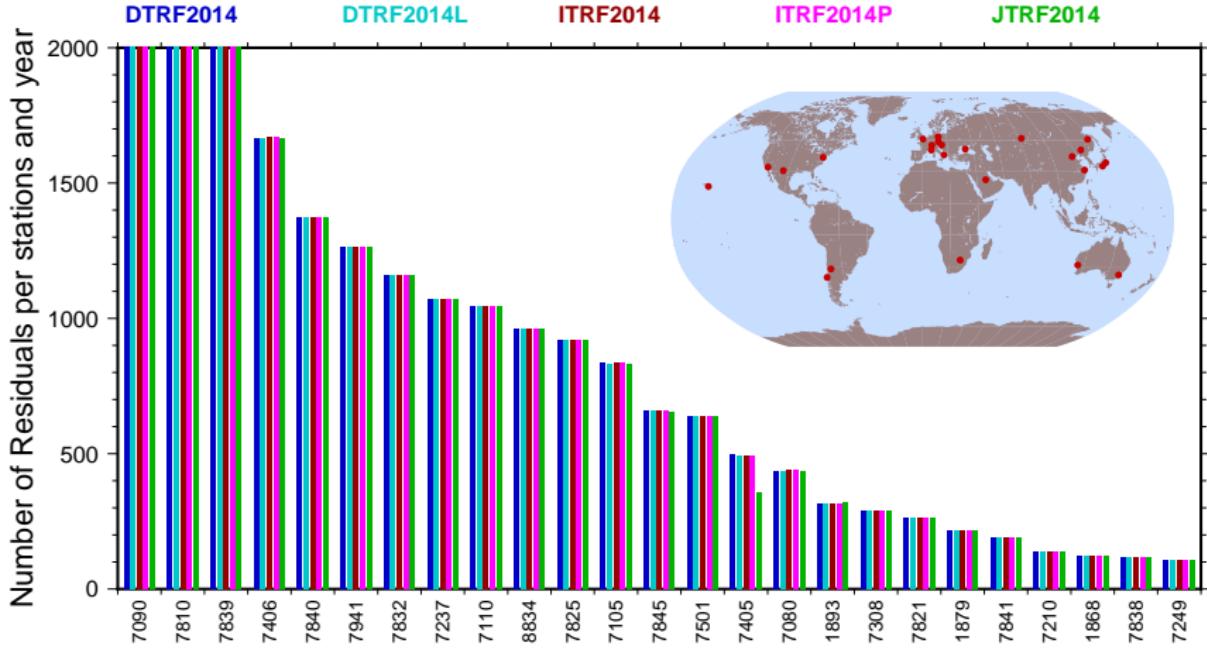
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# Comparison of orbits with SLR measurements

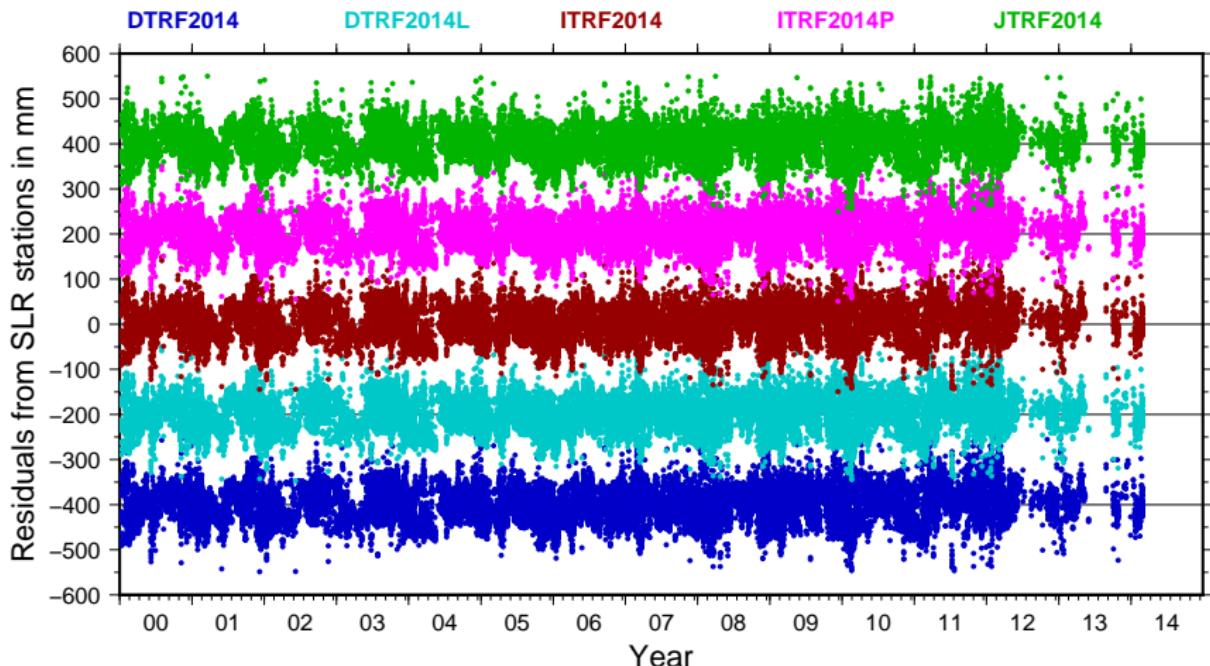
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- Station coordinates for the SLR tracking stations have been derived from the five reference frame solutions.
- The GNSS-satellite orbits (with the related ERPs) have been taken from the GNSS microwave solution.
- The SLR measurements are directly confronted with the geometry without estimating parameters).  
(of course the usual corrections for troposphere, relativistic effects, etc. have been applied).

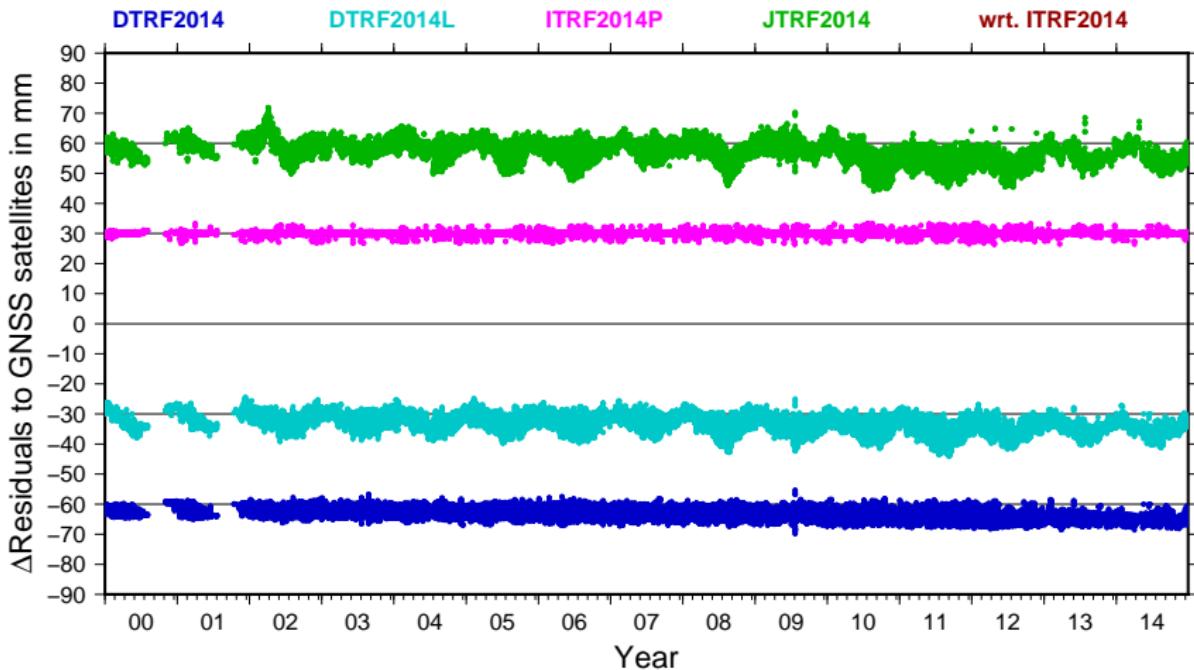
# SLR stations tracking GNSS satellites



# SLR residuals for G 036 satellite



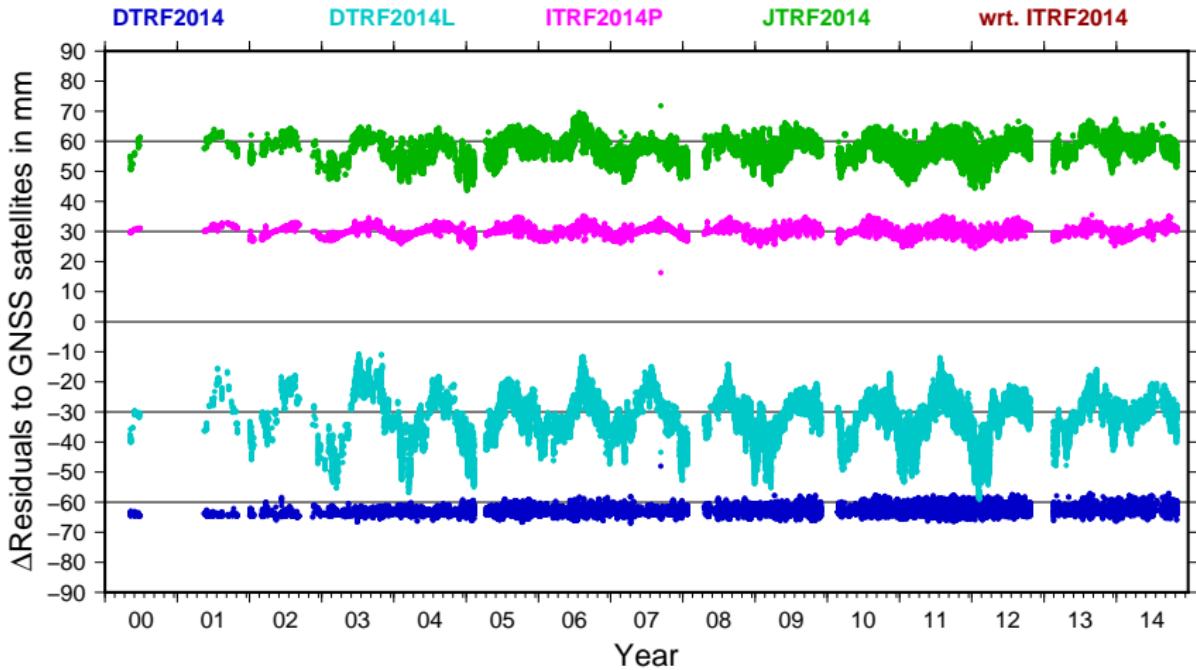
# SLR residuals to GNSS satellites per station



a) SLR station: Yarragadee, Australia (number 7090)

The reference ITRF2014 was arbitrary chosen.

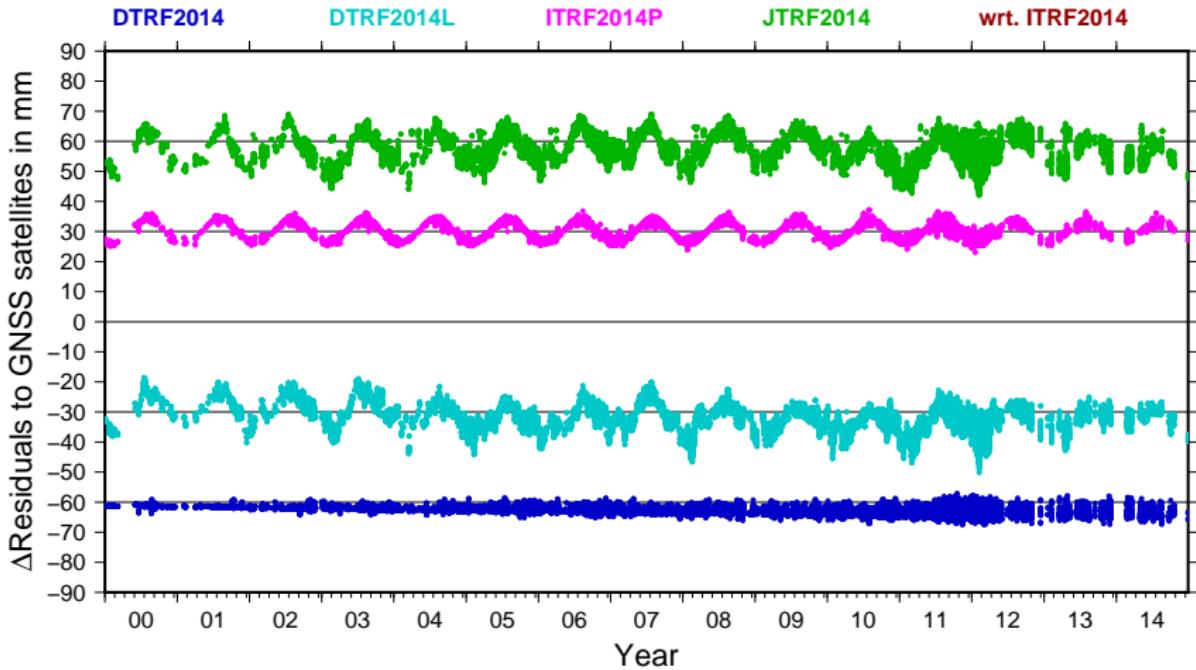
# SLR residuals to GNSS satellites per station



b) SLR station: Zimmerwald, Switzerland (number 7810)

The reference ITRF2014 was arbitrary chosen.

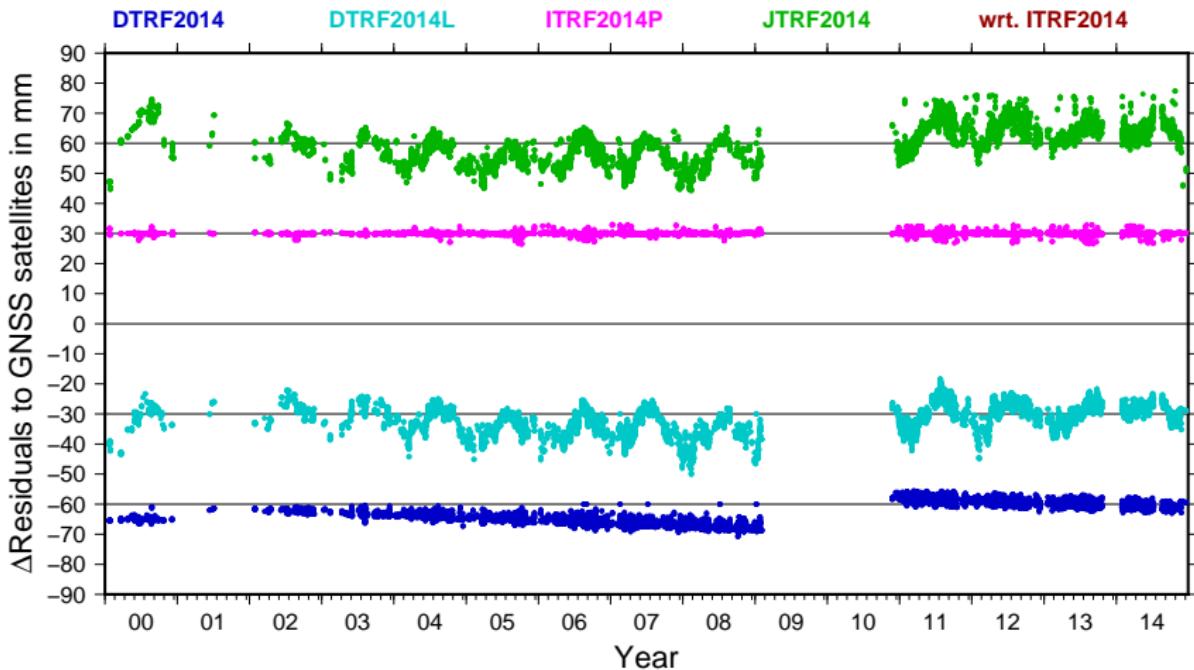
# SLR residuals to GNSS satellites per station



c) SLR station: Graz, Austria (number 7839)

The reference ITRF2014 was arbitrary chosen.

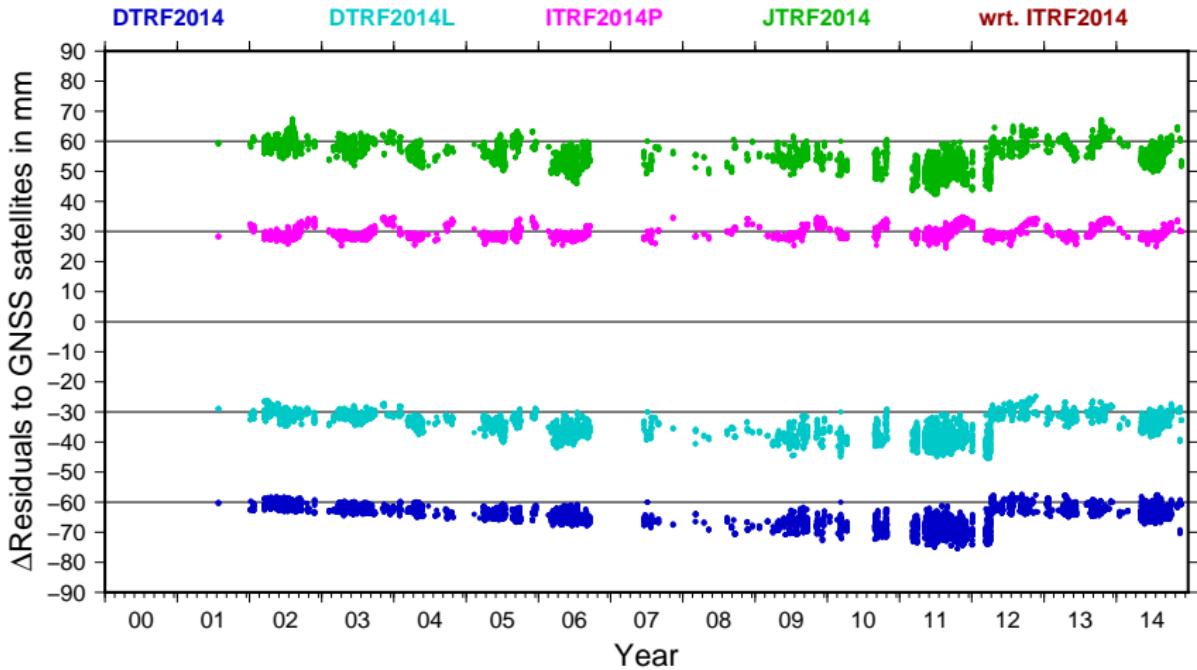
# SLR residuals to GNSS satellites per station



d) SLR station: Wettzell, Germany (number 8834)

The reference ITRF2014 was arbitrary chosen.

# SLR residuals to GNSS satellites per station

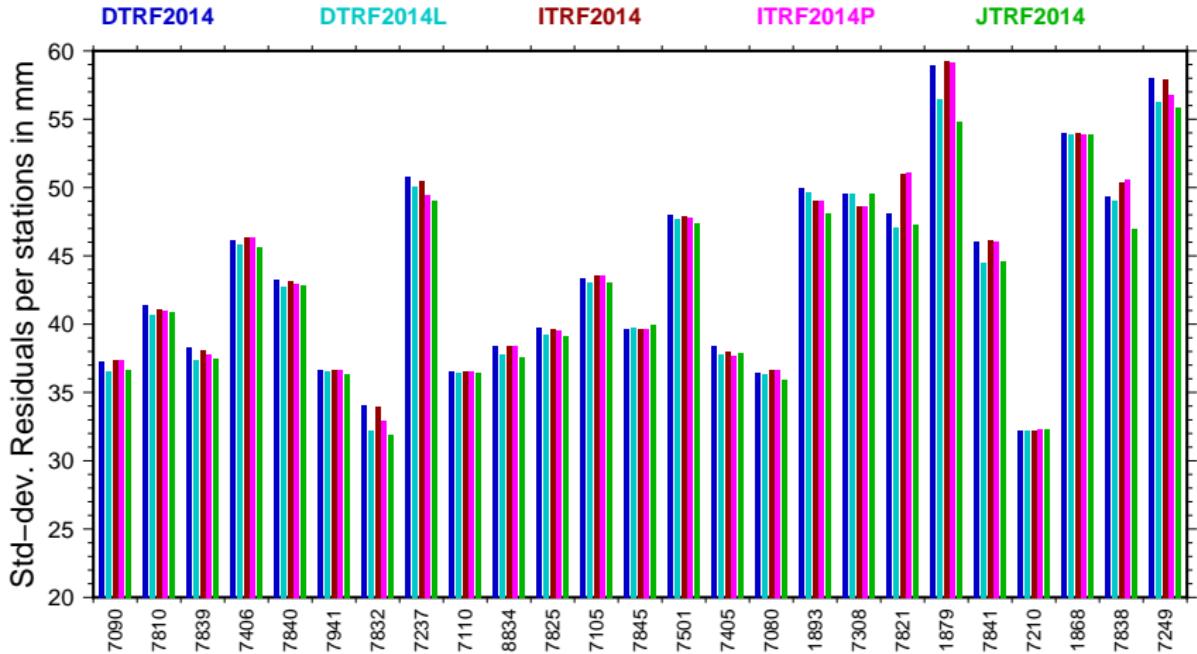


e) SLR station: Hartebeesthoek, South Africa (number 7501)

The reference ITRF2014 was arbitrary chosen.

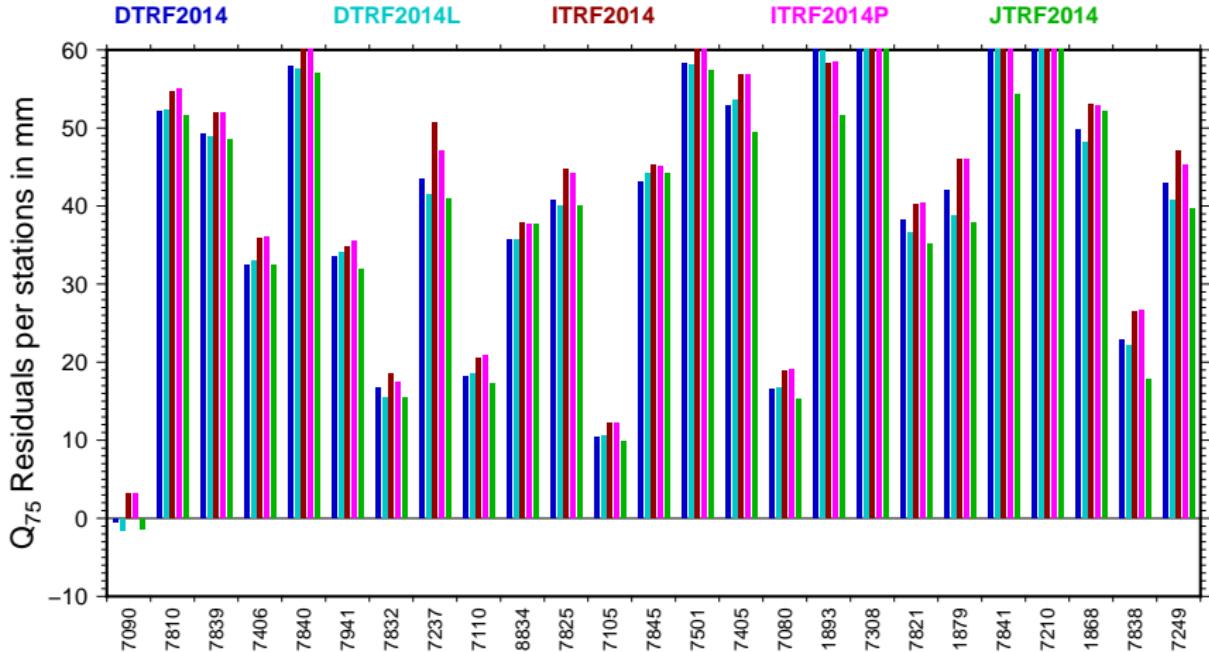
# SLR residuals to GNSS satellites per station

Median of all SLR residuals to GNSS satellites



# SLR residuals to GNSS satellites per station

Quantile 75% of all SLR residuals to GNSS satellites



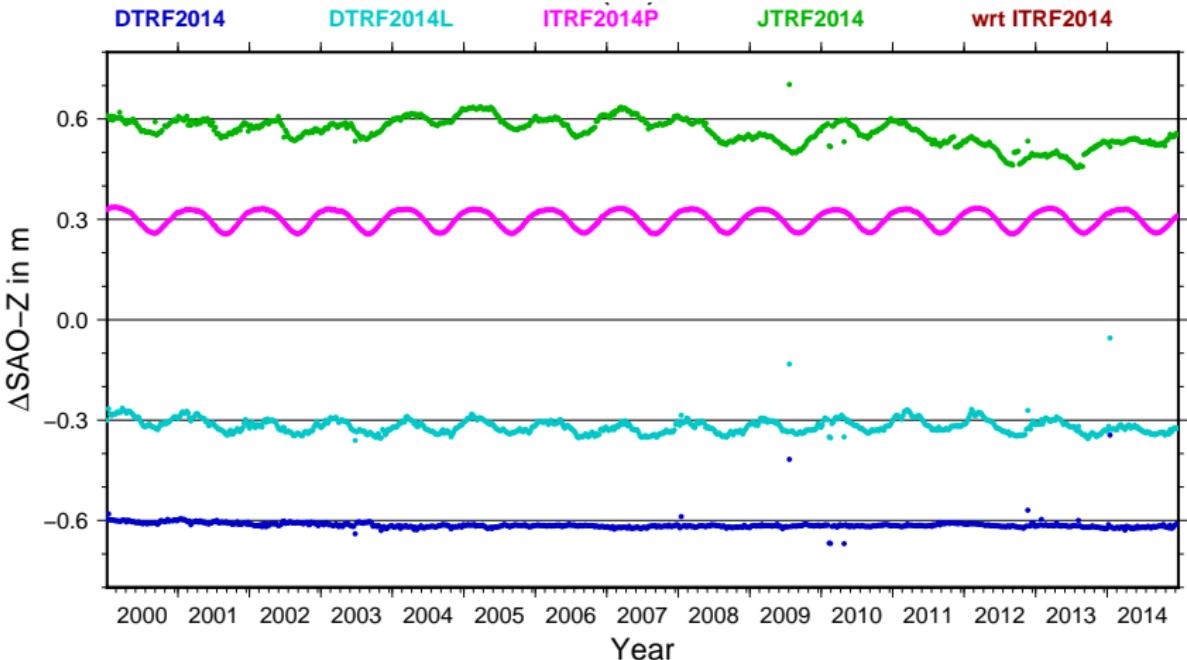
# Comparing satellite antenna offsets

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- For each solution series a weekly solution was created.
- The verified set of reference frame coordinates are used for the datum definition that includes even a **no scale change condition** in order to determine **satellite antenna offsets** (Z-component only).

# Consistency of satellite antenna Z-offsets

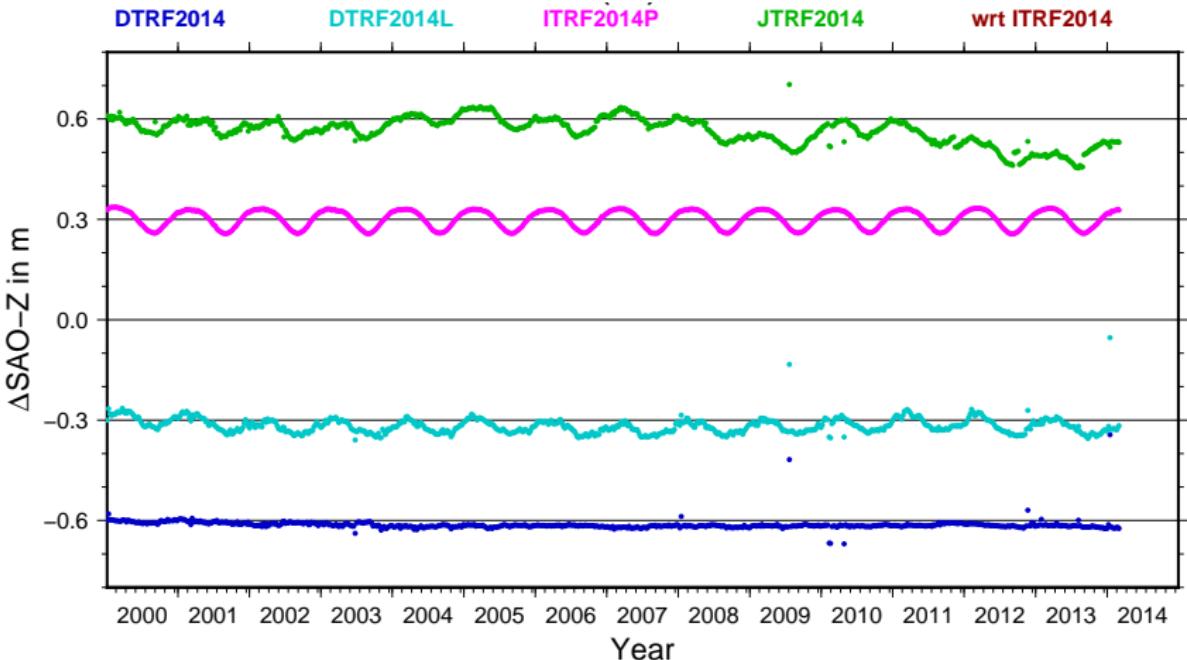
Satellite SVN G 034



The reference ITRF2014 was arbitrary chosen.

# Consistency of satellite antenna Z-offsets

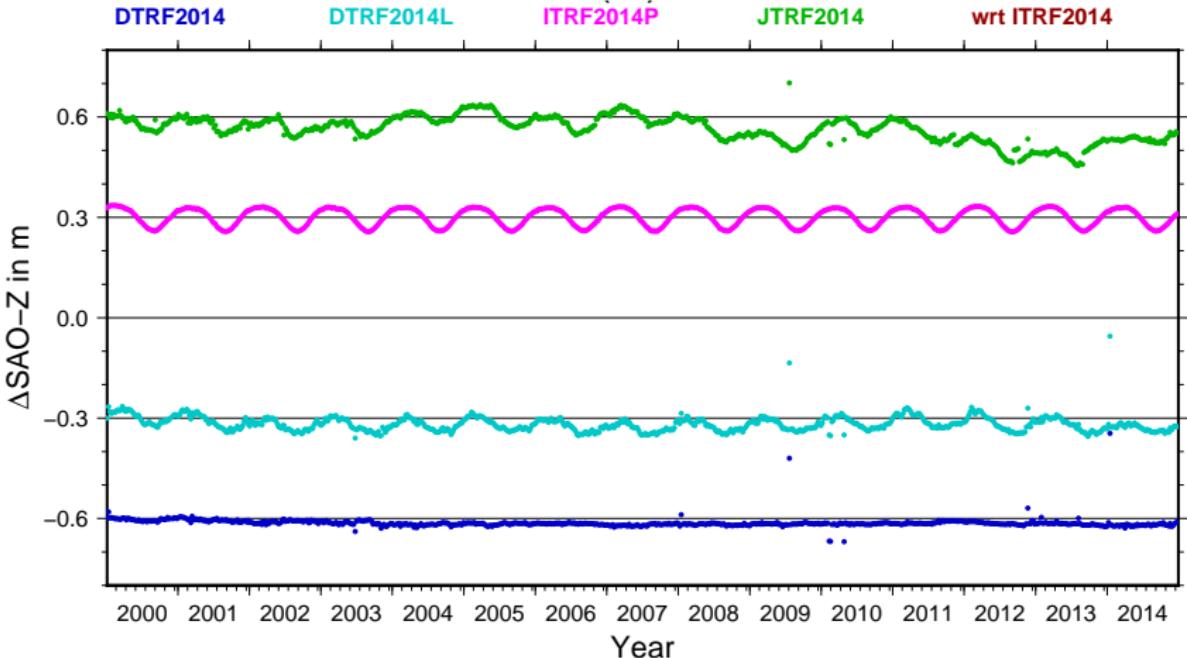
Satellite SVN G 036



The reference ITRF2014 was arbitrary chosen.

# Consistency of satellite antenna Z-offsets

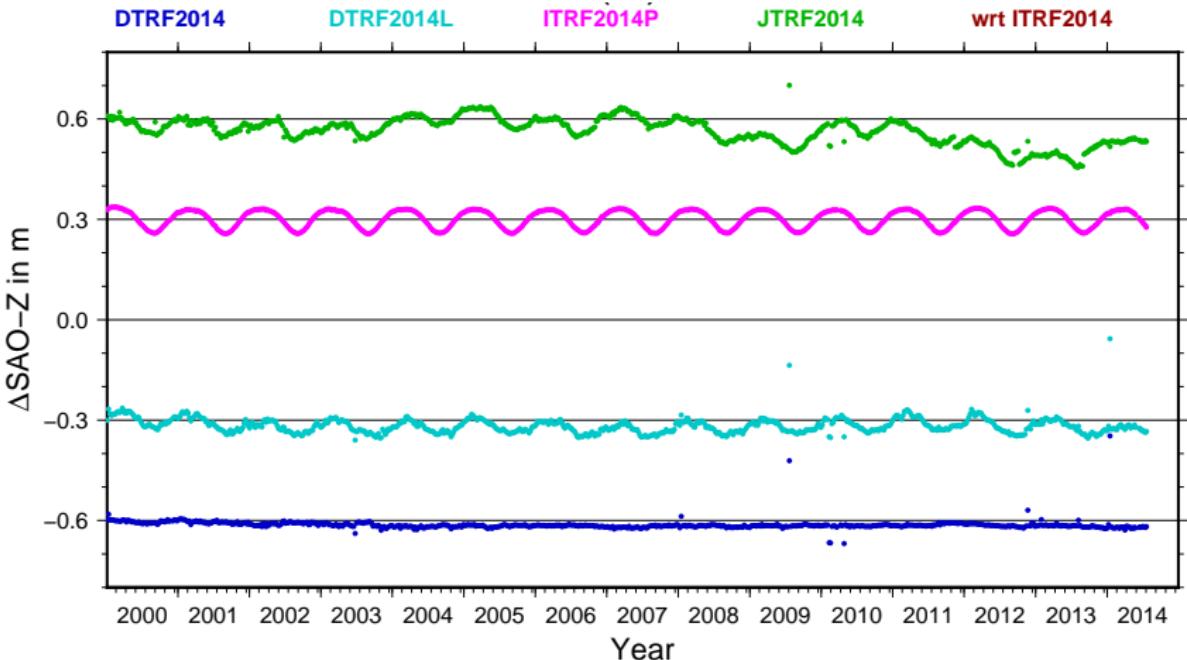
Satellite SVN G 038



The reference ITRF2014 was arbitrary chosen.

# Consistency of satellite antenna Z-offsets

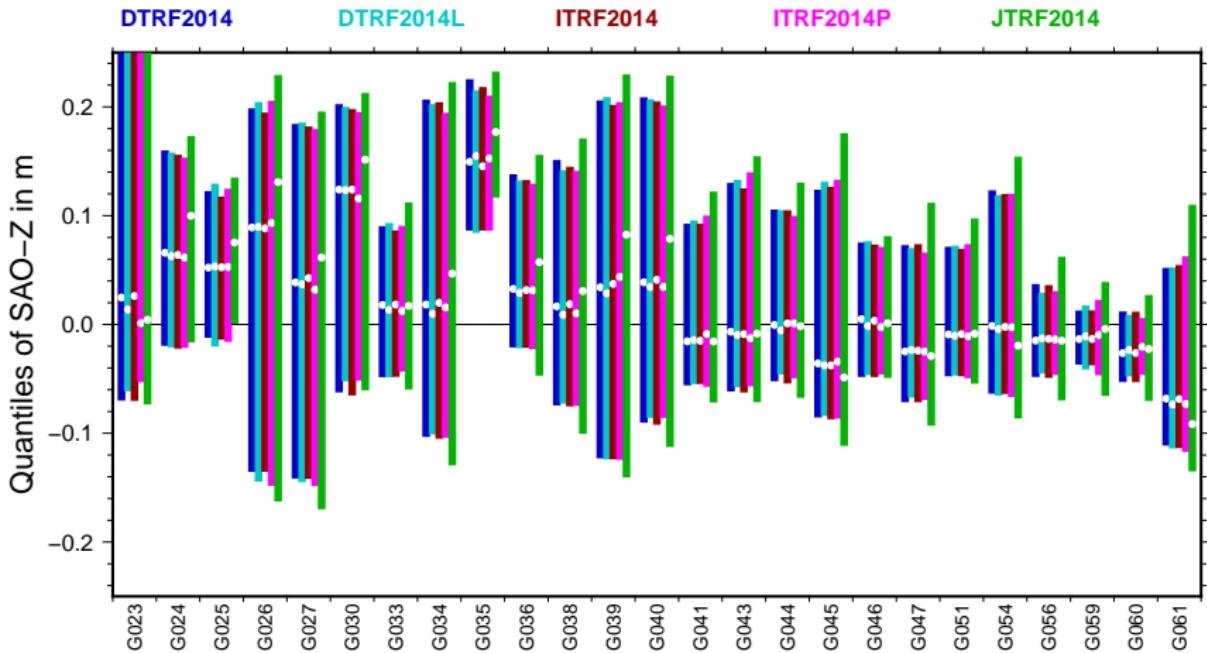
Satellite SVN G 039



The reference ITRF2014 was arbitrary chosen.

# Consistency of satellite antenna Z-offsets

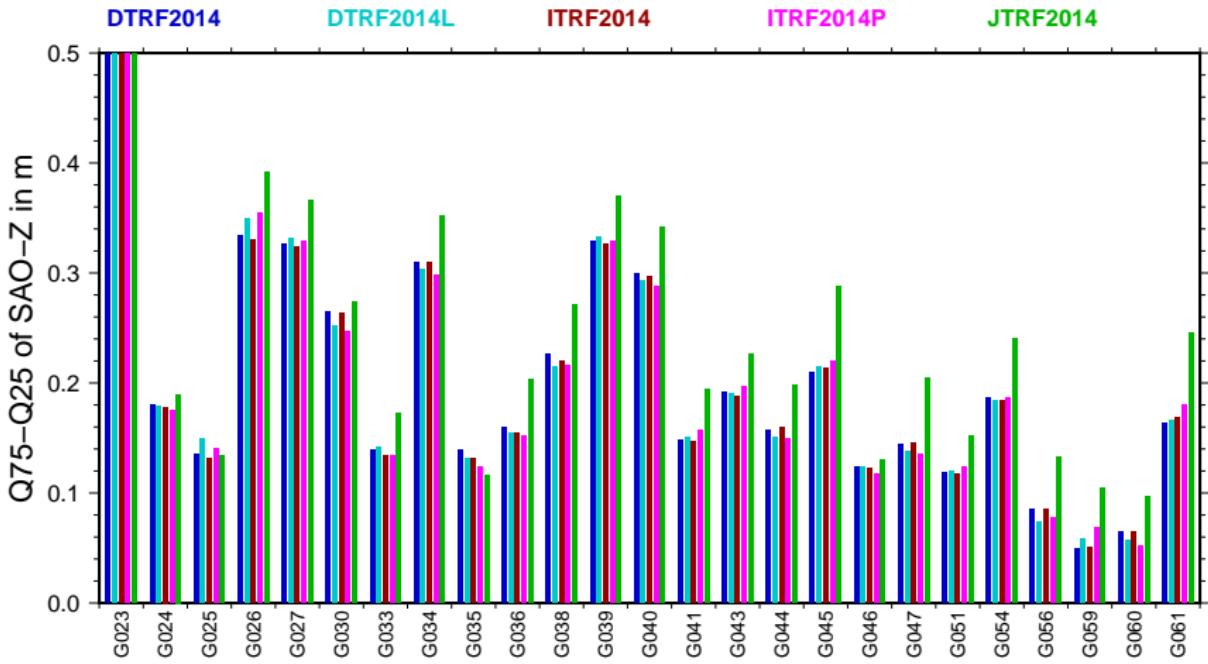
Quantiles 25%, 50% and 75% of the time series



Only satellites with more than 10 years of time series are considered.

# Consistency of satellite antenna Z-offsets

Difference between Quantiles 75% and 25%



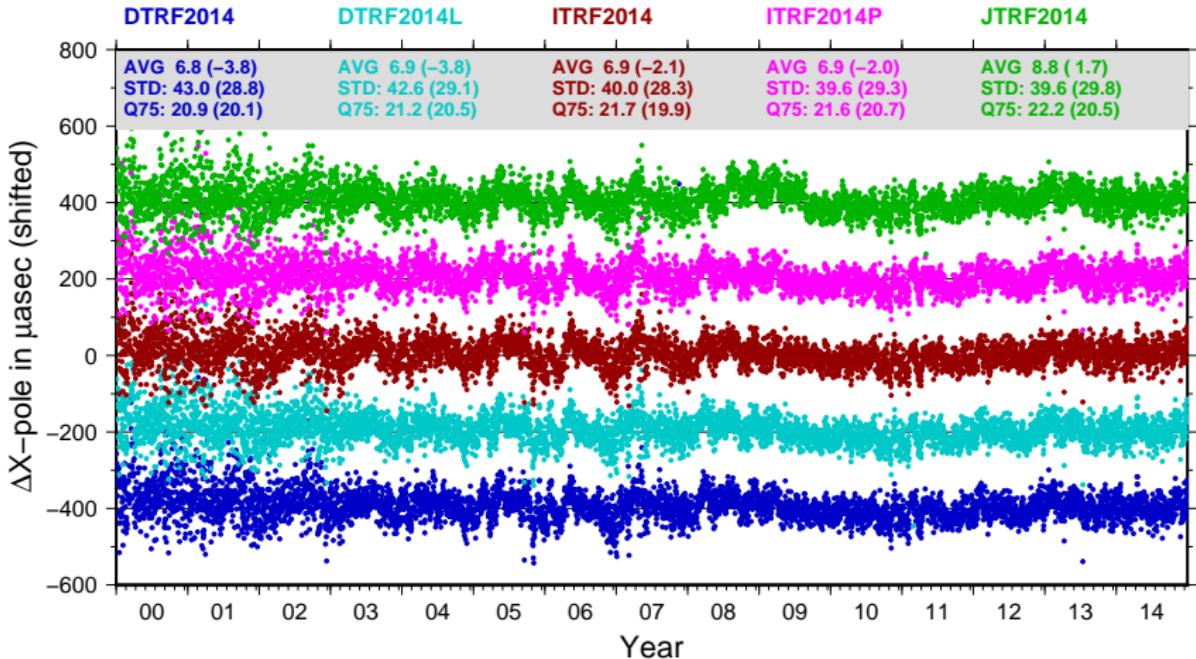
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# Comparing polar motion results

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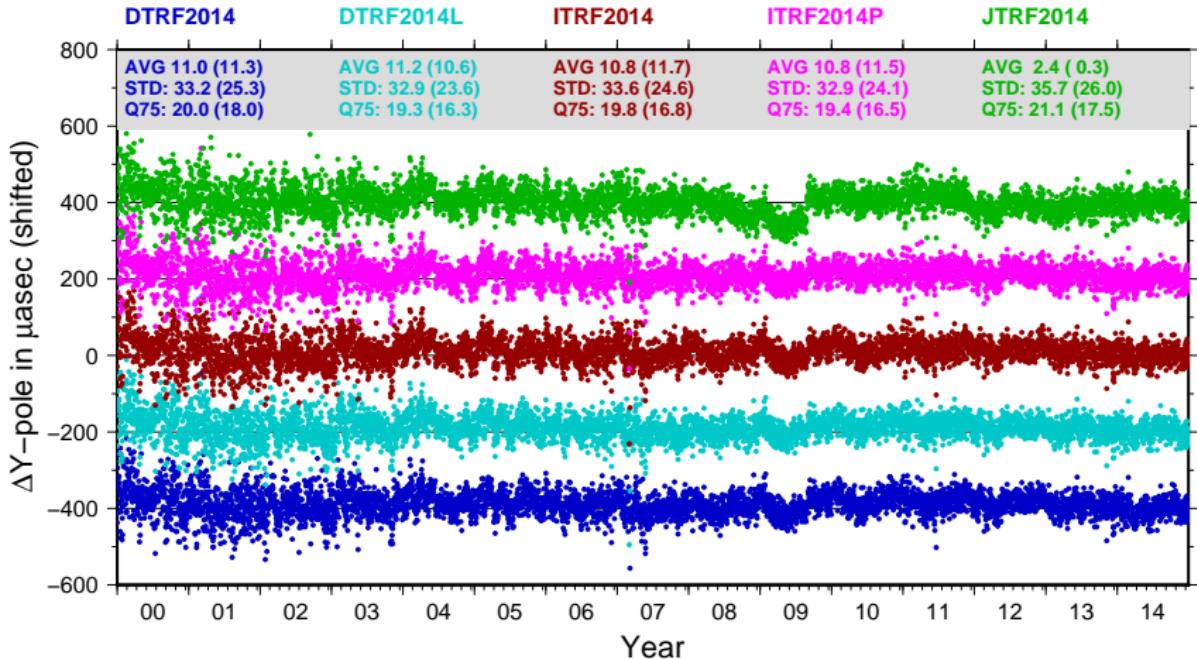
- The **polar motion estimates** can be compared with the values provided within the respective **reference frame solution** in order to obtain a measure for the **self-consistency**.
- The **polar motion estimates** can of course also be **directly compared** to each other in order to detect differences due to the orientation (**stability**) of the reference frame solutions.

# Consistency of ERP series



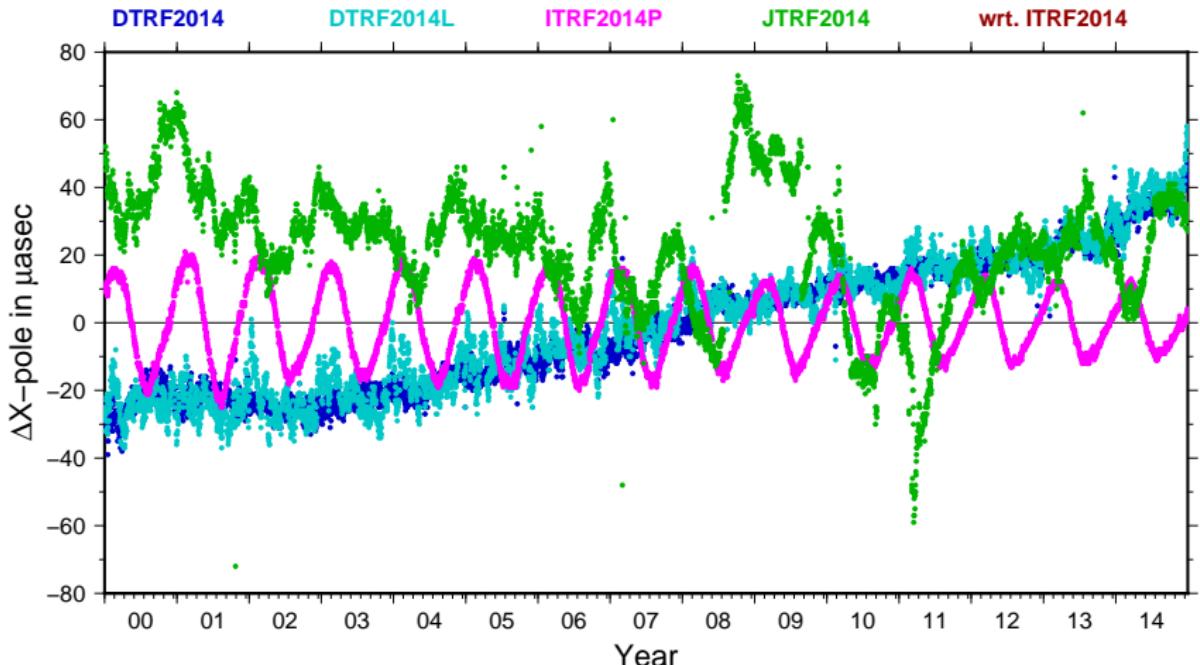
Number in brackets are computed from the time interval from epoch 2010.0 onwards.

# Consistency of ERP series



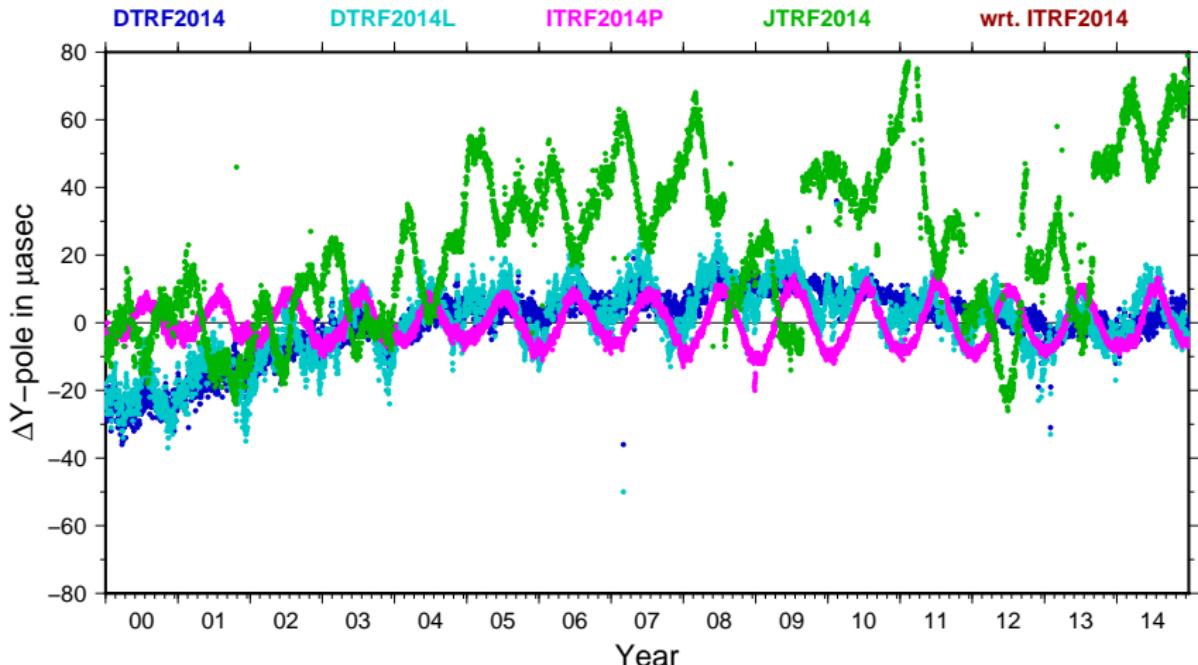
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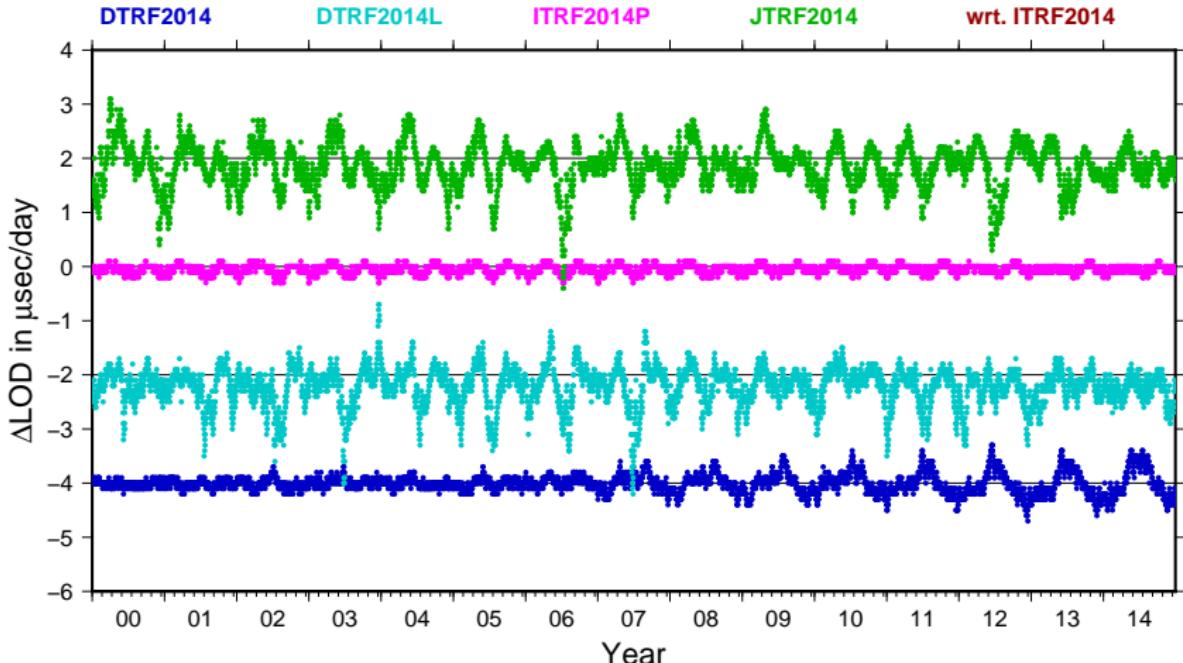
The reference ITRF2014 was arbitrary chosen.

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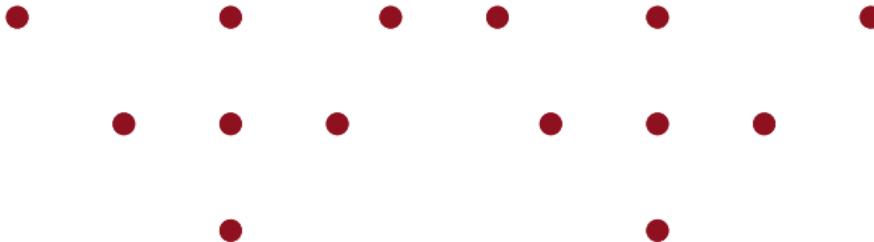
# Consistency of ERP series



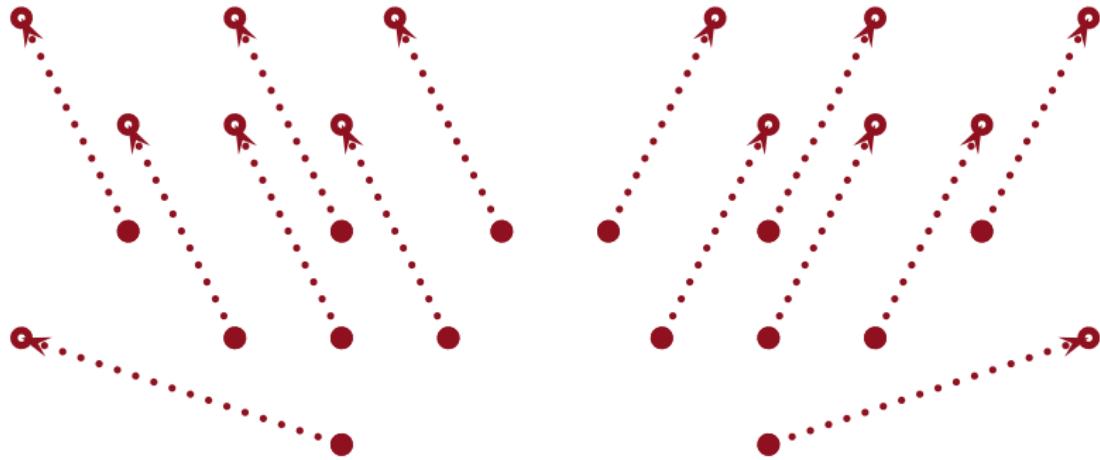
The reference ITRF2014 was arbitrary chosen.

# Evaluating the long-term stability

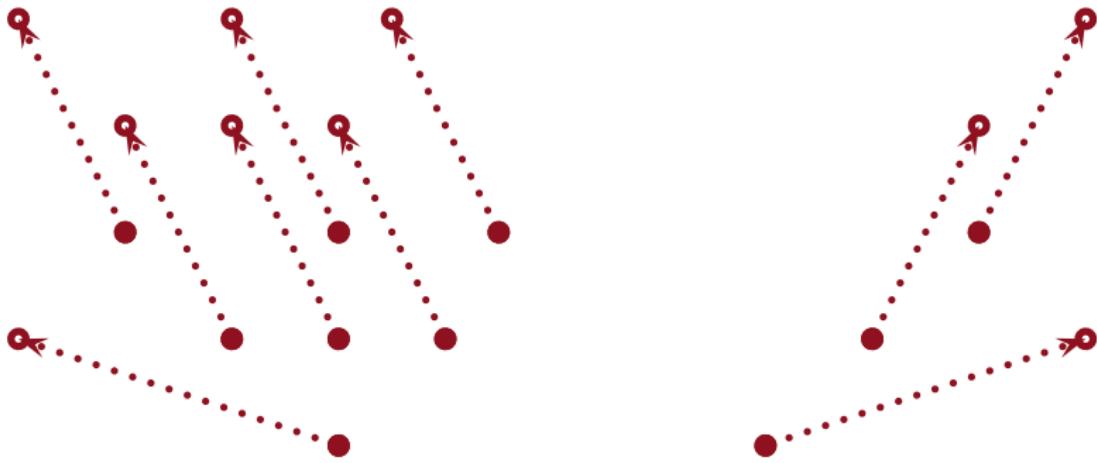
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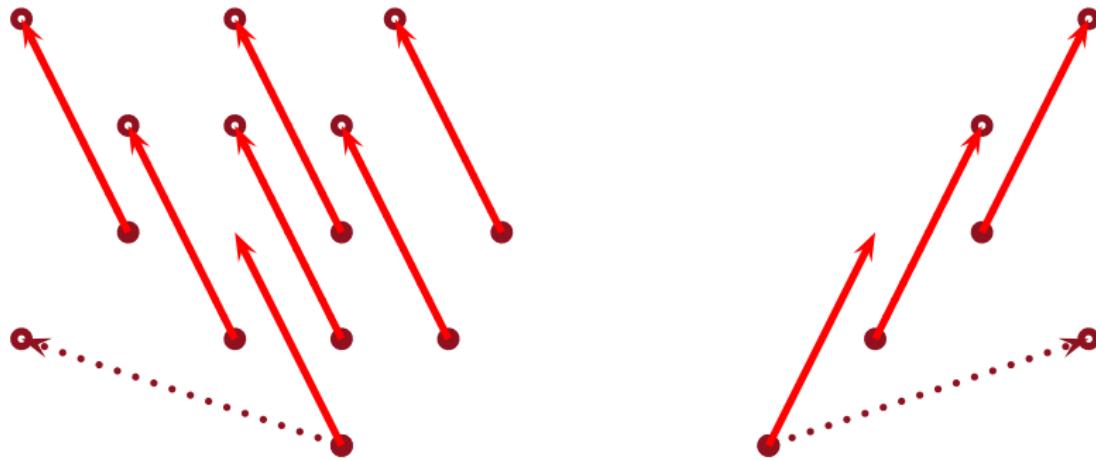
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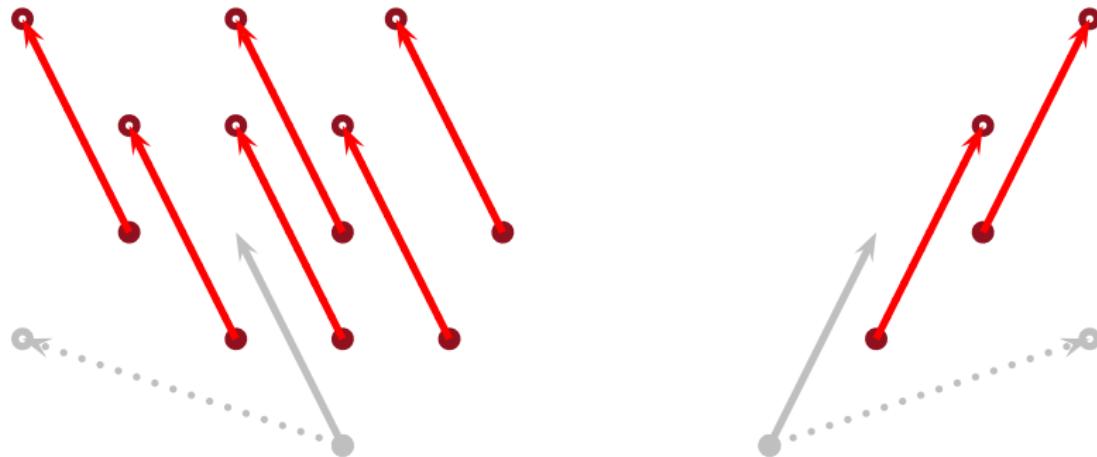


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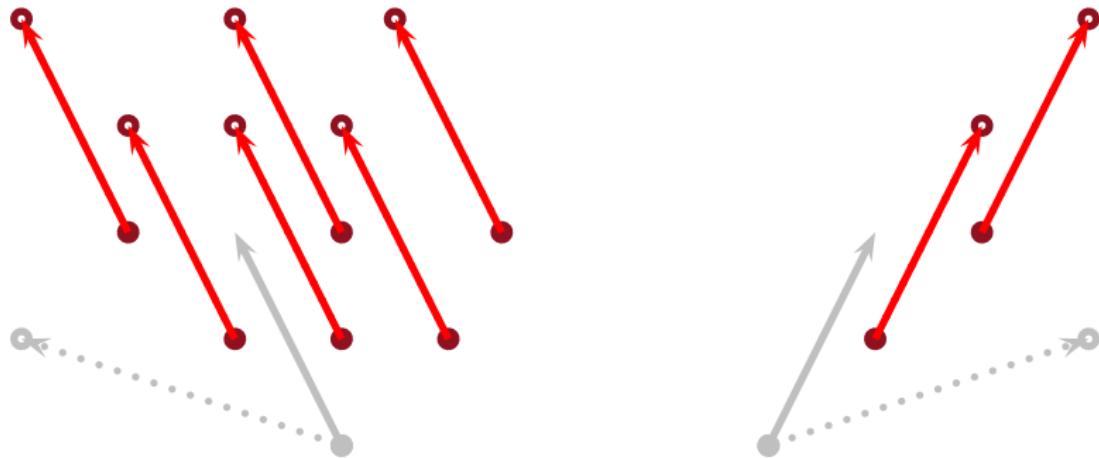
- The NNR-Nuvel1A model is assumed to be free of rotations.

# Evaluating the long-term stability



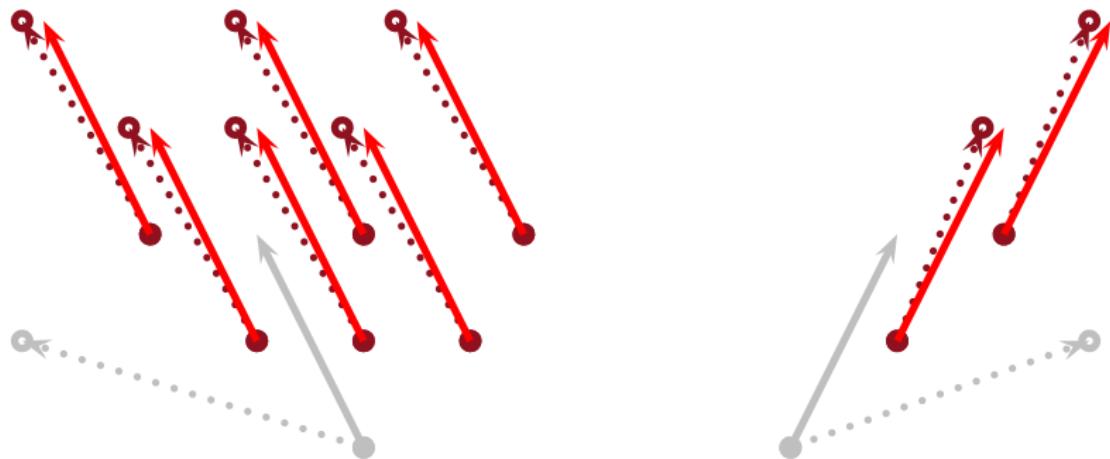
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# Evaluating the long-term stability



- The NNR-Nuvel1A model is assumed to be free of rotations.
- Since there are no rotations the reference frame solution wrt. the NNR vector field it is supposed to be a NNR-reference frame solution.

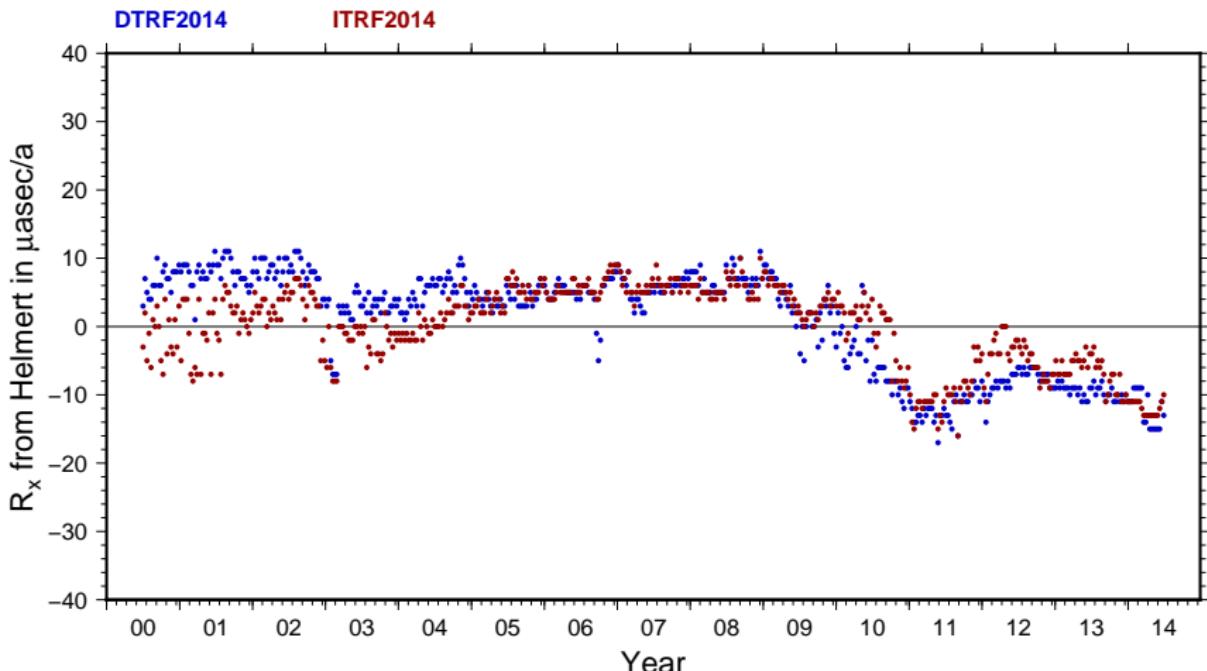
# Evaluating the long-term stability



- The NNR-Nuvel1A model is assumed to be free of rotations.
- If there are no rotations the reference frame solution wrt. the NNR vector field it is supposed to be a NNR-reference frame solution.
- If there are constant rotations the NNR condition either in the reference frame solution or in the NNR-Nuvel1A model is not satisfied.

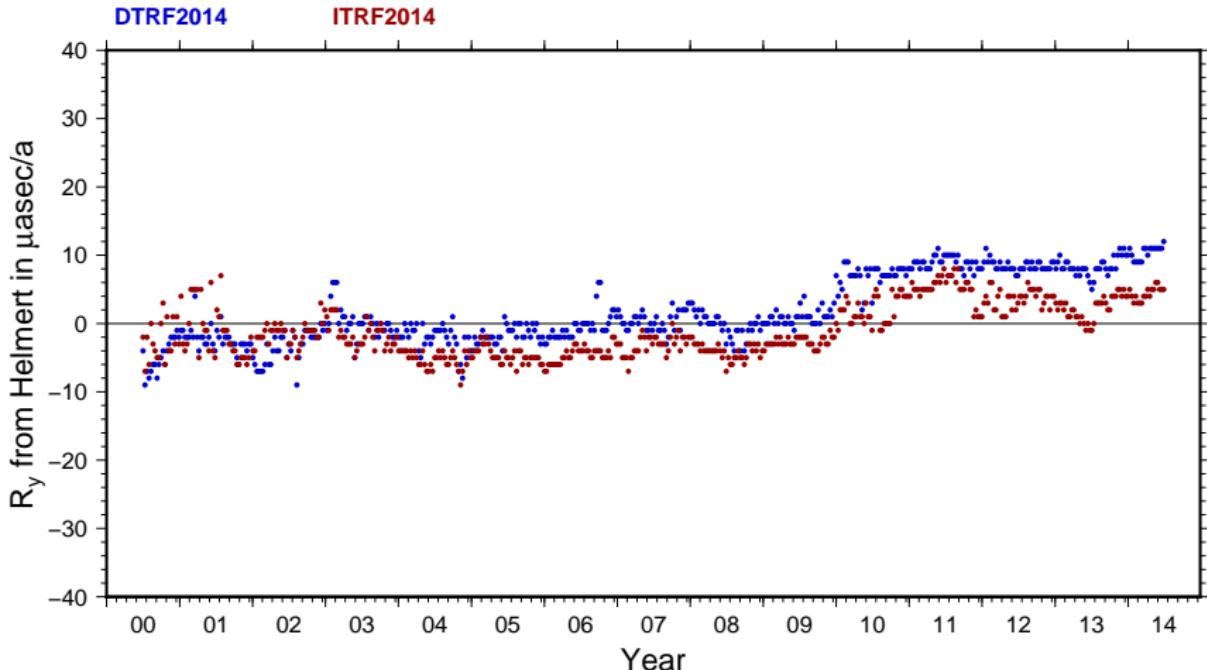
# Evaluating the long-term stability

Rotations in X



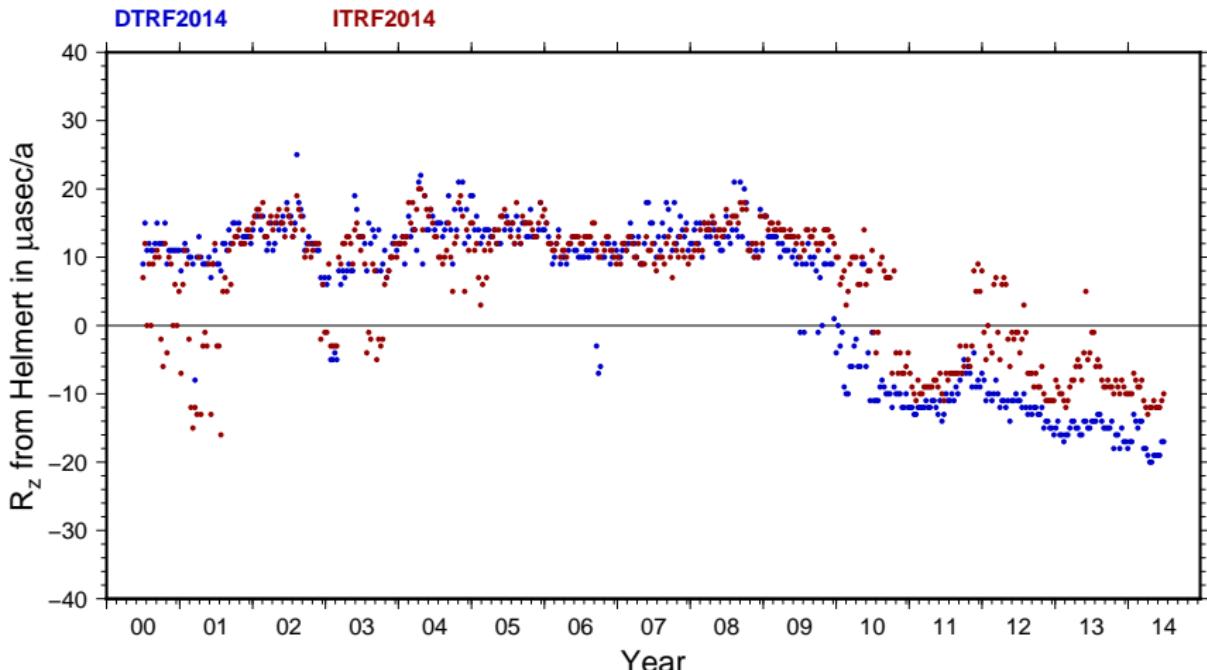
# Evaluating the long-term stability

Rotations in Y



# Evaluating the long-term stability

## Rotations in Z



# Acknowledgment

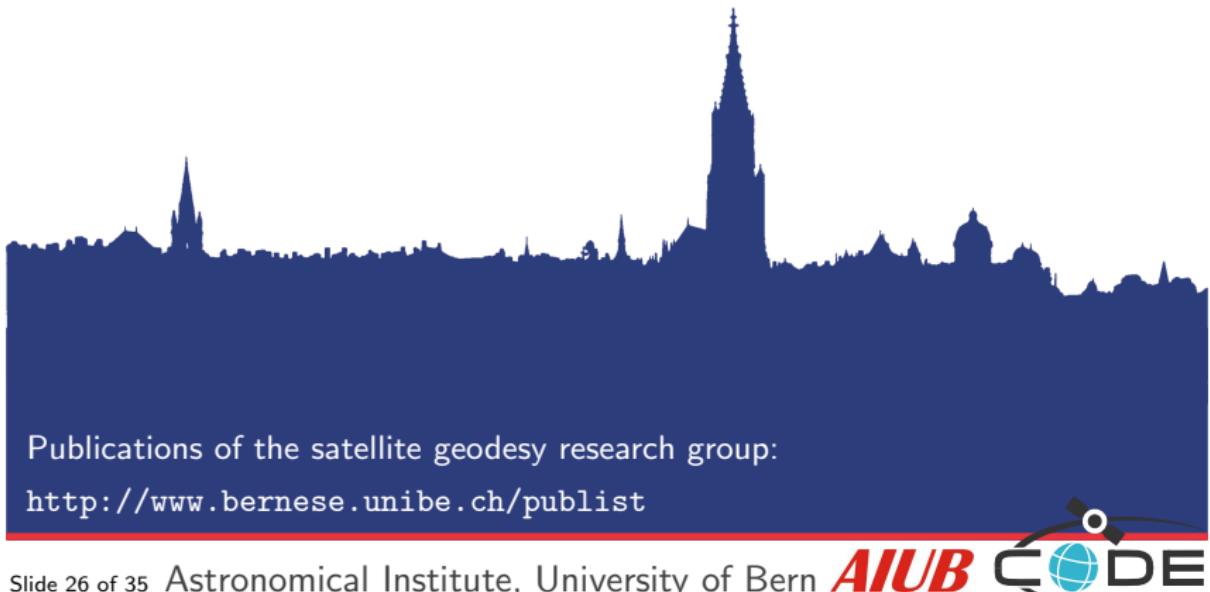
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We are grateful to the groups providing their reference frame solutions and accomplishing information used for this evaluation study, namely

- Z. Altamimi (IGN, France),
- C. Abbondanza (JPL, USA) as well as
- M. Bloßfeld and M. Seitz (DGFI-TUM, Germany).

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# THANK YOU for your attention



Publications of the satellite geodesy research group:

<http://www.bernese.unibe.ch/publist>

# xTRF2014 Solution Characterization

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**DOGS-CS**: combination of normal equations

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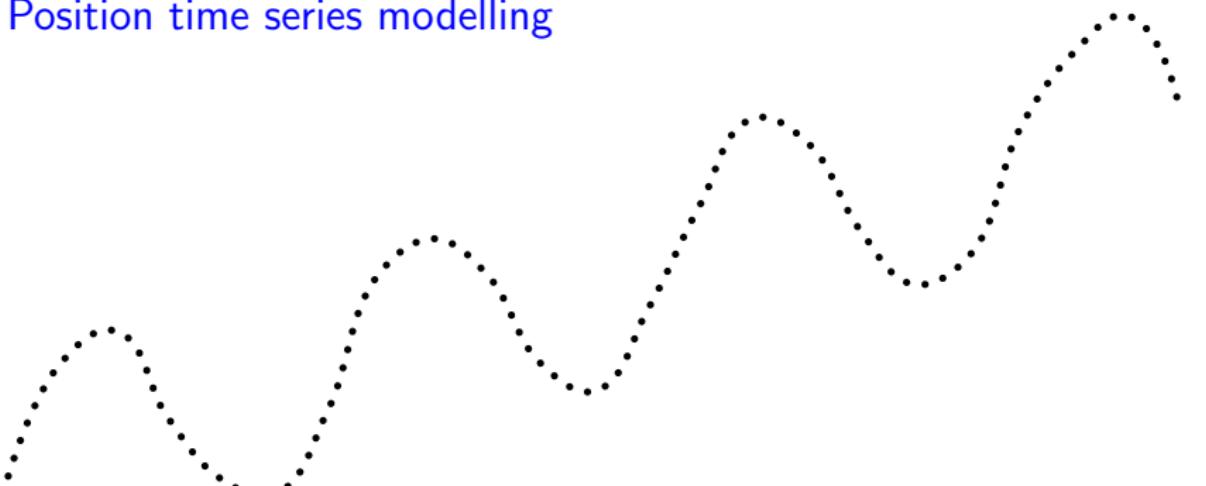
- **JTRF2014**

Jet Propulsion Laboratory (JPL, USA; Wu et al. 2015)

**CATREF+KALMAN**: combination of solutions

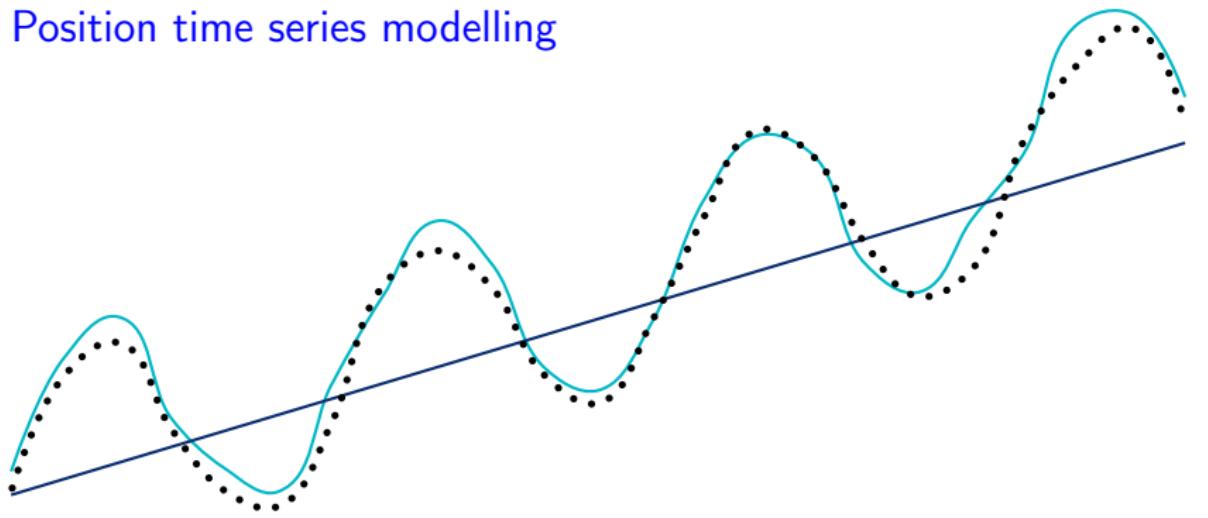
# xTRF2014 Solution Characterization

## Position time series modelling



# xTRF2014 Solution Characterization

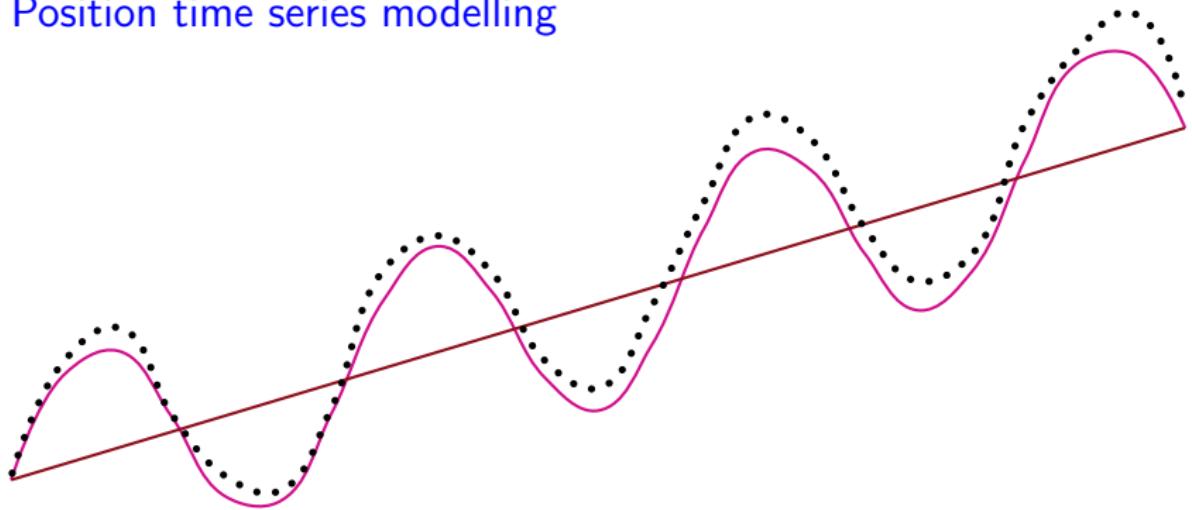
## Position time series modelling



- DTRF2014: linear velocities and external geophysical models

# xTRF2014 Solution Characterization

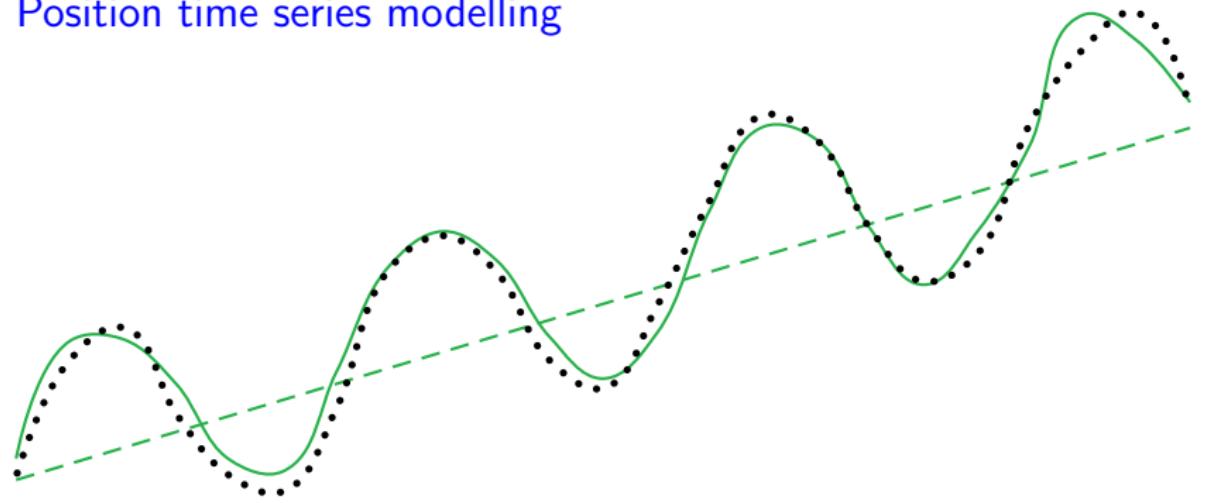
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- ITRF2014: linear velocities and empirical periodic functions

# xTRF2014 Solution Characterization

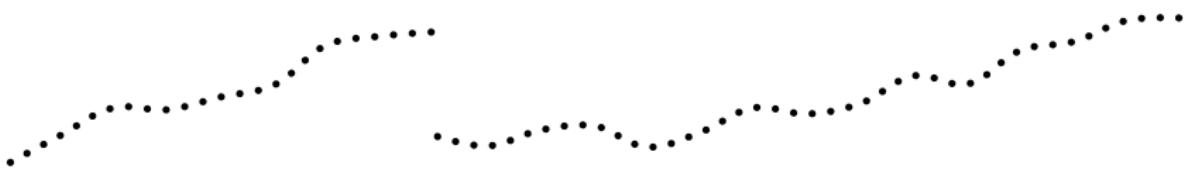
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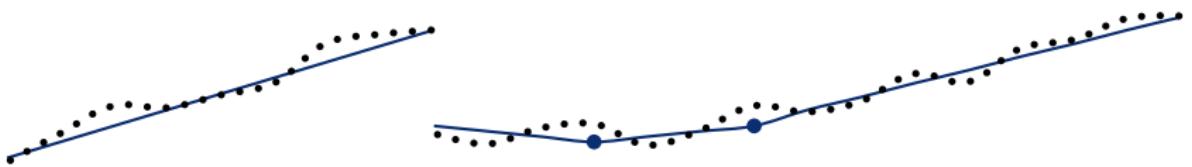
- DTRF2014: linear velocities and external geophysical models
- ITRF2014: linear velocities and empirical periodic functions
- JTRF2014: filter based on epoch-to-epoch changes

# xTRF2014 Solution Characterization

## Handling of Earthquakes

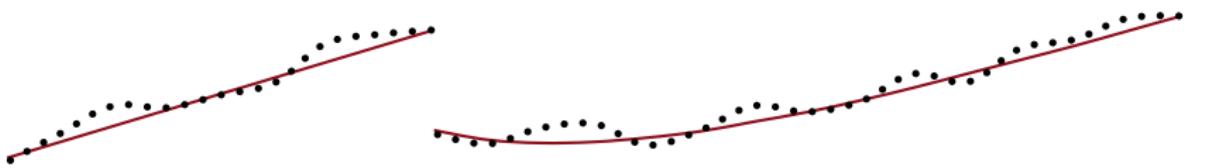


## Handling of Earthquakes



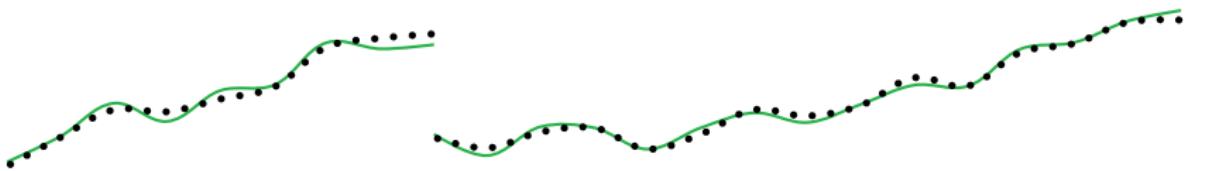
- DTRF2014: a sequence of linear velocities

## Handling of Earthquakes



- DTRF2014: a sequence of linear velocities
- ITRF2014: empirical deformation models (PSD)

## Handling of Earthquakes



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# xTRF2014 Solution Characterization

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- **DTRF2014**

Geophysical modeling of the position time series: e.g., use of geophysical models for non-tidal loading effects (NT-L)

- + good approximation of the regularized station position by considering NT-L
- global models do not cover regional effects; limited accuracy of the models

- **DTRF2014**

Geophysical modeling of the position time series: e.g., use of geophysical models for non-tidal loading effects (NT-L)

- **ITRF2014**

Advanced mathematical modeling of the position time series:  
e.g., approximation of post-seismic deformation (PSD) via empirical models

- + PSD models help to avoid discontinuities
- estimated annual signals may contain non-geophysical contributions

# xTRF2014 Solution Characterization

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Geophysical modeling of the position time series: e.g., use of geophysical models for non-tidal loading effects (NT-L)

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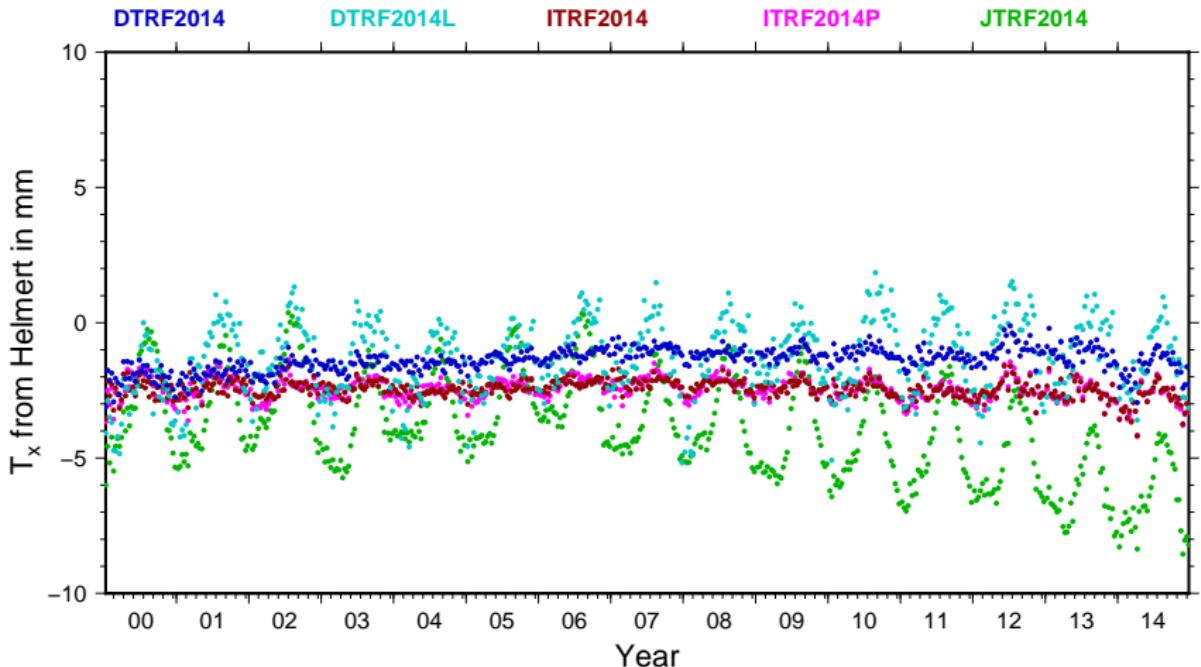
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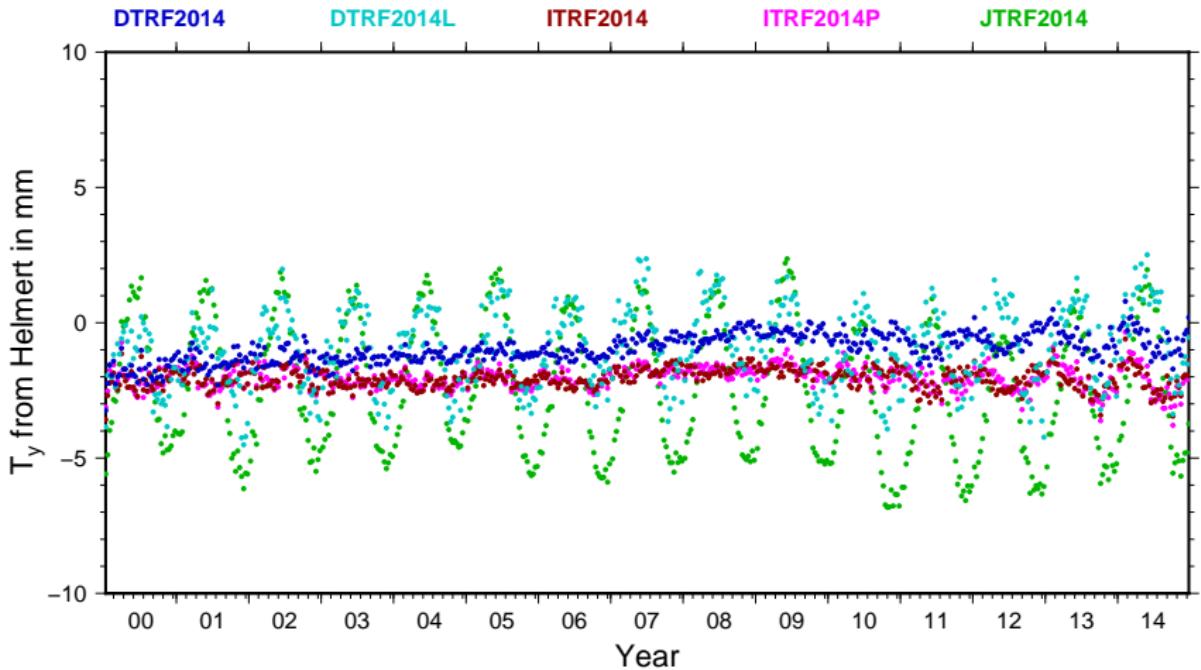
Advanced mathematical modeling of the position time series:  
e.g., weekly estimation of station coordinates

- + good approximation of the regularized station position
- uncertainty of geodetic datum; difficult extrapolation

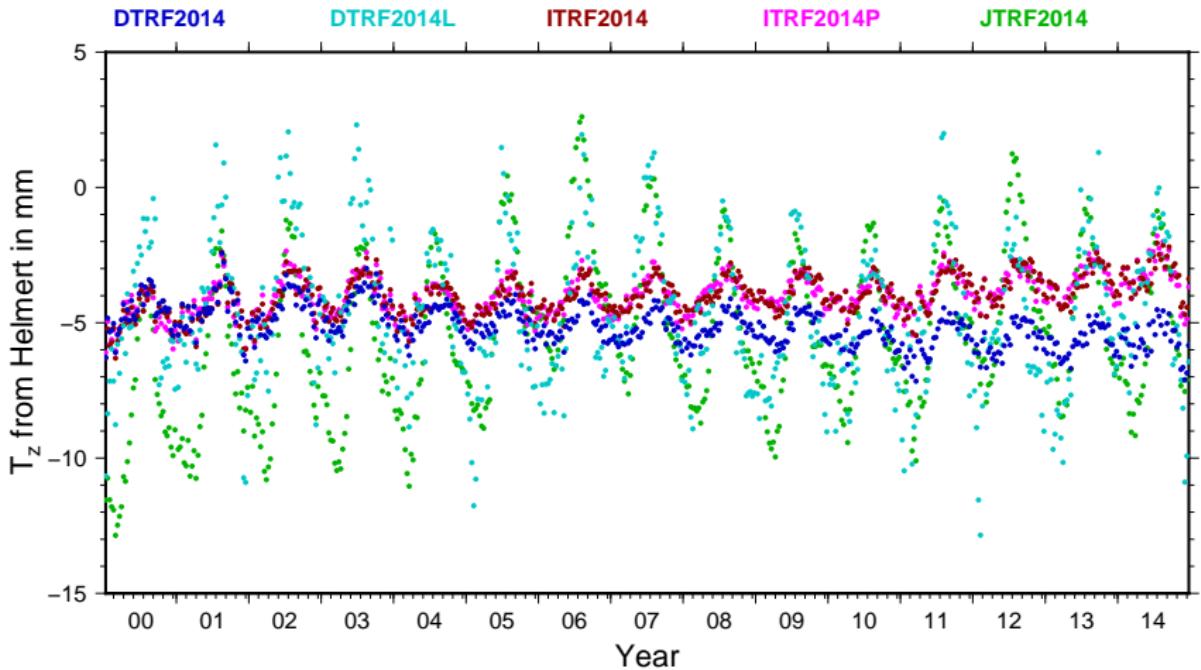
# Comparison of EGIEM solution (IGb08)



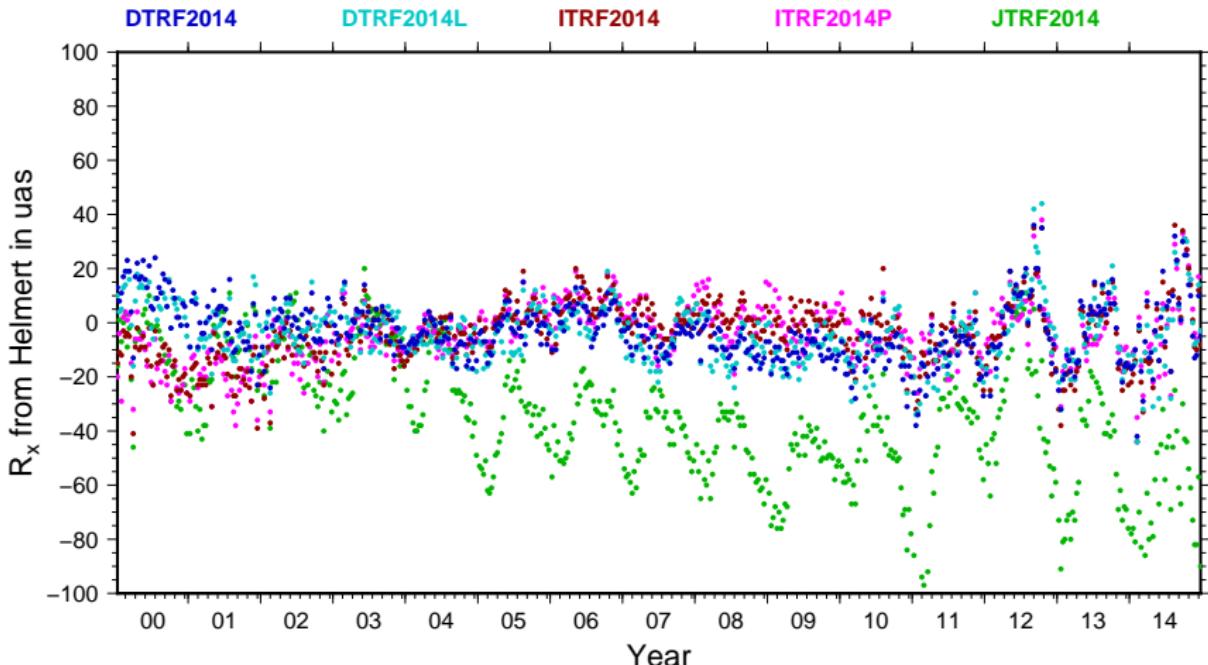
# Comparison of EGIEM solution (IGb08)



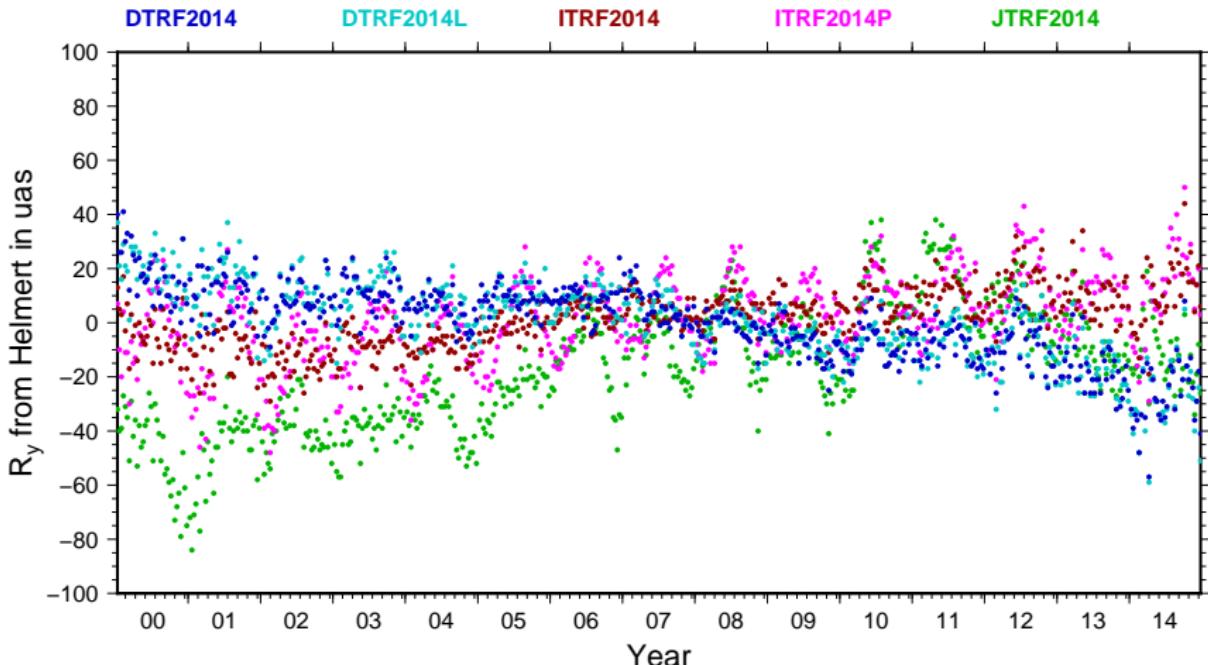
# Comparison of EGIEM solution (IGb08)



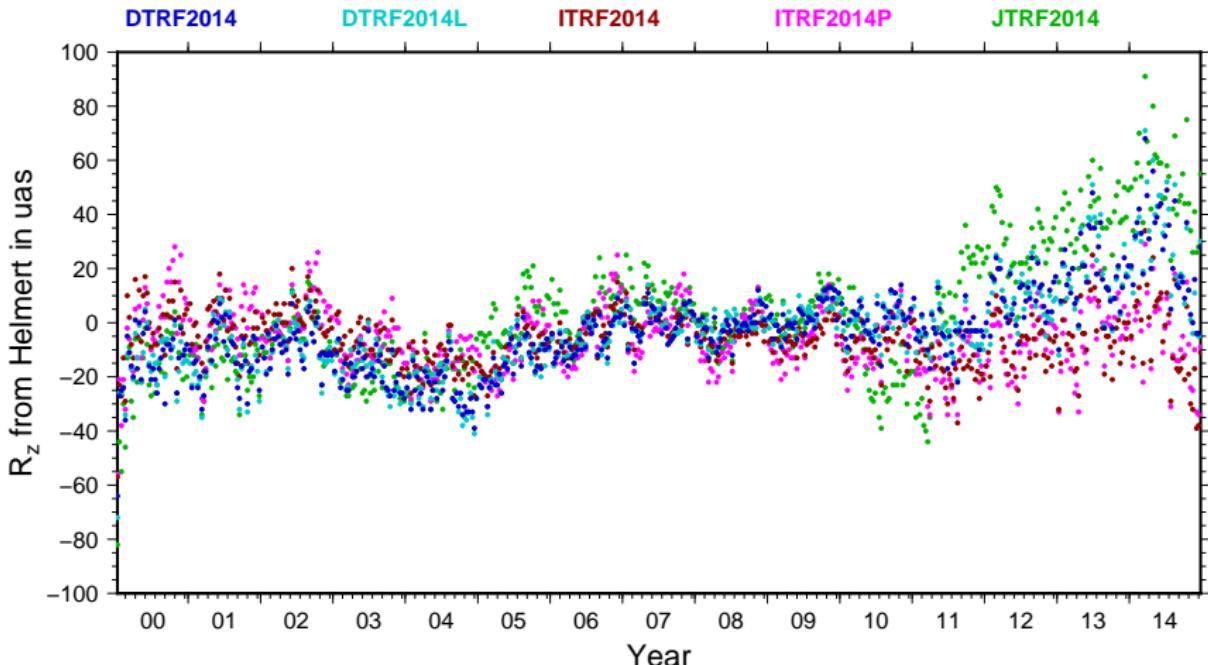
# Comparison of EGIEM solution (IGb08)



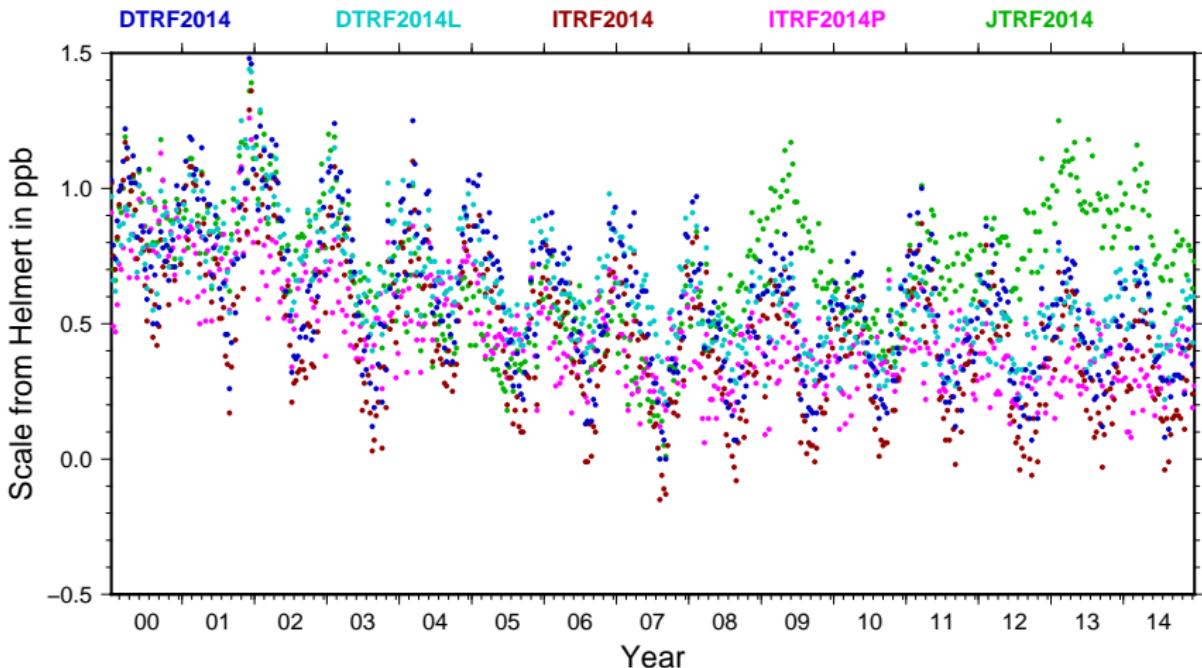
# Comparison of EGIEM solution (IGb08)



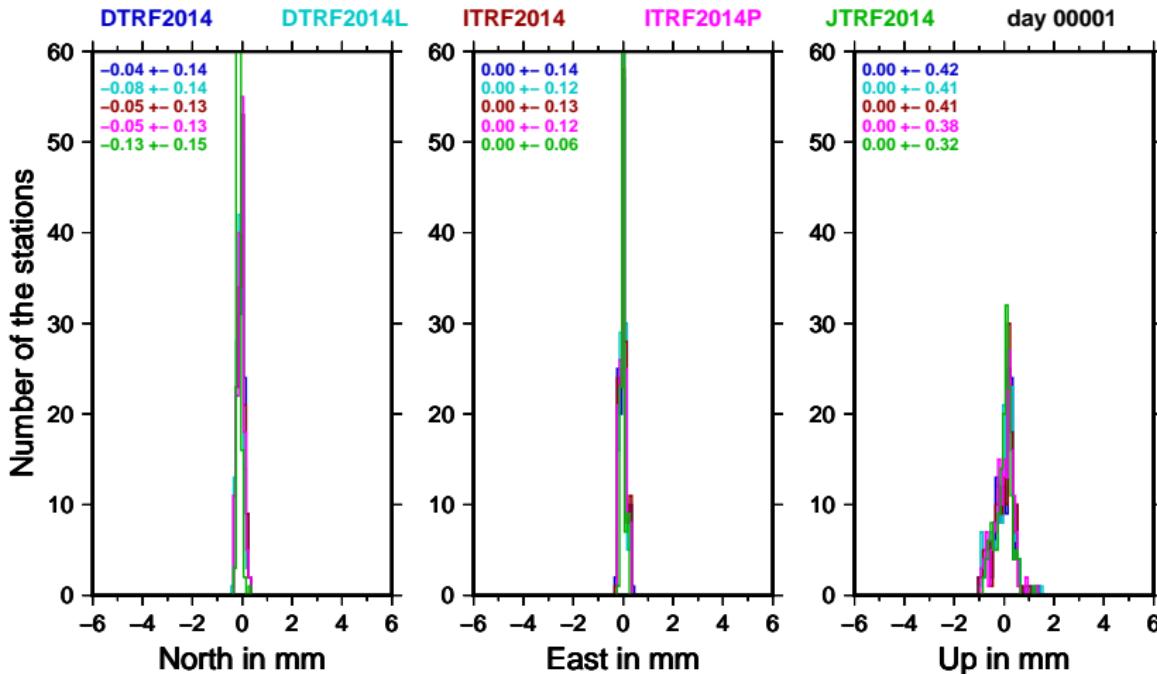
# Comparison of EGIEM solution (IGb08)



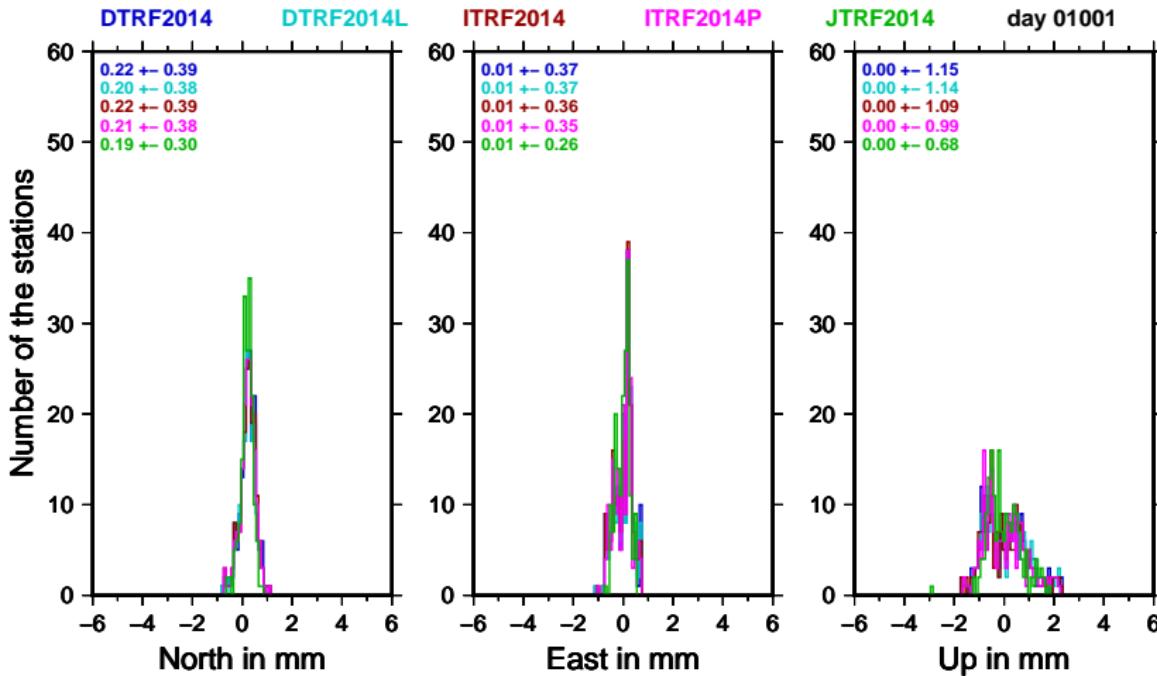
# Comparison of EGIEM solution (IGb08)



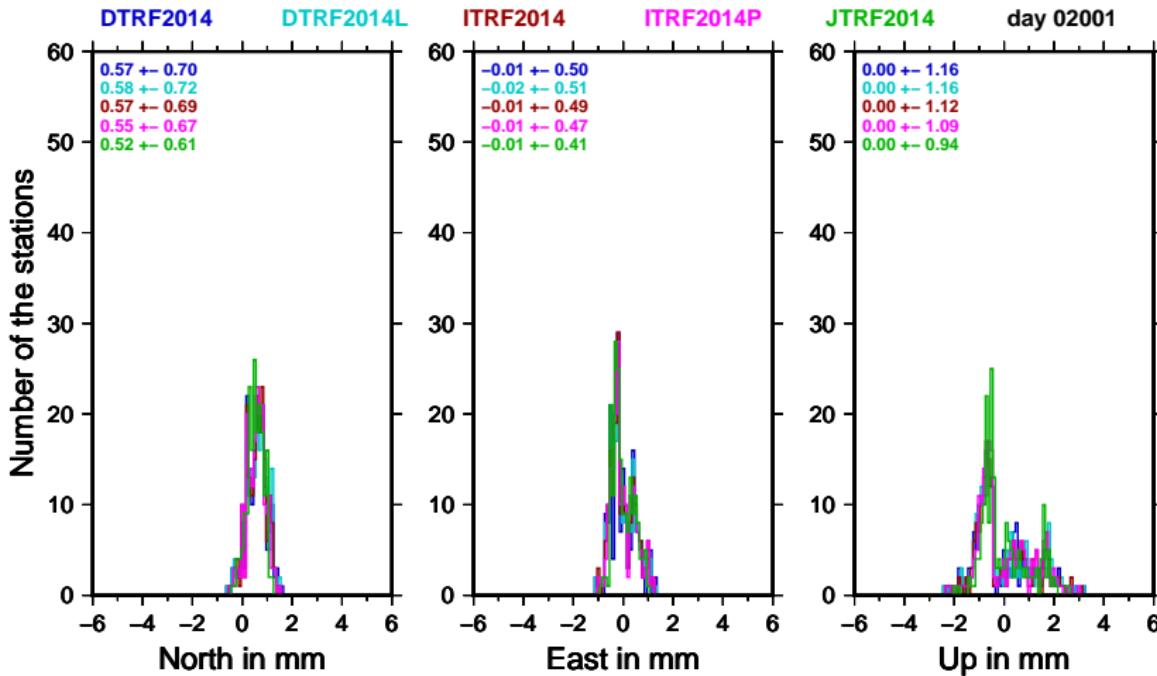
# Comparison of station coordinates



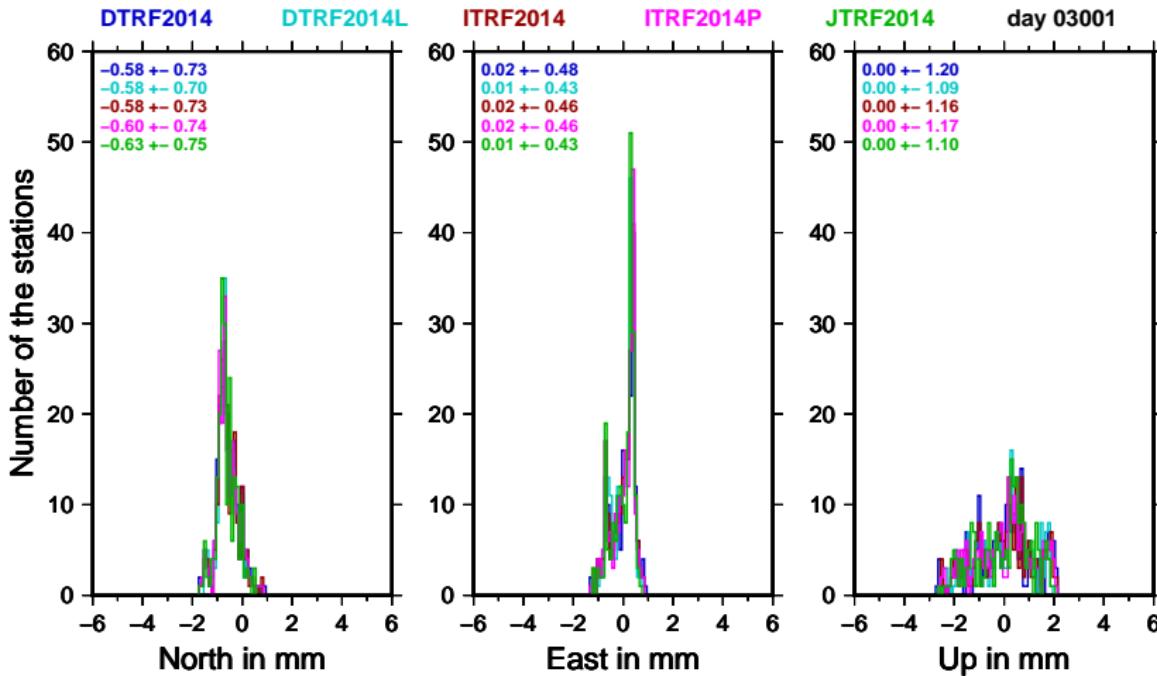
# Comparison of station coordinates



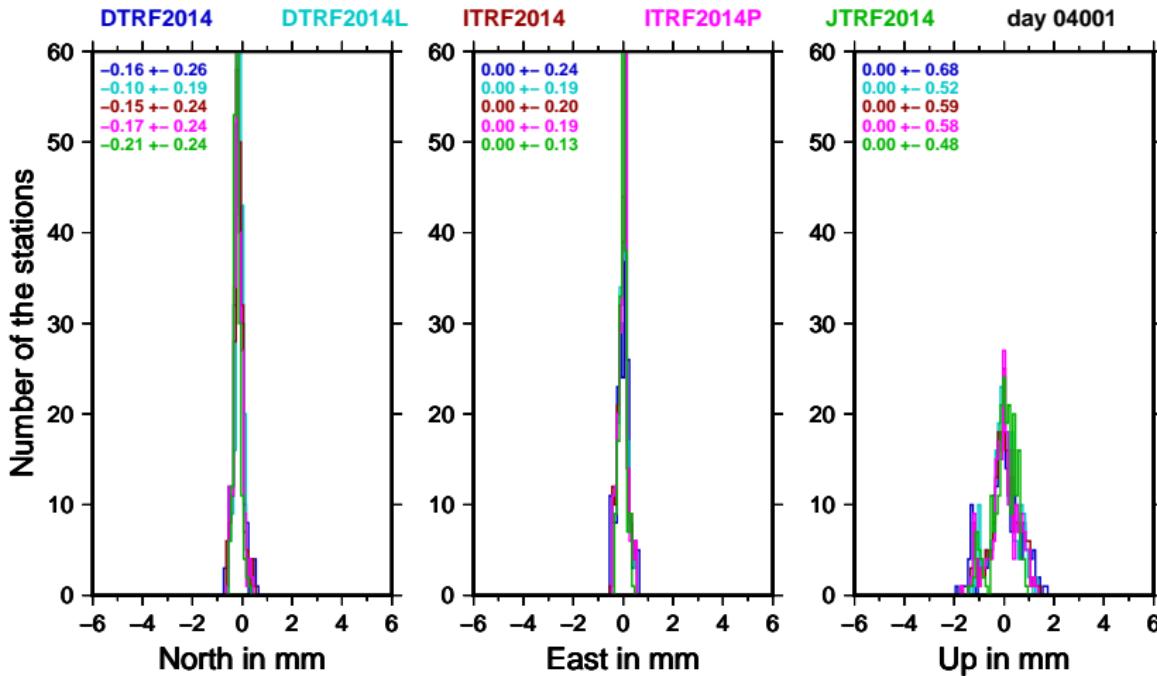
# Comparison of station coordinates



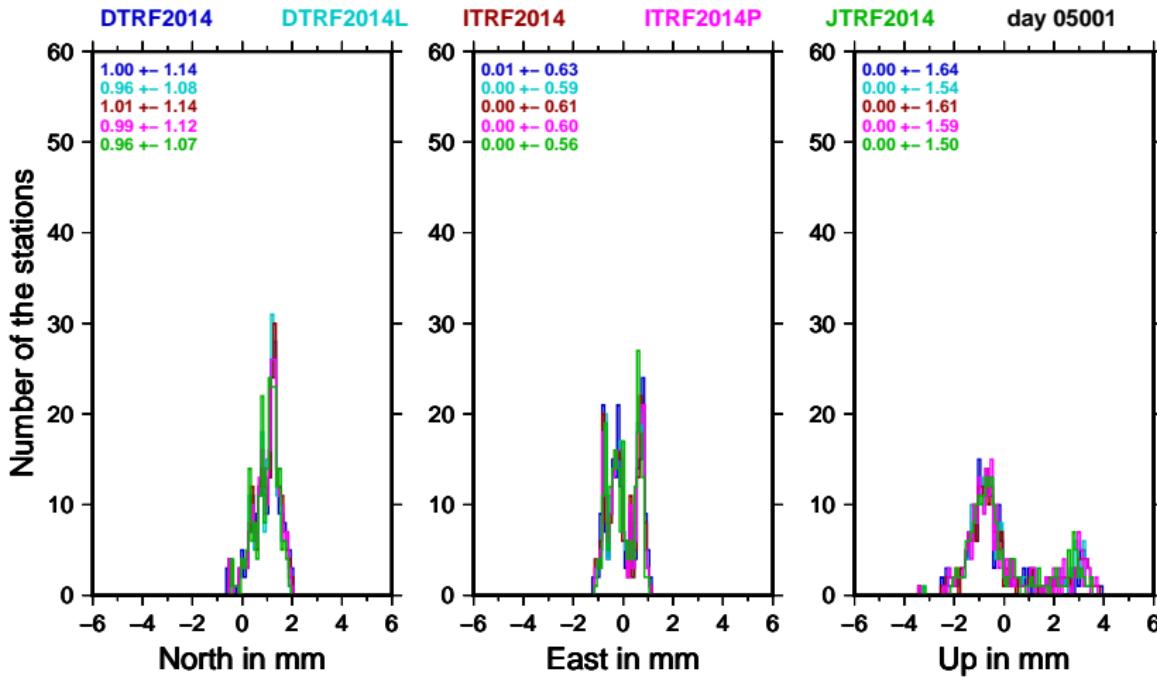
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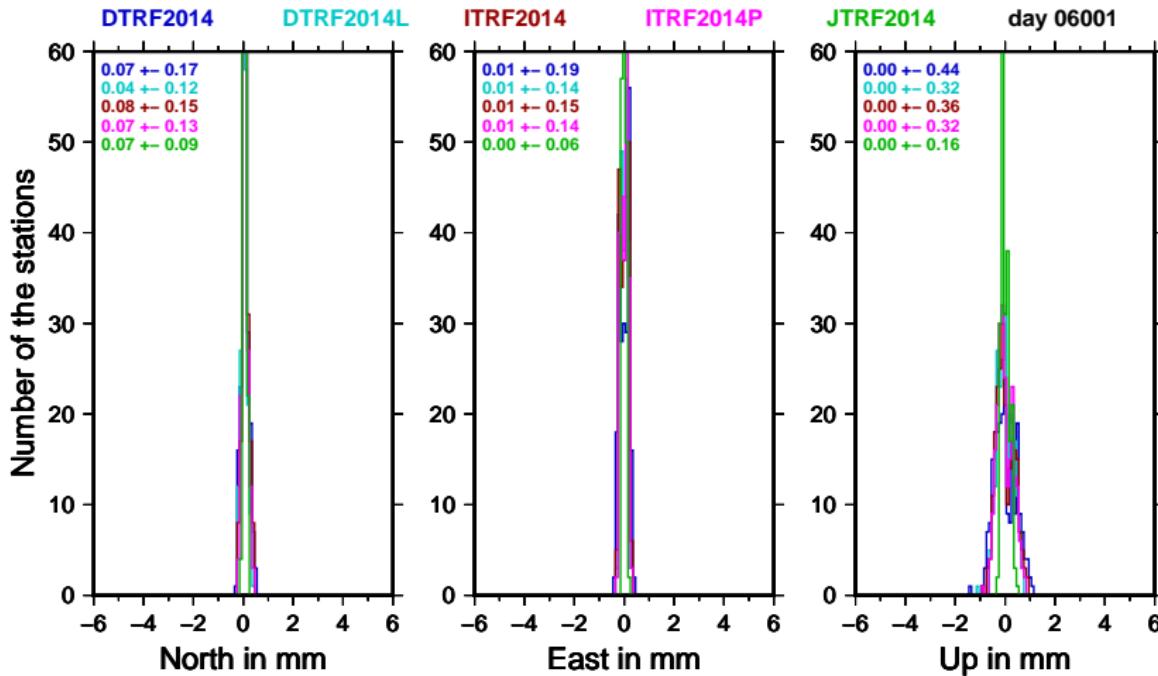
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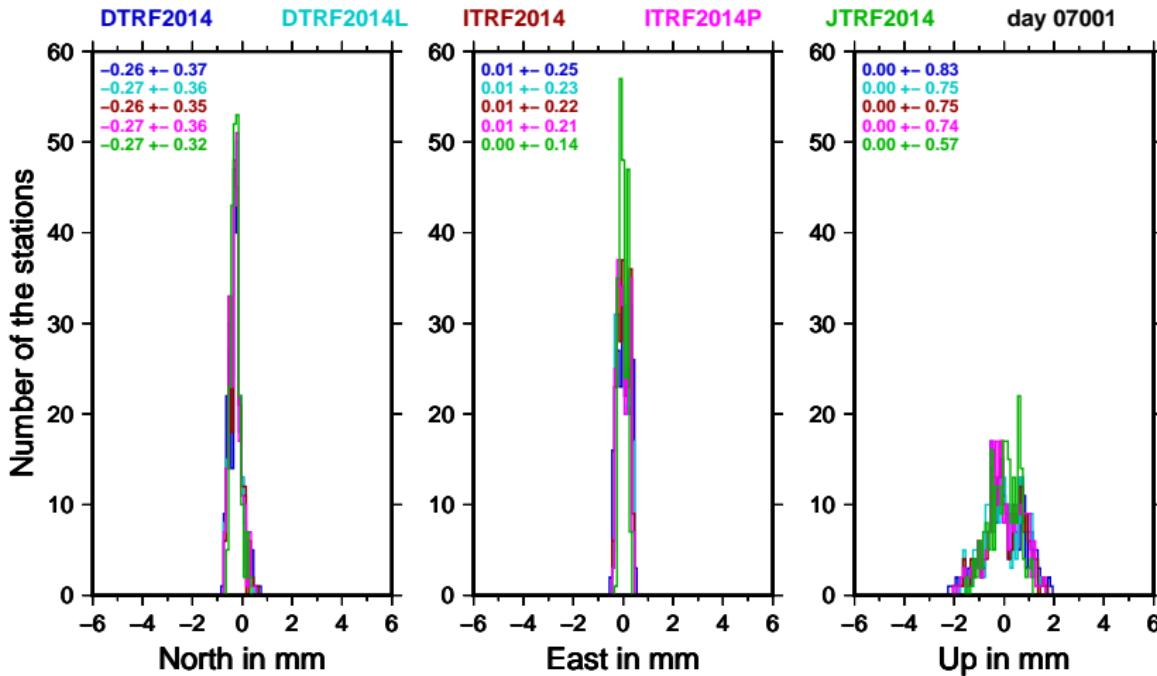
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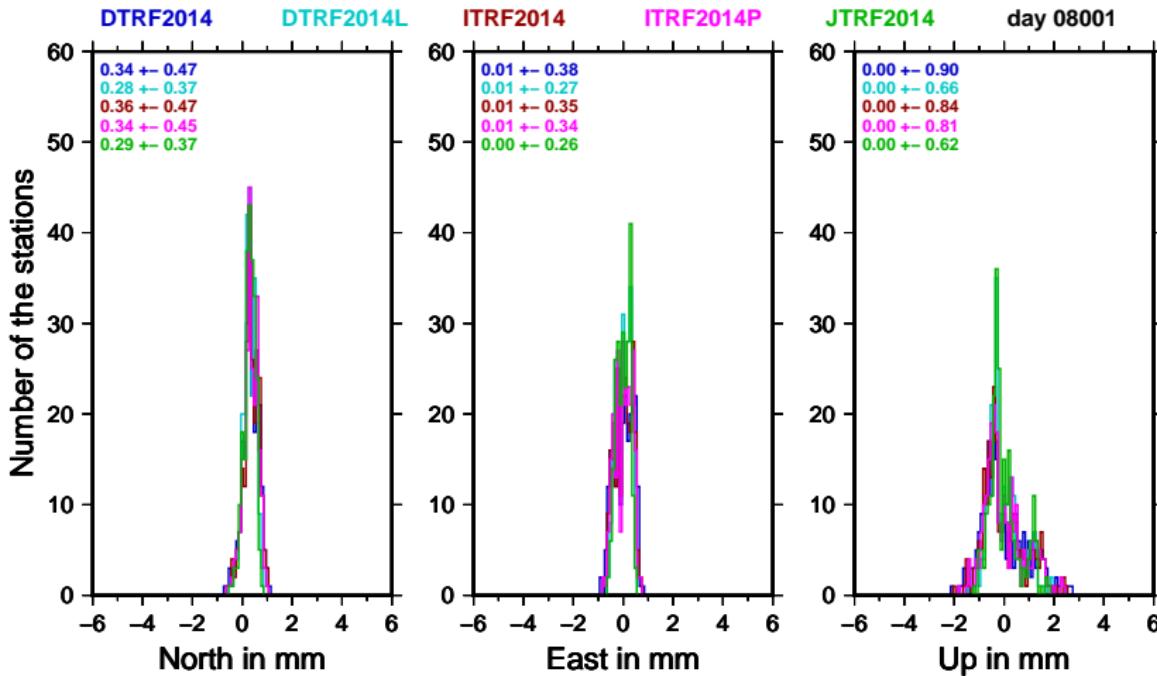
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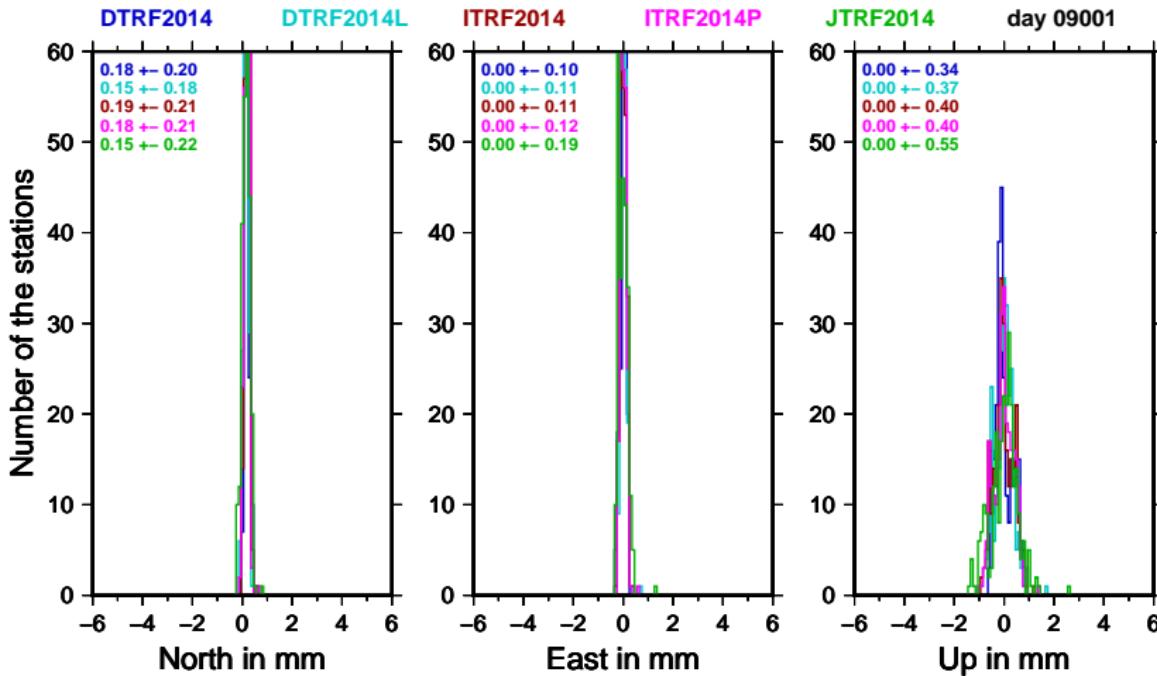
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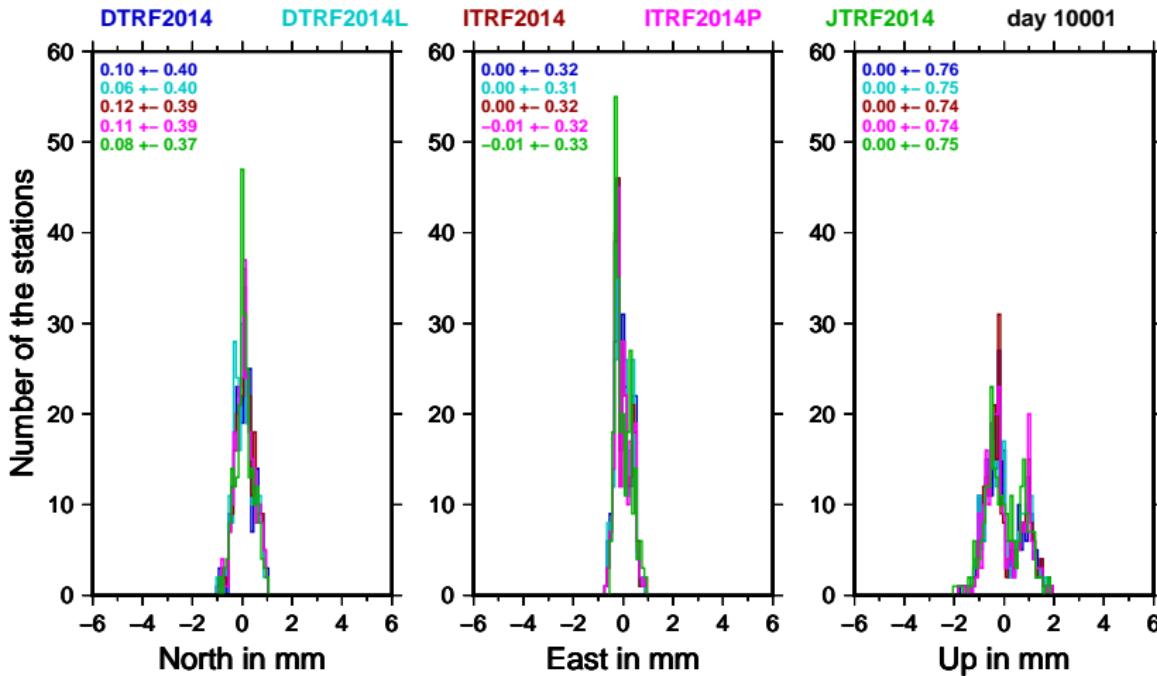
# Comparison of station coordinates



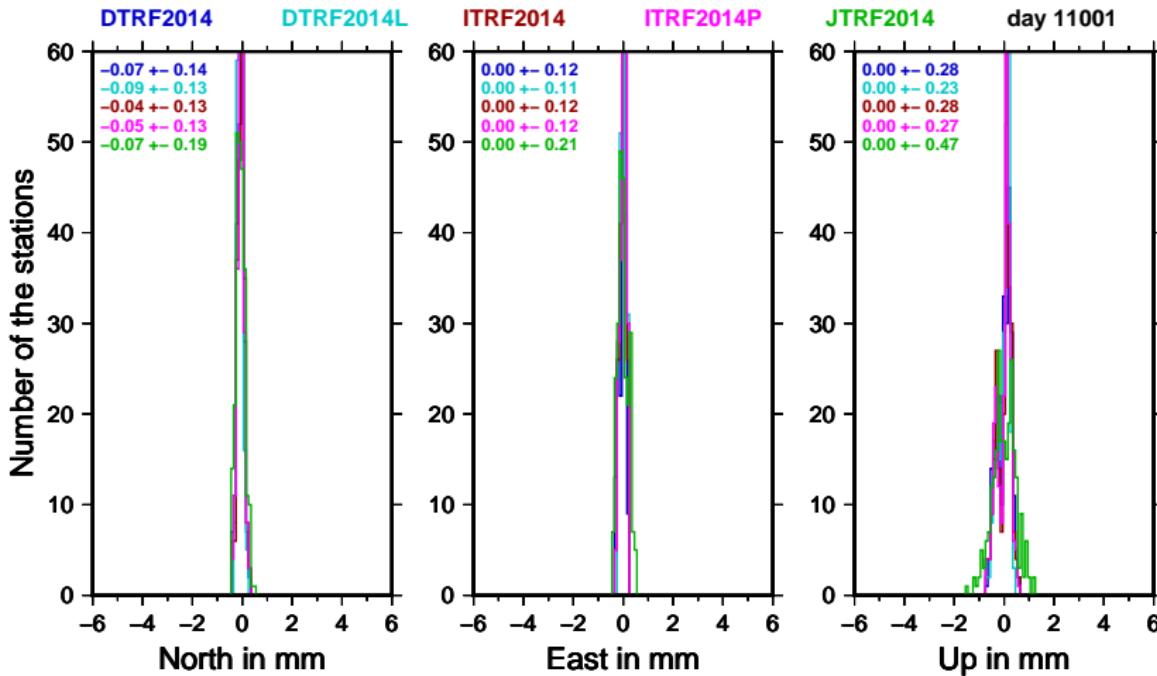
# Comparison of station coordinates



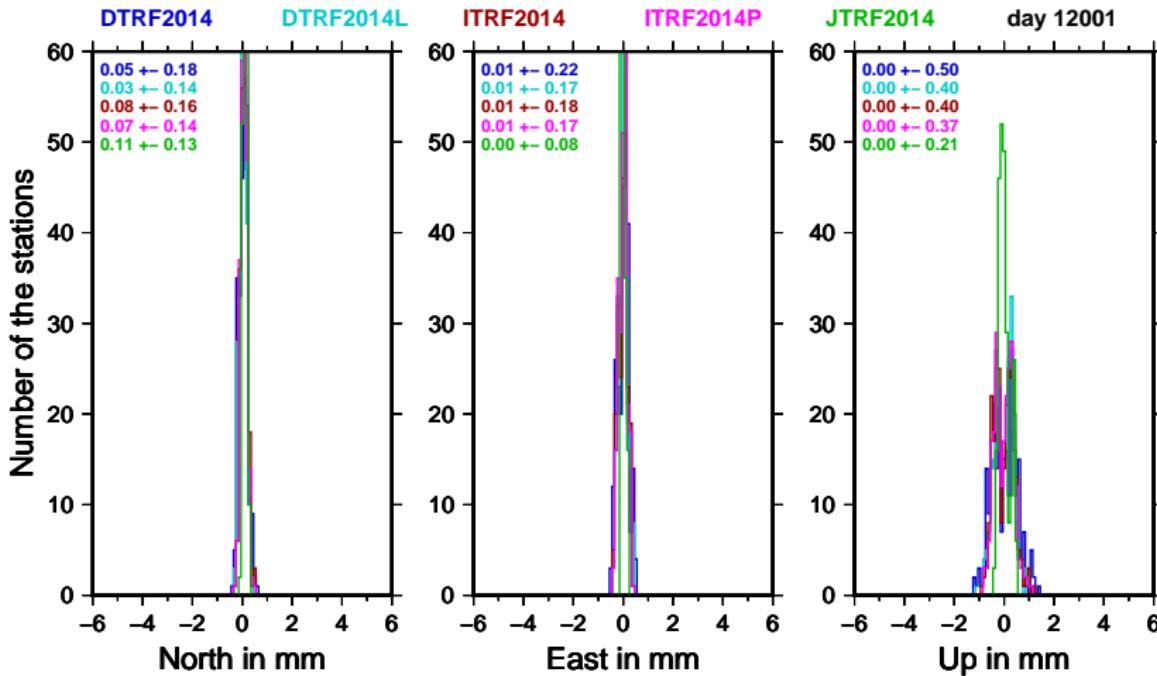
# Comparison of station coordinates



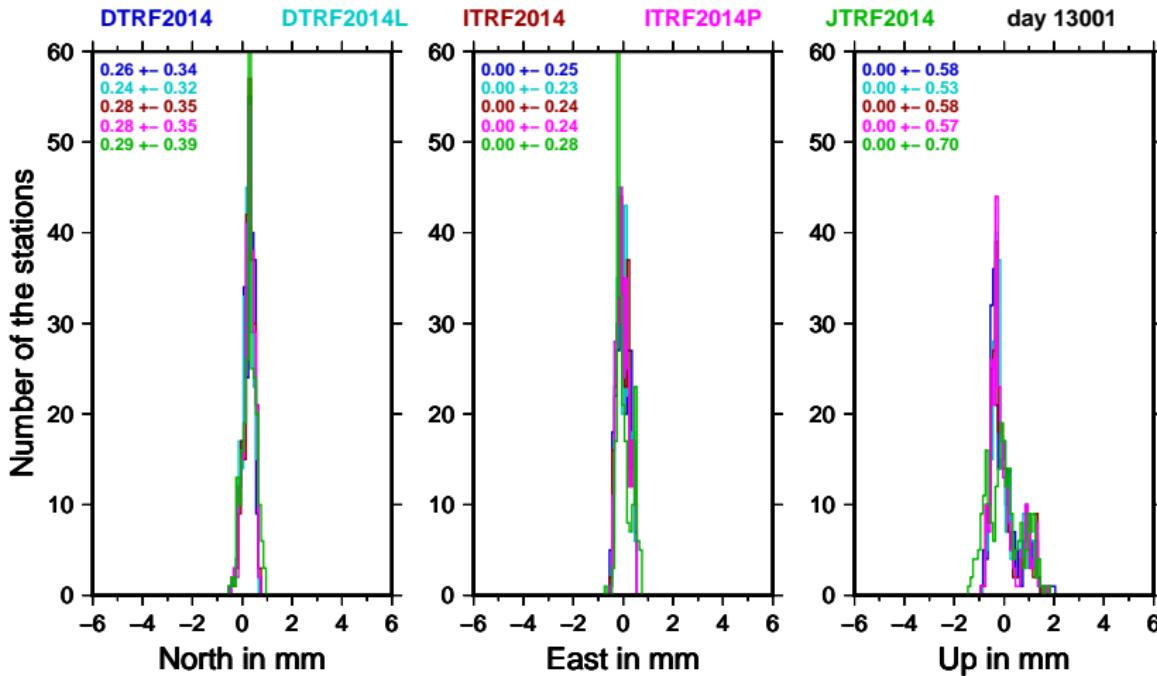
# Comparison of station coordinates



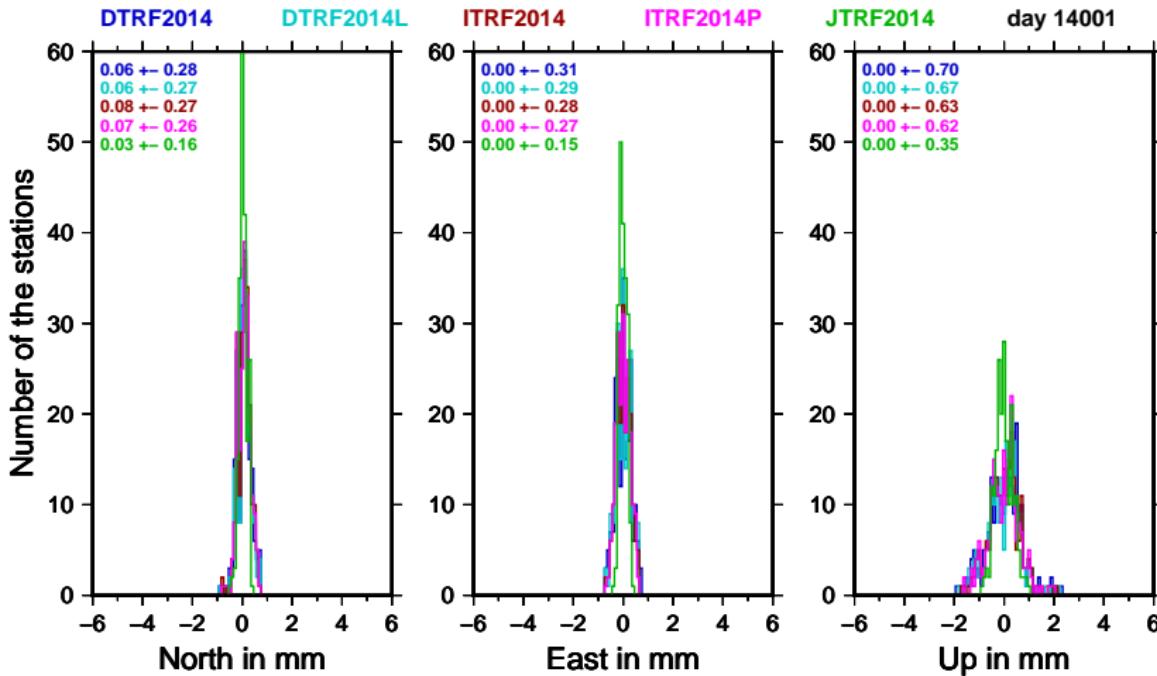
# Comparison of station coordinates



# Comparison of station coordinates

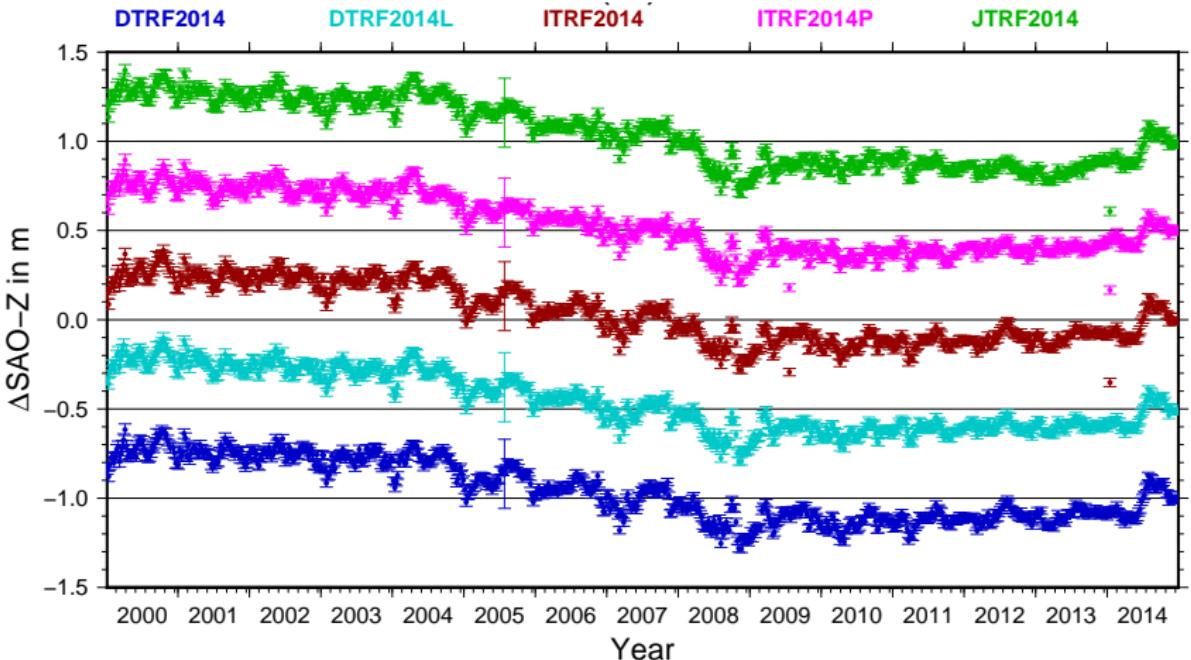


# Comparison of station coordinates



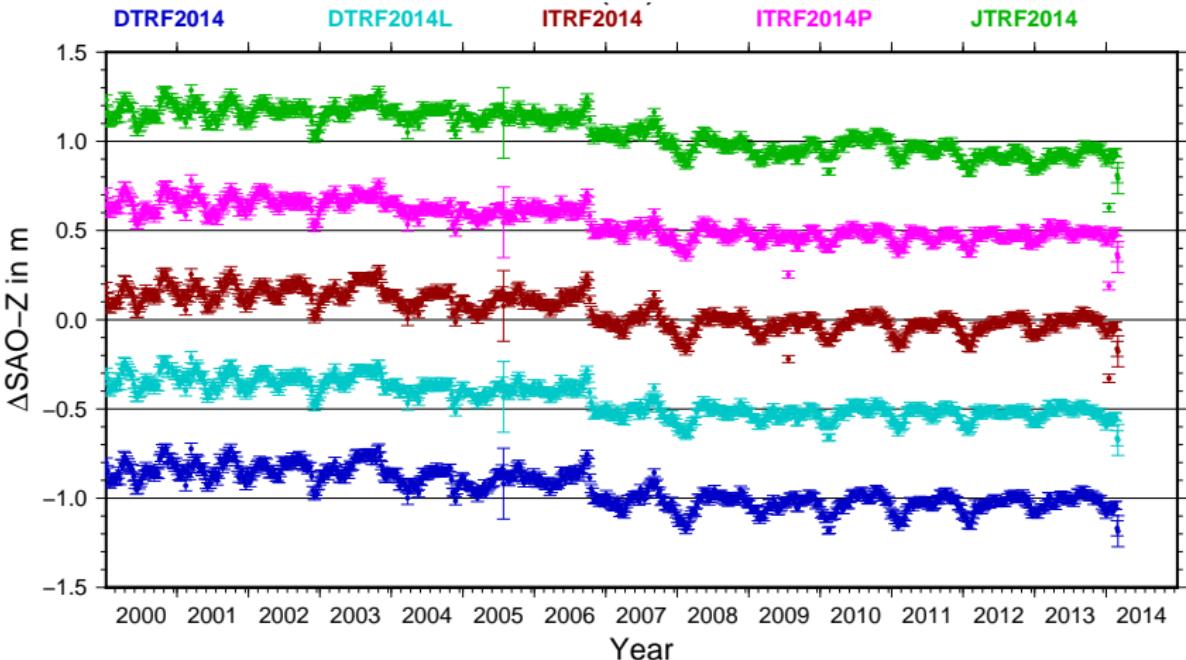
# Estimated satellite antenna Z-offset series

Satellite SVN G 034



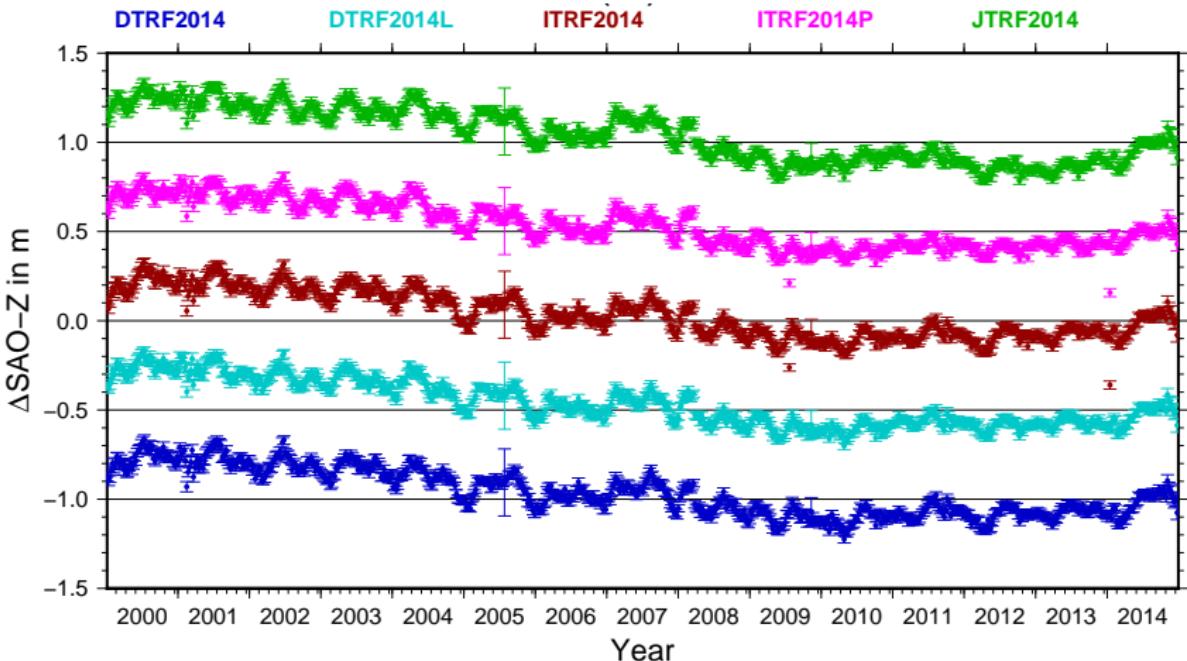
# Estimated satellite antenna Z-offset series

Satellite SVN G 036



# Estimated satellite antenna Z-offset series

Satellite SVN G 038



# Estimated satellite antenna Z-offset series

Satellite SVN G 039

