Spotlight on Bernese GNSS Software

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Building the Lötschberg tunnel in Switzerland

Before the construction of the tunnel starts a geodetic connection of the portals is needed.



at that time: triangulations over several months have been necessary



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today: few hours of GNSS-measurements are sufficient

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IGS Satellite Orbits



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- CODE, Center for Orbit Determination in Europe, is one of at present ten Analysis Centers of the IGS. CODE is formed as a joint venture of
 - the Astronomisches Institut, Universität Bern (AIUB),
 - the Bundesamt für Landestopografie (swisstopo),
 - the Bundesamt für Kartographie und Geodäsie (BKG), and
 - the Institut für Astronomische und Physikalische Geodäsie of TU München (IAPG, TUM).







Technische Universität München





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- CODE provides products for the repro, final, rapid, and ultra-rapid IGS products.
- CODE started with a rigorously combined GPS/GLONASS analysis in May 2003. Meanwhile also other IGS analysis centers join this a strategy for their final products: ESOC, GFZ, GRGS, NRCan, Wuhan.



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- CODE started with a rigorously combined GPS/GLONASS analysis in May 2003.
- Since 2012 CODE also contributes to the IGS MGEX project with a fully combined five-system solution: GPS+GLONASS+ Galileo+BeiDou+QZSS (currently 91 satellites).



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- CODE provides products for the repro, final, rapid, and ultra-rapid IGS products.
- CODE started with a rigorously combined GPS/GLONASS analysis in May 2003.
- Since September 2019, CODE as the first AC includes Galileo in the operational rapid and ultra-rapid solutions for the IGS, resulting in a GPS+GLONASS+Galileo solution.

Outline

Bernese GNSS Software: General overview

Bernese GNSS Software: Directory structure

Bernese GNSS Software: Technical aspects

Bernese GNSS Software: Processing examples Processing examples: coordinate computation Datum Definition in a Network Solution PPP – Precise Point Positioning

Bernese GNSS Software: Selected parameters

Summary

The Bernese GNSS Software

The Bernese GNSS Software is

- a scientific software package
- for multi-GNSS data analysis
- with highest accuracy requirements
- in regional to global scale networks.

It is developed, maintained and used at the Astronomical Institute of the University of Bern since many years.

The Bernese GNSS Software is online at http://www.bernese.unibe.ch.





The Bernese GNSS Software is particularly well suited for:

- rapid processing of small-size surveys (static as well as kinematic stations even LEOs)
- automatic processing of permanent networks (BPE: Bernese Processing Engine),
- combination of different receiver and antenna types, taking receiver biases and satellite antenna phase center variations into account,
- rigorosly combined processing of GPS, GLONASS, Galileo, BDS, and QZSS observations,
- ambiguity resolution on long baselines (2000 km and longer),
- precise point positioning (including ambigity resolution),
- generation of minimum constraint network solutions,
- ionosphere and troposphere monitoring,
- clock offset estimation and time transfer,
- orbit determination and estimation of Earth orientation parameters.

• . . .

Bernese GNSS Software: users



Bernese GNSS Software: users



Bernese GNSS Software: Program Overview



• Transfer Part:

Programs for generating files in the Bernese format from RINEX. Furthermore, this part also contains a set of tools to cut/concatenate and to manipulate RINEX files.

• Conversion Part:

Programs to extract external information necessary for the processing from international to Bernese specific formats (e.g., coordinates and velocities from ITRF in SINEX format, ANTEX, Bias SINEX).

• Orbit Part:

Programs for generation of a source-independent orbit representation (standard orbits), to update orbits, generate orbits in precise orbit format, compare orbits, etc. The Earth orientation related tools are included in this part too.

• Processing Part:

Programs for receiver clock synchronization, code and phase pre-processing, ambiguity resolution, parameter estimation based on GNSS observations (pgm. GPSEST) and on the superposition of normal equations (pgm. ADDNEQ2).

• Simulation Part:

Program to generate simulated GNSS observations (code and/or phase, one or two frequencies) based on statistical information (RMS for observations, biases, cycle slips).

• Service Part:

A collection of useful tools to edit/browse/manipulate binary data files, compare coordinate sets, display residuals, etc. A set of programs to convert binary files to ASCII and vice versa belong to the service part, too.

Main Directories:

• \$C=BERN54

Program area with source code, executables, and supporting files

• \$U=GPSUSER54

User area with user-specific settings for interactive processing and the BPE configurations running for this user

• \$T=GPSTEMP54

Temporary file area for the users BPE processing

Main Directories:

• \$D=GPSDATA/DATAPOOL

Local database with all external files needed for GNSS data processing

• \$P=GPSDATA/CAMPAIGN54

Campaign area where the processing with the Bernese GNSS Software takes place

• \$S=GPSDATA/SAVEDISK

Product archive containing all GNSS derived products for further analysis



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Dataflow realized in the processing examples of Version 5.4:

 $\textbf{DATAPOOL} \rightarrow \textbf{CAMPAIGN} \rightarrow \textbf{SAVEDISK}$

Defining what to do::



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- 4. Decide on consistent IERS modelling, antenna model, and reference frame.

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• Populate the DATAPOOL with the necessary files.

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- 5. Make a first network solution (real-valued ambiguities)

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- 6. Resolve ambiguities



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- 4. Data preprocessing: cycle slip detection and correction; outlier rejection
- 5. Make a first network solution (real-valued ambiguities)
- 6. Resolve ambiguities
- 7. Create a normal equation containing all relevant parameters
- 8. NEQ-based single- or multi-session solution
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 - what is to do: user scripts
 - the order of running the scripts (dependencies)
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 - the order of running the scripts (dependencies)
 - where a script can be started (CPU)
- Process Control File (PCF) is the way how this information is implemented.
- An example of such a PCF looks like:



PID	SCRIPT	OPT_DIR	PARAMETER	lS			
#							
# Co #	py requir	ed files					
001	R2S_COP	R2S_GEN	CPU = ANY				
011	RNX_COP	R2S_GEN	CPU = ANY;	WAIT = 001;	NEXTJOB=	101 99	99
#							
# Pr	epare the	pole and	orbit infor	mation			
#							
101	POLUPD	R2S_GEN	CPU = ANY;	WAIT = 001			
112	ORBGEN	R2S_GEN	CPU = ANY;	WAIT = 101	111		
#							
# Pr	eprocess,	convert,	and synchro	onize obse	rvation da	ta	
#							
221	RXOBV3	R2S_GEN	CPU = ANY;	WAIT = 011			
231	CODSPP	R2S_GEN	CPU = ANY;	WAIT = 112	221		
#							
# Fo	rm baseli	nes and pro	e-process p	ohase data	(incl. re	sidual	screening
#							
302	SNGDIF	R2S_GEN	CPU = ANY;	WAIT = 231			
311	MAUPRP	R2S_GEN	CPU = ANY;	WAIT = 302			
321	GPSEDT	R2S_EDT	CPU = ANY;	WAIT = 311			
341	ADDNEQ2	R2S_GEN	CPU = ANY;	WAIT = 331			

PID	SCRIPT	OPT_DIR	PARAMETERS
#			
# Co	py requir	ed files	
#			
001	R2S_COP	R2S_GEN	CPU=ANY T
011	RNX_COP	R2S_GEN	CPU=ANY; WAIT=001; NEXTJOB= 101 999
#			
# Pr	epare the	pole and	orbit information
#			
101	POLUPD	R2S_GEN	CPU=ANY; WAIT=001
112	ORBGEN	R2S_GEN	CPU=ANY; WAIT=101 111
#			
# Pr	eprocess,	convert, a	and synchronize observation data
#			
221	RXOBV3	R2S_GEN	CPU=ANY; WAIT=011
231	CODSPP	R2S_GEN	CPU=ANY; WAIT=112 221
#			
# Fo	rm baseli	nes and pre	-process phase data (incl. residual screening)
#			
302	SNGDIF	R2S_GEN	CPU=ANY; WAIT=231
311	MAUPRP	R2S_GEN	CPU=ANY; WAIT=302
321	GPSEDT	R2S_EDT	CPU=ANY; WAIT=311
341	ADDNEQ2	R2S_GEN	CPU=ANY; WAIT=331

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<pre># # Copy required files #</pre>
<pre># Copy required files #</pre>
OO1 R2S_CUP R2S_GEN CPU=ANY
011 RNX_COP R2S_GEN CPU=ANY; WAIT=001; NEXTJOB= 101 999
#
Prepare the pole and orbit information
#
101 POLUPD R2S_GEN CPU=ANY; WAIT=001
112 ORBGEN R2S_GEN CPU=ANY; WAIT=101 111
#
Preprocess, convert, and synchronize observation data
A
221 RXOBV3 R2S_GEN CPU=ANY; WAIT=011
231 CODSPP R2S_GEN CPU=ANY; WAIT=112 221
#
Form baselines and pre-process phase data (incl. residual screening)
302 SNGDIF R2S GEN CPU=ANY: WAIT=231
311 MAUPRP B2S GEN CPU=ANY: WAIT=302
321 COSEDT BOS EDT CDUEANY, WAIT=311
241 ADDRED DOG CEN COLLANY, WAIT-331
STI ADDREQZ RZS_GEN GFO-ANI, WAII-SSI

PID	SCRIPT	OPT_DIR	PARAMETERS	
#				
# Co	py requir	ed files		
#				
001	R2S_COP	R2S_GEN	CPU=ANY (1)	
011	RNX_COP	R2S_GEN	CPU=ANY; WAIT=001; NEXTJOB= 101 999	
#				
# Pr	epare the	pole and o	orbit information	
#				
101	POLUPD	R2S_GEN	CPU=ANY; WAIT=001	
112	ORBGEN	R2S_GEN	CPU=ANY; WAIT=101 111	
#				
# Pr	eprocess,	convert, a	and synchronize observation data	
#			<u>0</u>	
221	RXOBV3	R2S_GEN	CPU=ANY; WAIT=011	
231	CODSPP	R2S_GEN	CPU=ANY; WAIT=112 221	
#				
# Fo	rm baseli	nes and pre	e-process phase data (incl. residual screening)	
#				
302	SNGDIF	R2S_GEN	CPU=ANY; WAIT=231	
311	MAUPRP	R2S_GEN	CPU=ANY; WAIT=302	
321	GPSEDT	R2S_EDT	CPU=ANY; WAIT=311	
341	ADDNEQ2	R2S_GEN	CPU=ANY; WAIT=331	
			A # # /	

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PID	SCRIPT	OPT_DIR	PARAMETERS			
#						
# Cc	# Copy required files					
#						
001	R2S_COP	R2S_GEN	CPU=ANY (1)			
011	RNX_COP	R2S_GEN	CPU=ANY; WAIT=001; NEXTJOB= 101 999			
#						
# Pr	epare the	pole and	orbit information			
#						
101	POLUPD	R2S_GEN	CPU=ANY; WAIT=001			
112	ORBGEN	R2S_GEN	CPU=ANY; WAIT=101 111			
#						
# Pr	eprocess,	convert,	and synchronize observation data			
#						
221	RXOBV3	R2S_GEN	CPU=ANY; WAIT=011			
231	CODSPP	R2S_GEN	CPU=ANY; WAIT=112 221			
#						
# Fc	orm baseli	nes and pr	e-process phase data (incl. residual screening)			
#						
302	SNGDIF	R2S_GEN	CPU=ANY; WAIT=231			
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Slide	16 of 42		Astronomical Institute, University of Bern AIUb			

PID	SCRIPT	OPT_DIR	PARAMETERS	
#				
# <mark>C</mark> o	py requir	ed files		
#				
001	R2S_COP	R2S_GEN	CPU=ANY (1)	
011	RNX_COP	R2S_GEN	CPU=ANY; WAIT=001; NEXTJOB= 101 999	
#				
# Pr	epare the	pole and	orbit information	
#				
101	POLUPD	R2S_GEN	CPU=ANY; WAIT=001	
112	ORBGEN	R2S_GEN	CPU=ANY; WAIT=101 111	
#				
# Pr	eprocess,	convert, a	and synchronize observation data	
#			6	
221	RXOBV3	R2S_GEN	CPU=ANY; WAIT=011	
231	CODSPP	R2S_GEN	CPU=ANY; WAIT=112 221	
#				
# Fo	rm baseli	nes and pre	e-process phase data (incl. residual screening)	
#	SNCDIE	DOG CEN		
311	MAIIDED	R25_GEN	$CDII - ANY \cdot WATT - 302$	
321	CRSEDT	ROS EDT	CDII-ANV. WATT-311	
3/1	ADDNEO2	R25_EDI	CDIL-ANV. WATT-331	
541	RDDNEQZ	NZD_GEN	0r0-ANI, WALL-331	

```
PID
     SCRIPT
               OPT_DIR
                          PARAMETERS
#
 Resolve phase ambiguities
#
411
     GNSAMBAP
               R2S AMB
                          CPU = ANY: WAIT = 401
412
     GNSAMB_P
               R2S_AMB
                          CPU = ANY; WAIT = 411;
                                              PARALLEL = 411
#
# Compute ambiguity-fixed network solution, create final NEQ/SNX/TRO files
     GPSEST
               R2S_FIN
                          CPU=ANY; WAIT=412;
                                               PARAM2 = V_FIN
501
511
     ADDNEQ2
               R2S FIN
                          CPU=ANY: WAIT=501
513
    HELMCHK
               R2S_FIN
                         CPU=ANY; WAIT=511;
                                              NEXTJOB = 511
               R2S FIN
                          CPU = ANY: WAIT=513
514
    COMPAR
#
# Create summary file and delete files
901
    R2S SUM
               R2S GEN
                          CPU=ANY: WAIT=513
    R2S_SAV
               R2S_GEN
                          CPU=ANY: WAIT=901
902
904
     R2S_DEL
               R2S_GEN
                          CPU=ANY: WAIT=902 903:
                                                   PARAM1 = (10)
#
# End of BPE
999 DUMMY
               NO_OPT
                          CPU=ANY; WAIT=904
```

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Example Data for Demonstration

Seventee	en Eur	opean stations of the IGS
network	and fr	rom the EPN:
BRST		Brest, FRA
GANP		Ganovce, SVK
HERT		Hailsham, GBR
JOZ2		Jozefoslaw, POL
LAMA		Olsztyn, POL
MATE		Matera, ITA
MIKL		Mykolaiv, UKR
ONSA		Onsala, SWE
ORID		Ohrid, MKD
PTBB		Braunschweig, DEU
TLSE		Toulouse, FRA
VILL		Villafranca, ESP
WSRT		Westerbork, NLD
WTZR,	WTZZ	Kötzting, DEU
ZIM2,	ZIMM	Zimmerwald, CHE



Stations used in example campaign (green stations with coordinates given in the IGS 20 reference frame)

Demonstration



Bernese GNSS Software: some facts

The software package consists of:

- a QT-based graphical user interface
- a set of processing programs (Fortran 2003)
- distribution contains the full source code
- it runs on PC/Windows, UNIX/LINUX, MAC

```
! Update the statistics over all files per system
D0 iSys = 1,maxSys
CALL statisSysAll%stat(iSys)%stack(statisSys%stat(iSys))
ENDD0
```

```
! Update the statistics over all files and satellites
CALL statisTotAll%stat(1)%stack(statisTot%stat(1))
```

```
! Print the statistics for this observation file
CALL obxprt(opt, iFil, obsHeadObx, statisSat, statisSys, stat
```

```
/ Consider the condition regarding file selection
IF ( opt%what%isOptionWhatObservation() ) THEN
IF ( opt%checkObs(statisTot%stat(1)) ) THEN
CALL opt%lstFile%append(opt%fillst(1,iFil))
ELSE
CALL opt%delFile%append(opt%fillst(1,iFil))
CALL opt%delFile%append(opt%fillst(2,iFil))
ENDIF
ENDIF
```

The software package counts today:

- nearly 90 processing programs and 1400 subroutines, functions, and modules about 600,000 lines of source code (including comment lines),
- the GUI/BPE-program with 18,000 lines of source code

Bernese GNSS Software: some facts

Intensive user support includes

- online-help system provides explanations on the options,
- a 850 pages user manual (downloadable as PDF for free),
- a series of README-files on various topics
- FAQ-section on the webpage,
- e-mail support to help with potential problems,
- regular updates for bugfixes and improvements,
- a one week introductory course in Bern.



The distribution of the software package contains ready-to-use examples:

• PPP – PRECISE POINT POSITIONING

- standard PPP for coordinate, troposphere, and receiver clock determination
- as single- or multi-GNSS solutions (GPS, GLONASS, Galileo, BeiDou, QZSS)
- ambiguity resolution, if the consistent bias products are available
- several extended processing examples can be enabled: geocenter estimation, pseudo-kinematic, high-rate troposphere



The distribution of the software package contains ready-to-use examples:

• RNX2SNX: RINEX-to-SINEX

- standard double difference network solution
- primary products are coordinates and troposphere corrections
- as single- or multi-GNSS solutions (GPS, GLONASS, Galileo, BeiDou, QZSS)
- extended ambiguity resolution scheme
- datum definition with verification based on minimum constraint solution

CLKDET: CLOCK DETERMINATION

- standard zero difference network solution
- primary products are receiver and satellite clock corrections (also, w.r.t. an existing coordinate and troposphere solution)
- as single- or multi-GNSS solutions (GPS, GLONASS, Galileo, BeiDou, QZSS)

The distribution of the software package contains ready-to-use examples:

- IONDET: IONOSPHERE MODEL DETERMINATION for LEOs
 - ionosphere model determination from regional or global networks for dual-frequency
- LEOPOD: PRECISE ORBIT DETERMINATION for LEOs
 - Precise Orbit Determination for a Low Earth Orbiting Satellites based on on-board GPS-measurements (e.g., for GRACE)
- SLRVAL: SLR ORBIT VALIDATION
 - Validation of an existing GNSS or LEO orbit using SLR measurements

Each example BPEs is accompanied by an extensive README file:

- explaining the main purpose,
- providing a detailed description on the realization of the purpose,
- showing where to find the key quality indicators for the results and giving some ideas about potential sources of problems,
- listing of the BPE example configuration,
- listing the necessary input and result files.

The processing examples distributed with the *Bernese GNSS Software* offer three ways to compute coordinates:

1. PPP: Precise Point Positioning

processing of single stations, very efficient in case of parallelization

2. RNX2SNX: double-difference network solution

efficient because clock parameters are not explicitly setup, but needs bookkeeping to consider correlations due to differencing

3. CLKDET: zero-difference network solution

network solution means, to solved for satellite and receiver clock corrections at least a normal equation with all satellite clock parameters need to be inverted.

Are there differences between the three strategies or are they equivalent?



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We have the GNSS observations of several stations to some satellites:

$$L_i^k = \left| \vec{x^k} - \vec{x_i} \right| + T_i^k + c\delta_i - c\delta^k + \lambda N_i^k \qquad L_i^l = \left| \vec{x^l} - \vec{x_i} \right| + T_i^l + c\delta_i - c\delta^l + \lambda N_i^l \qquad \dots$$

$$L_j^k = \left| \vec{x^k} - \vec{x_j} \right| + T_j^k + c\delta_j - c\delta^k + \lambda N_j^k \qquad L_j^l = \left| \vec{x^l} - \vec{x_j} \right| + T_j^l + c\delta_j - c\delta^l + \lambda N_j^l \qquad \dots$$



If you are not interested in the clock parameters

$$L_i^k = \left| \vec{x^k} - \vec{x_i} \right| + T_i^k + c\delta_i - c\delta^k + \lambda N_i^k \qquad L_i^l = \left| \vec{x^l} - \vec{x_i} \right| + T_i^l + c\delta_i - c\delta^l + \lambda N_i^l \qquad \dots$$

$$L_j^k = \left| \vec{x^k} - \vec{x_j} \right| + T_j^k + c\delta_j - c\delta^k + \lambda N_j^k \qquad L_j^l = \left| \vec{x^l} - \vec{x_j} \right| + T_j^l + c\delta_j - c\delta^l + \lambda N_j^l \qquad \dots$$

If you are not interested in the clock parameters

$$L_i^k = \left| \vec{x^k} - \vec{x_i} \right| + T_i^k + c\delta_i - c\delta^k + \lambda N_i^k \qquad L_i^l = \left| \vec{x^l} - \vec{x_i} \right| + T_i^l + c\delta_i - c\delta^l + \lambda N_i^l \qquad \dots$$

$$L_j^k = \left| \vec{x^k} - \vec{x_j} \right| + T_j^k + c\delta_j - c\delta^k + \lambda N_j^k \qquad L_j^l = \left| \vec{x^l} - \vec{x_j} \right| + T_j^l + c\delta_j - c\delta^l + \lambda N_j^l \qquad \dots$$

... we may form differences between observations to cancel out the clock parameters:

$$L_{i}^{k} - L_{j}^{k} = \left| \vec{x^{k}} - \vec{x_{i}} \right| - \left| \vec{x^{k}} - \vec{x_{j}} \right| + T_{i}^{k} - T_{j}^{k} + c \left(\delta_{i} - \delta^{k} - \delta_{j} + \delta^{k} \right) + \lambda \left(N_{i}^{k} - N_{j}^{k} \right)$$
$$L_{i}^{l} - L_{j}^{l} = \left| \vec{x^{l}} - \vec{x_{i}} \right| - \left| \vec{x^{l}} - \vec{x_{j}} \right| + T_{i}^{l} - T_{j}^{l} + c \left(\delta_{i} - \delta^{k} - \delta_{j} + \delta^{k} \right) + \lambda \left(N_{i}^{l} - N_{j}^{l} \right)$$

If you are not interested in the clock parameters

$$L_i^k = \left| \vec{x^k} - \vec{x_i} \right| + T_i^k + c\delta_i - c\delta^k + \lambda N_i^k \qquad L_i^l = \left| \vec{x^l} - \vec{x_i} \right| + T_i^l + c\delta_i - c\delta^l + \lambda N_i^l \qquad \dots$$

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• A consequent creation of (artificial) double-difference observations is equivalent to pre-eliminating the clock parameters on normal equation level.



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Conclusions:

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Conclusions:

- A consequent creation of (artificial) double-difference observations is equivalent to pre-eliminating the clock parameters on normal equation level.
- When using the same original observations, we obtain the same estimates for the geometry-related parameters on zero, single or double difference level (given that all existing correlations are considered).
- The ambiguity resolution is directly possible only on double-difference level (otherwise some bias parameters are needed).
- Effects that cancel out when differencing the observations are absorbed by the satellite clock parameters in the zero-difference approach.

1. PPP: Precise Point Positioning

processing of single stations, very efficient in case of parallelization

2. RNX2SNX: double-difference network solution

efficient because clock parameters are not explicitly setup, but needs bookkeeping to consider correlations due to differencing

3. CLKDET: zero-difference network solution

network solution means, to solved for satellite and receiver clock corrections at least a normal equation with all satellite clock parameters need to be inverted.

Are there differences between the three strategies or are they equivalent?

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Zero- and double-difference solutions are equivalent.

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What is the consequence of introducing the GNSS orbits?

Datum Definition in a Network Solution

The Bernese GNSS Software supports:

• Free network solution

no constraints on station coordinates

Datum information is only introduced by fixed satellite orbits.

• Minimum constraint solution

no-net translation, no-net rotation, no-net scale

w.r.t. reference network

• Coordinates constrained:

Constraining of station coordinate parameters

• Coordinates fixed:

Deleting coordinate parameters from the NEQ

Not recommended if NEQ-files are stored.

Demonstration



Principle of datum definition



Principle of datum definition



Principle of datum definition

Solution A Minimum constraint solution

Solution B

Fixed reference coordinates



Minimum constraint solution:

- Constraint on translation/rotation/scale of the network w.r.t. reference sites
- No distortion of the network geometry
- All coordinates are improved
- Well suited to identify problems with reference sites

List of reference sites may automatically be verified by HELMR1-program.

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Usually (regional solutions):

- Orientation of the network is given if the orbits were introduced as fixed \Rightarrow no-net-rotation conditions are not needed/reasonable
- Only "Center of network" condition (translations), i.e., the center of selected reference sites remains unchanged

Minimum constraint solution:

- Constraint on translation/rotation/scale of the network w.r.t. reference sites
- No distortion of the network geometry
- All coordinates are improved
- Well suited to identify problems with reference sites List of reference sites may automatically be verified by HELMR1-program.

Coordinates introduced:

- "Fixing" coordinates of reference stations is useful if they are expected to be more accurate than the current GNSS solution.
- In that scenario it is even more essential to check the consistency first!

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A consistent datum definition using verified sites only is indispersible.

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What about the datum definition in case of PPP?



















$$L_{1}^{k} = \left| \vec{x^{k}} - \vec{x_{1}} \right| + T_{1}^{k} + c\delta_{1} - c\delta^{k} + \lambda N_{1}^{k} \qquad L_{1}^{l} = \left| \vec{x^{l}} - \vec{x_{1}} \right| + T_{1}^{l} + c\delta_{1} - c\delta^{l} + \lambda N_{1}^{l} \qquad \dots$$



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GNSS observation equations for a large number of stations

$$\begin{split} L_{1}^{k} &= \left| \vec{x^{k}} - \vec{x_{1}} \right| + T_{1}^{k} + c\delta_{1} - c\delta^{k} + \lambda N_{1}^{k} \qquad L_{1}^{l} = \left| \vec{x^{l}} - \vec{x_{1}} \right| + T_{1}^{l} + c\delta_{1} - c\delta^{l} + \lambda N_{1}^{l} \qquad \dots \\ L_{2}^{k} &= \left| \vec{x^{k}} - \vec{x_{2}} \right| + T_{2}^{k} + c\delta_{2} - c\delta^{k} + \lambda N_{2}^{k} \qquad L_{2}^{l} = \left| \vec{x^{l}} - \vec{x_{2}} \right| + T_{2}^{l} + c\delta_{2} - c\delta^{l} + \lambda N_{2}^{l} \qquad \dots \\ L_{3}^{k} &= \left| \vec{x^{k}} - \vec{x_{3}} \right| + T_{3}^{k} + c\delta_{3} - c\delta^{k} + \lambda N_{3}^{k} \qquad L_{3}^{l} = \left| \vec{x^{l}} - \vec{x_{3}} \right| + T_{3}^{l} + c\delta_{3} - c\delta^{l} + \lambda N_{3}^{l} \qquad \dots \\ \vdots \\ L_{n}^{k} &= \left| \vec{x^{k}} - \vec{x_{n}} \right| + T_{n}^{k} + c\delta_{n} - c\delta^{k} + \lambda N_{n}^{k} \qquad L_{n}^{l} &= \left| \vec{x^{l}} - \vec{x_{n}} \right| + T_{n}^{l} + c\delta_{n} - c\delta^{l} + \lambda N_{n}^{l} \qquad \dots \end{split}$$

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GNSS observation equations for a large number of stations

$$\begin{split} L_{1}^{k} &= \left| \vec{x^{k}} - \vec{x_{1}} \right| + T_{1}^{k} + c\delta_{1} - c\delta^{k} + \lambda N_{1}^{k} \qquad L_{1}^{l} = \left| \vec{x^{l}} - \vec{x_{1}} \right| + T_{1}^{l} + c\delta_{1} - c\delta^{l} + \lambda N_{1}^{l} \qquad \dots \\ L_{2}^{k} &= \left| \vec{x^{k}} - \vec{x_{2}} \right| + T_{2}^{k} + c\delta_{2} - c\delta^{k} + \lambda N_{2}^{k} \qquad L_{2}^{l} = \left| \vec{x^{l}} - \vec{x_{2}} \right| + T_{2}^{l} + c\delta_{2} - c\delta^{l} + \lambda N_{2}^{l} \qquad \dots \\ L_{3}^{k} &= \left| \vec{x^{k}} - \vec{x_{3}} \right| + T_{3}^{k} + c\delta_{3} - c\delta^{k} + \lambda N_{3}^{k} \qquad L_{3}^{l} = \left| \vec{x^{l}} - \vec{x_{3}} \right| + T_{3}^{l} + c\delta_{3} - c\delta^{l} + \lambda N_{3}^{l} \qquad \dots \\ \vdots \\ L_{n}^{k} &= \left| \vec{x^{k}} - \vec{x_{n}} \right| + T_{n}^{k} + c\delta_{n} - c\delta^{k} + \lambda N_{n}^{k} \qquad L_{n}^{l} &= \left| \vec{x^{l}} - \vec{x_{n}} \right| + T_{n}^{l} + c\delta_{n} - c\delta^{l} + \lambda N_{n}^{l} \qquad \dots \end{split}$$

Conclusions:

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 Any inconsistency will degrade your PPP results.



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- That's why the observation equations for a PPP processing have to be fully consistent to the related network solution. Any inconsistency will degrade your PPP results.
- PPP-based station coordinates join the datum realization of the original network solution.

Demonstration



• Station Coordinates

Rectangular coordinates X, Y, Z in the ITRF (at present the ITRF 2014 is used). The results are also expressed in the (user defined) geodetic datum (λ, β, h)

• Station Velocities

In program ADDNEQ2 station velocities may be set up if a long time series of NEQ systems containing the same stations is available.

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• Epoch specific station coordinates

A set of station coordinates is assigned to each epoch (kinematic surveys).

List of Parameters (II)

• Scaling factors

Scaling factors for up to three crustal deformation models provided in global grid files can be estimated to validate the model and/or to investigate the impact of the model on GNSS-derived parameters.

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• HELMERT-parameters

Transformation parameters (translation, rotation, scale) between the coordinate parameters from different normal equations can be estimated.

Astronomical Institute, University of Bern AIUB

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- You have all aspects of the GNSS analysis under your control.
- Many other groups have discovered the software already for their tasks.

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THANK YOU for your attention

Publications of the satellite geodesy research group:

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