

Combined analysis of GNSS and SLR data using satellite co-locations

D. Thaller ¹⁾, R. Dach ¹⁾, M. Seitz ²⁾,
G. Beutler ¹⁾, M. Mareyen ³⁾, B. Richter ³⁾

(1) Astronomical Institute, University of Bern (AIUB), Switzerland

(2) Deutsches Geodätisches Forschungsinstitut (DGFI), München, Germany

(3) Bundesamt für Kartographie und Geodäsie (BKG), Frankfurt / Main, Germany

Overview

1. Combination of GNSS and SLR: **General considerations**
2. **Expectation** from a combined analysis of GNSS and SLR@GNSS
3. **Results** from one year of combining GNSS and SLR@GNSS
4. Conclusions and outlook

Combination of GNSS and SLR

Co-location at stations:

- Application of known **local tie** values
- GNSS observations of ground network; SLR observations to Lageos

Problem:

- Phase center modelling of GNSS antenna
- Local ties

Co-location at satellites:

- 1.) **GNSS satellite:** Transmitting point for GNSS
Reflecting point for SLR (target)
 - 2.) **LEO satellite:** Receiving point for GNSS (“kinematic station”)
Reflecting point for SLR (target)
- **Vector** of GNSS and SLR reference points **w.r.t. satellite CoM** needed

Co-location at GNSS satellites

SLR to GNSS satellites:

1. **Validation** of microwave-only GNSS orbits by SLR range residuals
⇒ control of a priori models (e.g., radiation pressure)
2. **Combined orbit determination**
⇒ only few SLR normal points per day (~ 10-20 per satellite)
⇒ problematic on daily basis

Strength of *SLR to geodetic satellites* (Lageos,...):

Reference frame: mainly **scale** and **geocenter**

⇒ **Applicable as well for SLR @ GNSS?**

Expectation from combined analysis

	GNSS @GNSS	SLR @GNSS	SLR @Lageos
Radiation pressure ↔ Geocenter	Problems in RPR modelling	Problems in RPR modelling	RPR well modelled
GNSS satellite antenna phase center ↔ Scale	Problems in phase center modelling	independent	-
Range biases ↔ Scale	-	Decorrelated if different elevation angles	For a few sites only

SLR @ GNSS: ⇒ Geocenter is affected as well
 ⇒ **Scale** is transferred directly to GNSS

 ⇒ **Independent** control of **local ties**

Combined analysis of GNSS and SLR

- Studies using one year of data: 2008
- Analysis and combination with the *Bernese GPS Software*

→ *GNSS-only NEQs (daily):*

- Combined GPS+Glonass analysis performed at CODE

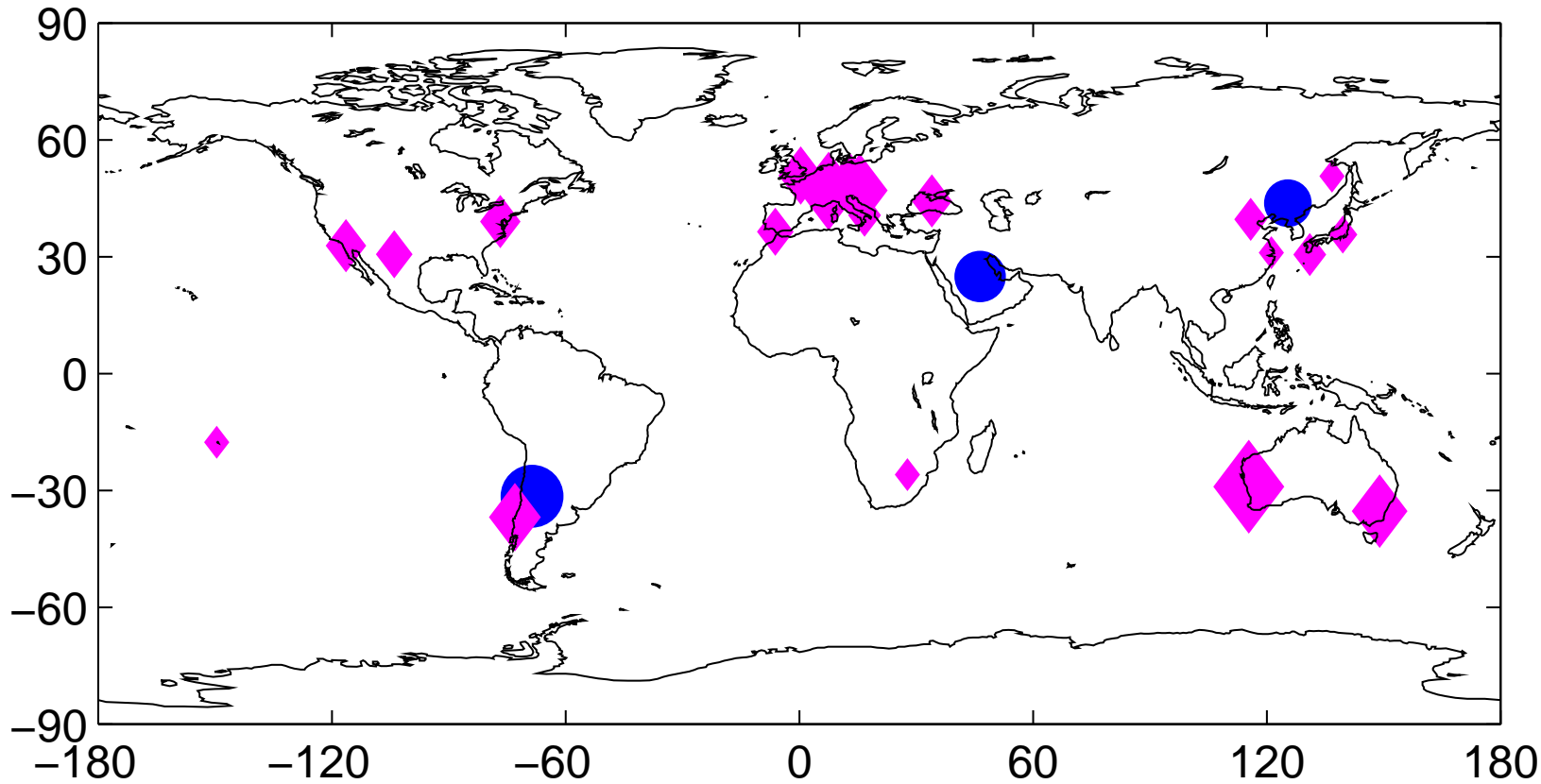
→ *SLR-only NEQs (daily):*

- SLR data to GPS and Glonass satellites
- Parameterization identical to GNSS analysis (orbits, ERP, geocenter)
- In addition: Range biases

→ *Combination:*

- Daily combination
- Accumulation to annual solution
- Use of “space ties” only, no “local ties”!

Network in 2008



Satellites tracked:

GPS: G05
G06

GLONASS: R15
R24
R07
R11

Altogether:

25 SLR sites

31855 normal points (NP)

8 sites with > 1000 NP

5 sites with > 500 NP

6 sites with > 100 NP

6 sites with < 100 NP

Northern hemisphere:

16804 NP

Southern hemisphere:

15051 NP

Combined analysis of GNSS and SLR

Questions to be answered:

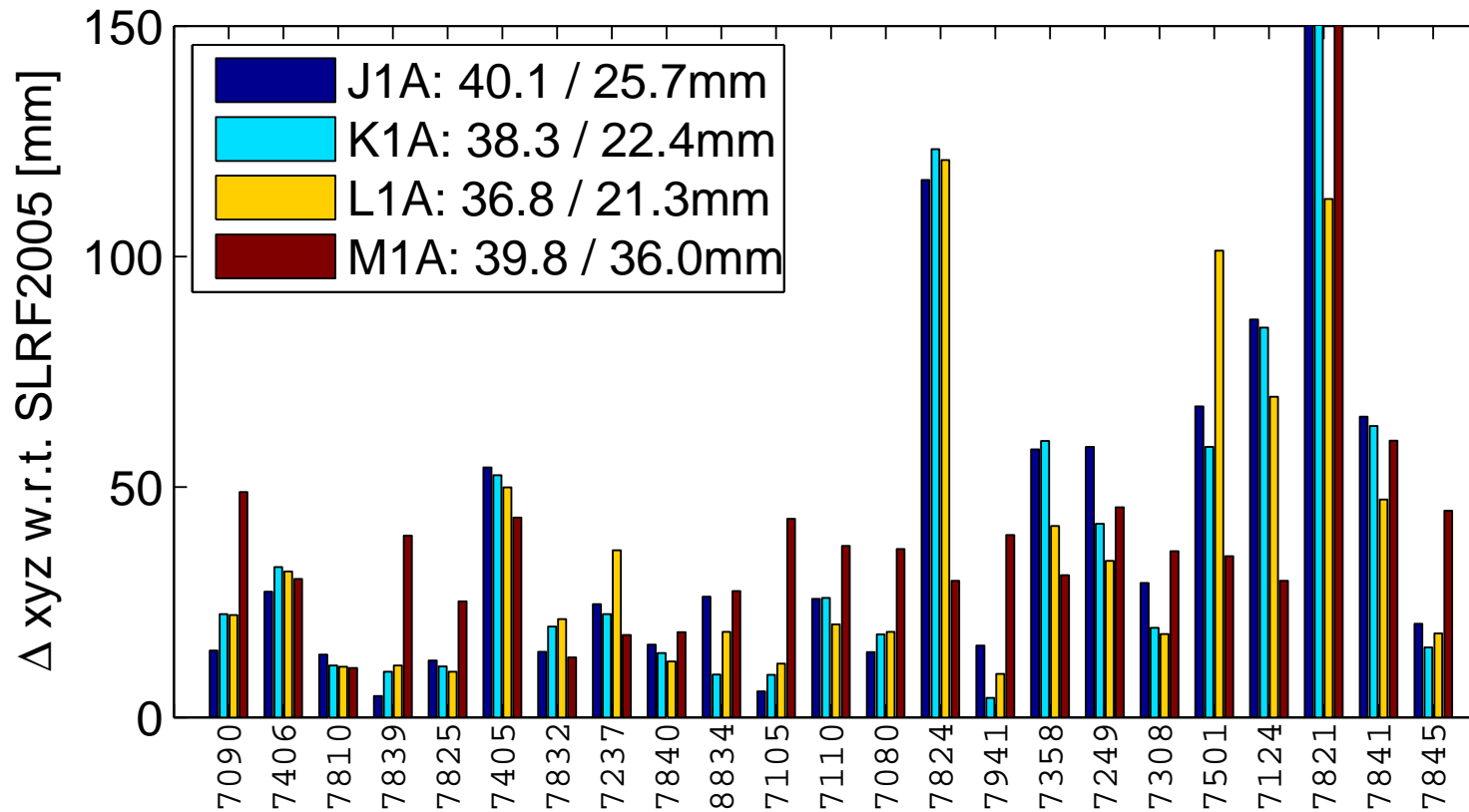
Are satellite co-locations strong enough to fully replace co-locations at ground?
(**space ties** instead of **local ties**)

Is an estimation of **GNSS SAO** together with **SLR range biases** possible or does this cause a rank deficiency for the **scale**?

Combined analysis of GNSS and SLR

		GNSS SAO fixed on igs05.atx	GNSS SAO corrections estimated
M	No SLR range bias	SLR and GNSS deliver information on the scale	SLR delivers information on the scale
L	SLR range bias <i>per satellite</i> (G05, G06, R15, R24, ...)	↓ Scale of combined solution is a weighted mean of the GNSS and SLR scale	GNSS has a rank deficiency w.r.t. the scale
K	SLR range bias <i>per system</i> (GPS, GLONASS)	(GNSS will dominate)	↓ Scale of combined solution comes only from SLR
J	SLR range bias <i>per station</i>		

Comparison with SLRF2005



Stations sorted according to number of SLR observations (descending order)

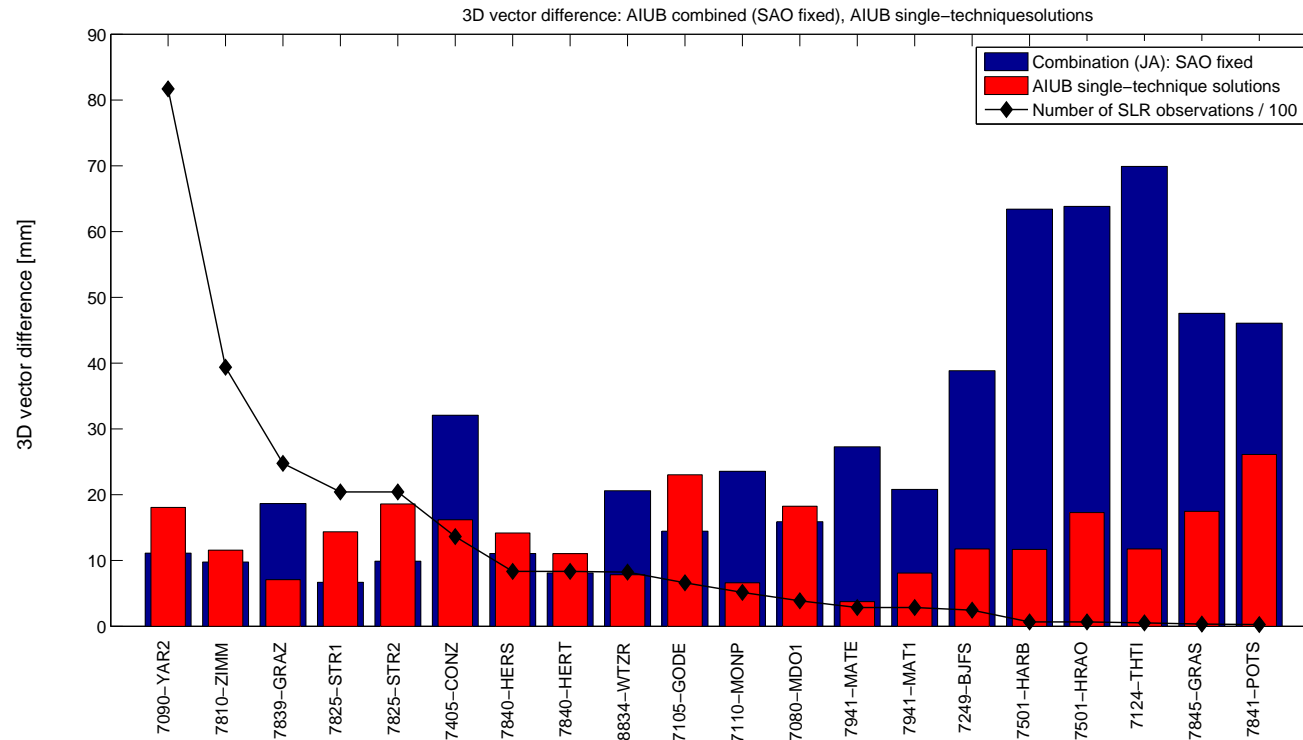
SLR station coordinates are well determined by using solely “space ties”
(no local ties to GNSS sites; not included in datum definition)

Prerequisite: sufficient number of SLR observations (~ 200-300 NP)

Comparison with local ties

Combining GNSS and SLR@GNSS using „space ties“ only

- Combined yearly GNSS+SLR solution
- Datum definition: NNR+NNT (GNSS core sites), **no Local ties**
- **GNSS antenna phase center (SAO) fixed** = Scale defined by GNSS and SLR



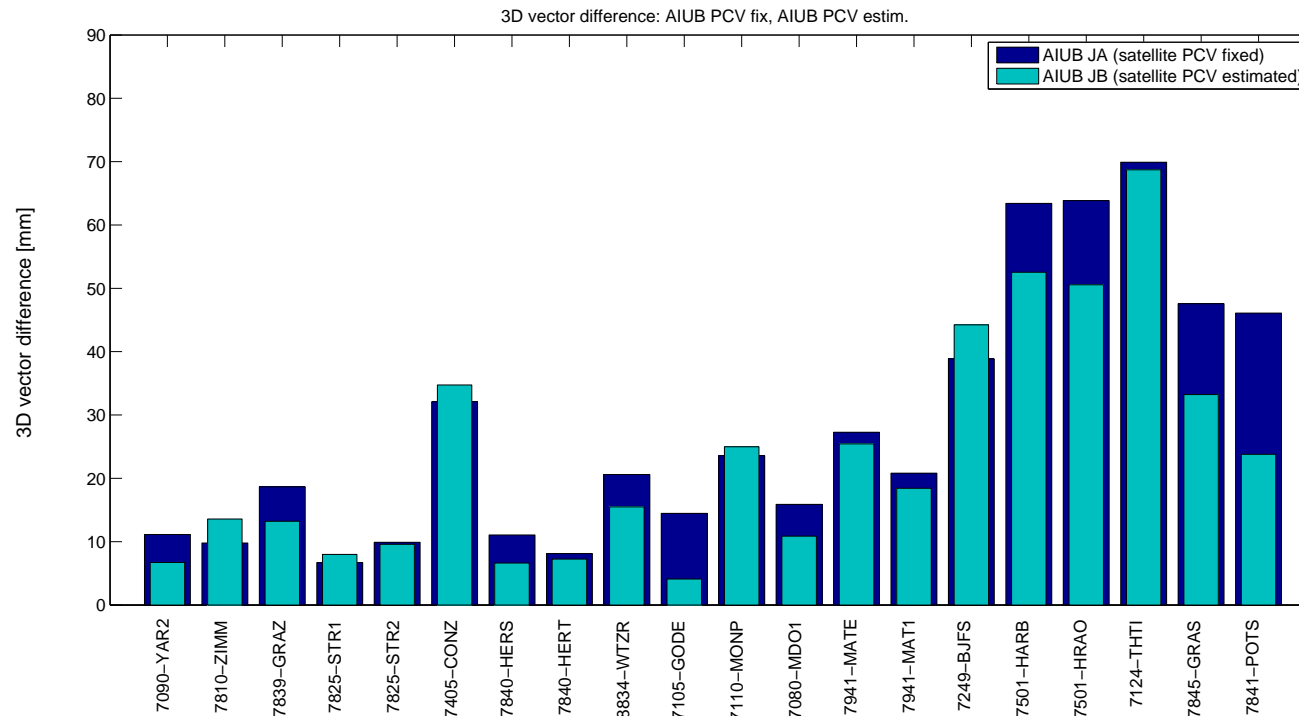
Red:
From annual
single-technique
solutions

Blue:
Combined solution,
GNSS SAO fixed

Comparison with local ties

Impact of GNSS antenna phase center (SAO) estimation:

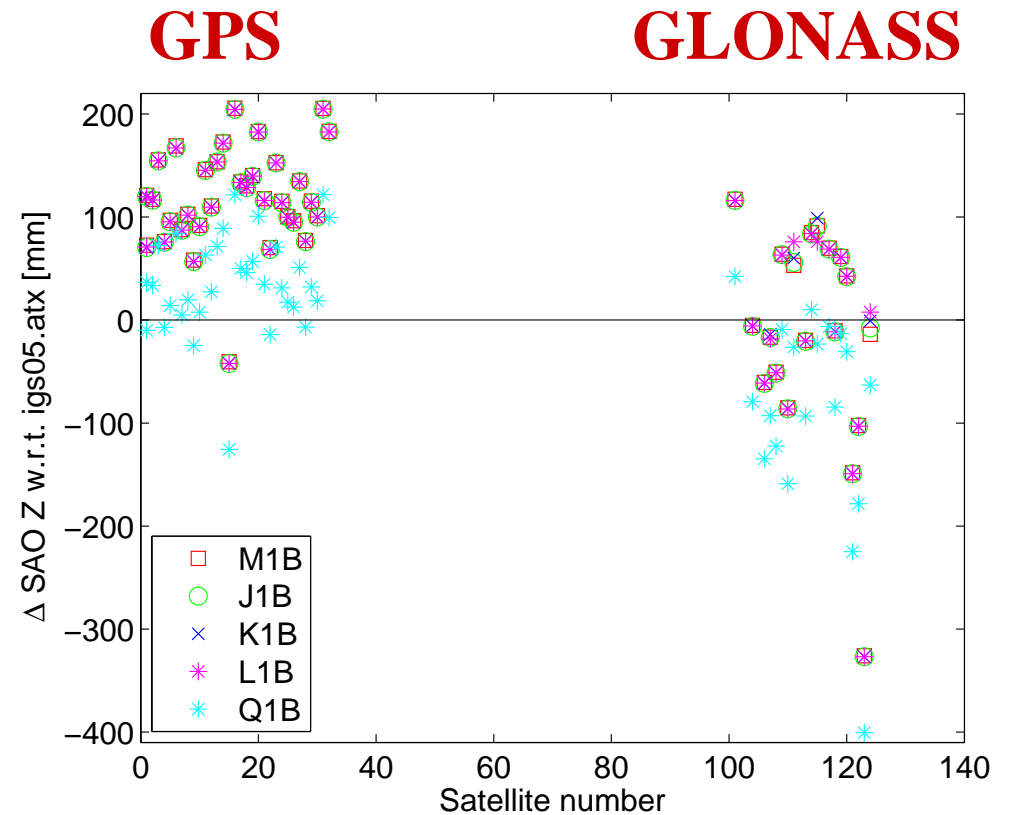
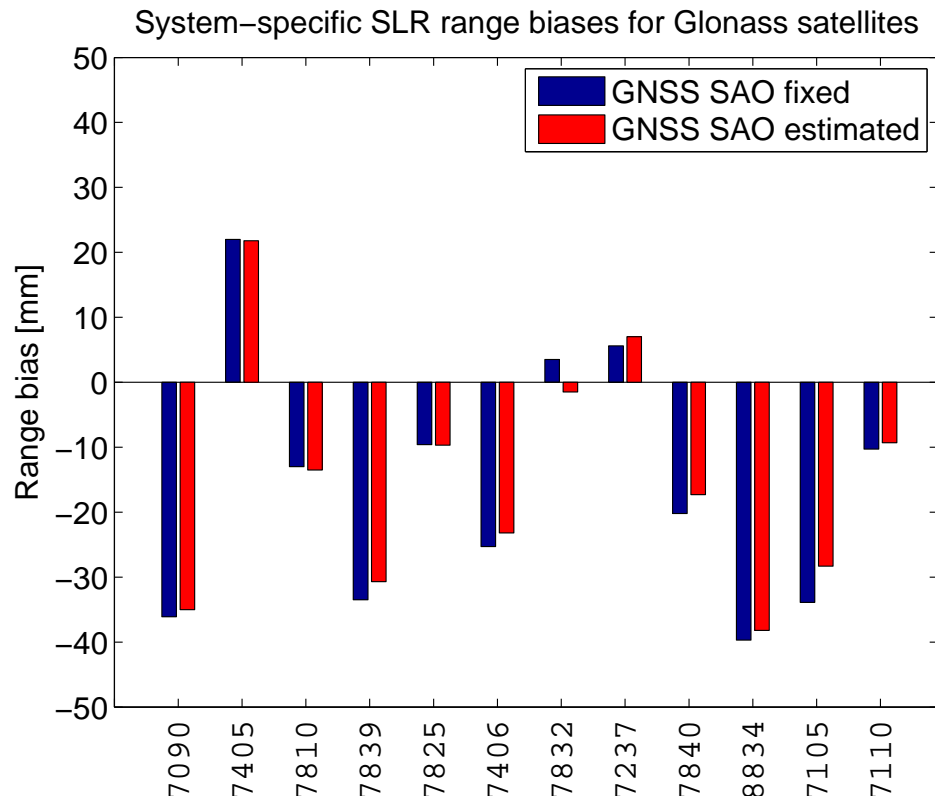
- No big differences \Rightarrow Estimation of SAO is possible
- Slightly better agreement with local ties if scale is NOT defined by GNSS (has to be verified using longer time span of data!)



Blue:
Combined solution,
GNSS SAO fixed

Green:
Combined solution,
GNSS SAO estimated

SLR range biases and GNSS SAO



Simultaneous estimation of GNSS antenna phase center offsets and SLR range biases is possible

⇒ Scale of SLR can be transferred into GNSS network

Conclusions and outlook

- Combination using *SLR@GNSS* works fine
 - ⇒ most direct way to combine GNSS and SLR
- Connection via „*space ties*“ only is possible (without local ties)
 - ⇒ Independent control of local ties
- BUT:***
 - Accurate ties*** (in space and on sites) required for combination
 - Number of SLR observations*** critical (not possible on a daily basis)
- ***Scale from SLR*** is transferred to GNSS ***directly*** (not via local ties)
 - ⇒ Estimation of GNSS SAO consistent to SLR scale
- Orbit overlap error is slightly improved (mainly GLONASS)
- Studies have to be extended to ***longer time span***
- ***Inclusion of Lageos***: Geocenter; more stable SLR station coordinates