

# Precise orbit determination for low Earth orbit satellite during maneuver periods

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# Outline

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- Motivation
- Bernese POD strategy
- Internal consistency check
- External orbit validations
- Conclusions

# Motivation

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- Low Earth Orbit (LEO) satellite perform maneuvers to,
  - overcome highly-perturbed in-flight conditions
  - maintain pre-defined trajectory
  - keep formation/constellation flying
  - avoid threatening collisions...
- However the challenges are,
  - maneuvers can be significantly different for various satellite missions
  - (reduced-) dynamic Precise Orbit Determination (POD) gets worse
  - follow-on scientific research might be influenced by imperfect orbit...



# Motivation

- Research case 1 : Sentinel-3 (A/B)
  - Part of the fleet of European Space Agency's Copernicus Earth observation satellites
  - High-precision GPS receiver and Satellite Laser Ranging (SLR) for POD and validation
  - Data sets: all maneuver days in 2020, a reference day (w/o maneuvers) is selected

Sentinel-3A maneuver information\*

| DOY   | Duration [s] | Acceleration [mm/s <sup>2</sup> ] |
|-------|--------------|-----------------------------------|
| 20071 | 889.7        | 2.487                             |
| 20169 | 3.4          | 1.885                             |
| 20245 | N/A          | NA                                |
| 20246 | 774.8        | 2.429                             |
| 20337 | 13.9         | 0.615                             |
| 20351 | 997.6        | 2.403                             |

Sentinel-3B maneuver information\*

| DOY   | Duration [s] | Acceleration [mm/s <sup>2</sup> ] |
|-------|--------------|-----------------------------------|
| 20036 | 718.6        | 2.658                             |
| 20099 | 673.8        | 2.632                             |
| 20148 | 2.9          | 1.913                             |
| 20211 | 1.9          | 1.901                             |
| 20281 | 885.6        | 2.587                             |
| 20351 | 13.8         | 0.609                             |

\* In telemetry data, the start and end accelerations are different, the average of them is shown.



# Motivation

- Research case 2 : GRACE-FO (C/D)
  - A NASA/DLR Earth gravitational science satellite formation
  - High-precision GPS receiver, SLR and K-Band Radar (KBR) for POD and validation
  - Data sets: all orbit maneuver days since launch

GRACE-FO-C maneuver information\*

| DOY   | Duration [s] | Acceleration [mm/s <sup>2</sup> ] |
|-------|--------------|-----------------------------------|
| 18144 | 127          | 0.157                             |
| 18145 | 416          | 0.144                             |
| 18146 | 423          | 0.144                             |
| 18173 | 49           | 0.143                             |
| 18295 | 735          | 0.144                             |
| 21307 | 1790 and 31  | 0.145                             |

GRACE-FO-D maneuver information\*

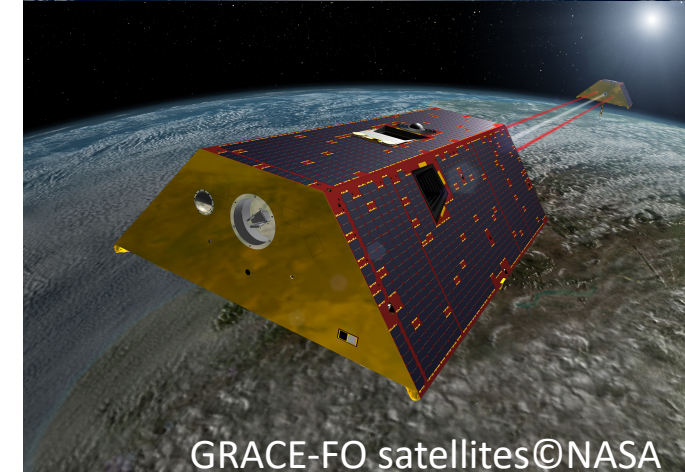
| DOY   | Duration [s] | Acceleration [mm/s <sup>2</sup> ] |
|-------|--------------|-----------------------------------|
| 18144 | 126          | 0.159                             |
| 18146 | 406 and 413  | 0.148                             |
| 18173 | 84           | 0.148                             |
| 19078 | 17           | 0.149                             |
| 20253 | 5            | 0.130                             |
| 21307 | 1790         | 0.149                             |

\* Durations and accelerations are from the spacecraft-event (TN-01a\_SCE.txt) file.

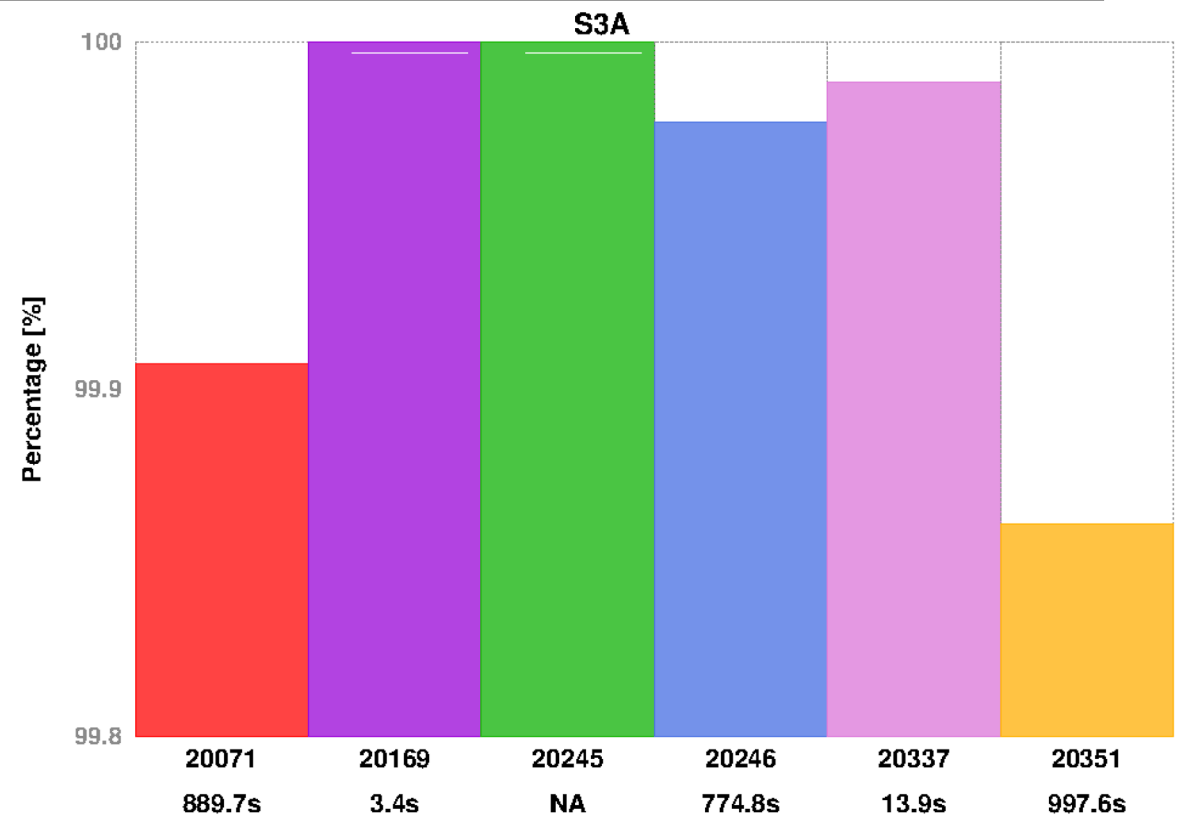
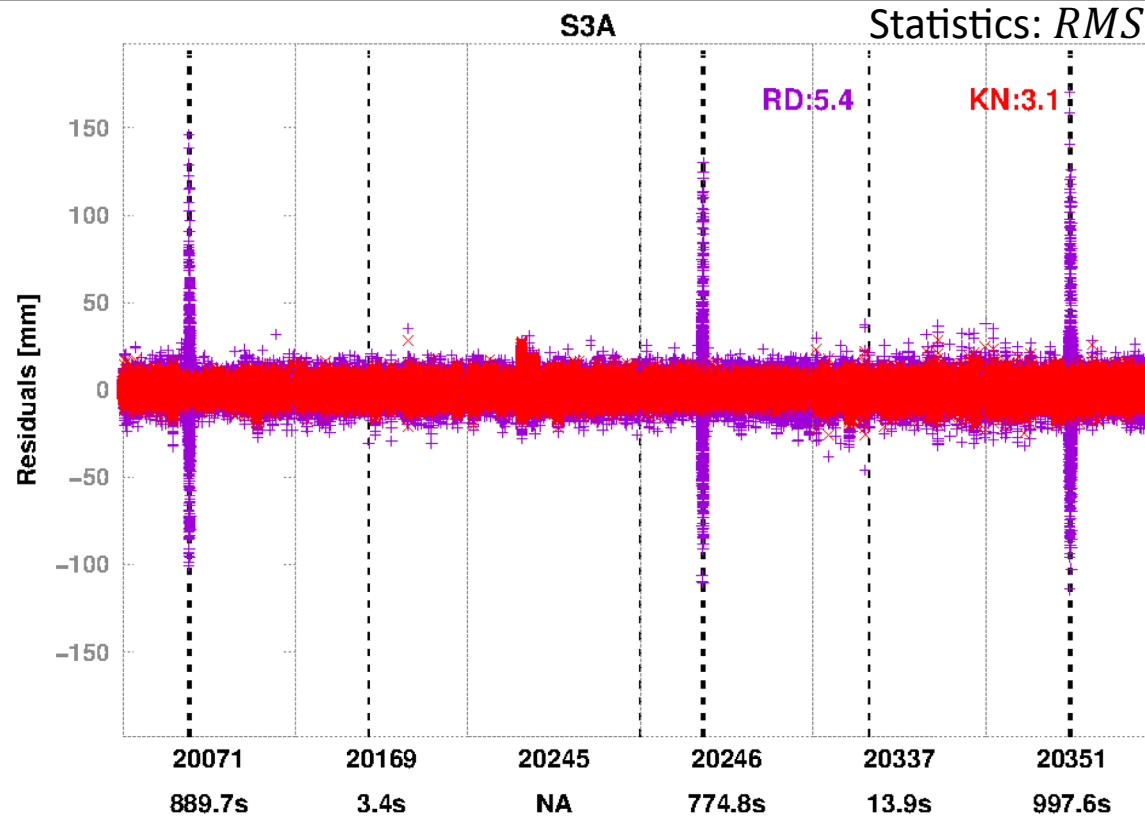
# Bernese POD strategy

- Software: Bernese GNSS Software v5.5
- POD solutions: reduced-dynamic and kinematic
- Satellite geometry: macro-model
- Gravitational and non-gravitational forces
- Dynamic parameters:
  - orbit elements
  - constant empirical acc.
  - **constant maneuver acc. in satellite body-fixed frame**
- Pseudo-stochastic parameters:
  - piece-wise constant acc.
  - **velocity pulses depending on maneuver time span**
- **Single receiver integer ambiguity resolution (IAR)**
  - No IAR during maneuver periods!

**No a-priori maneuver accelerations,  
only durations are used!**



# Internal orbit consistency: residuals



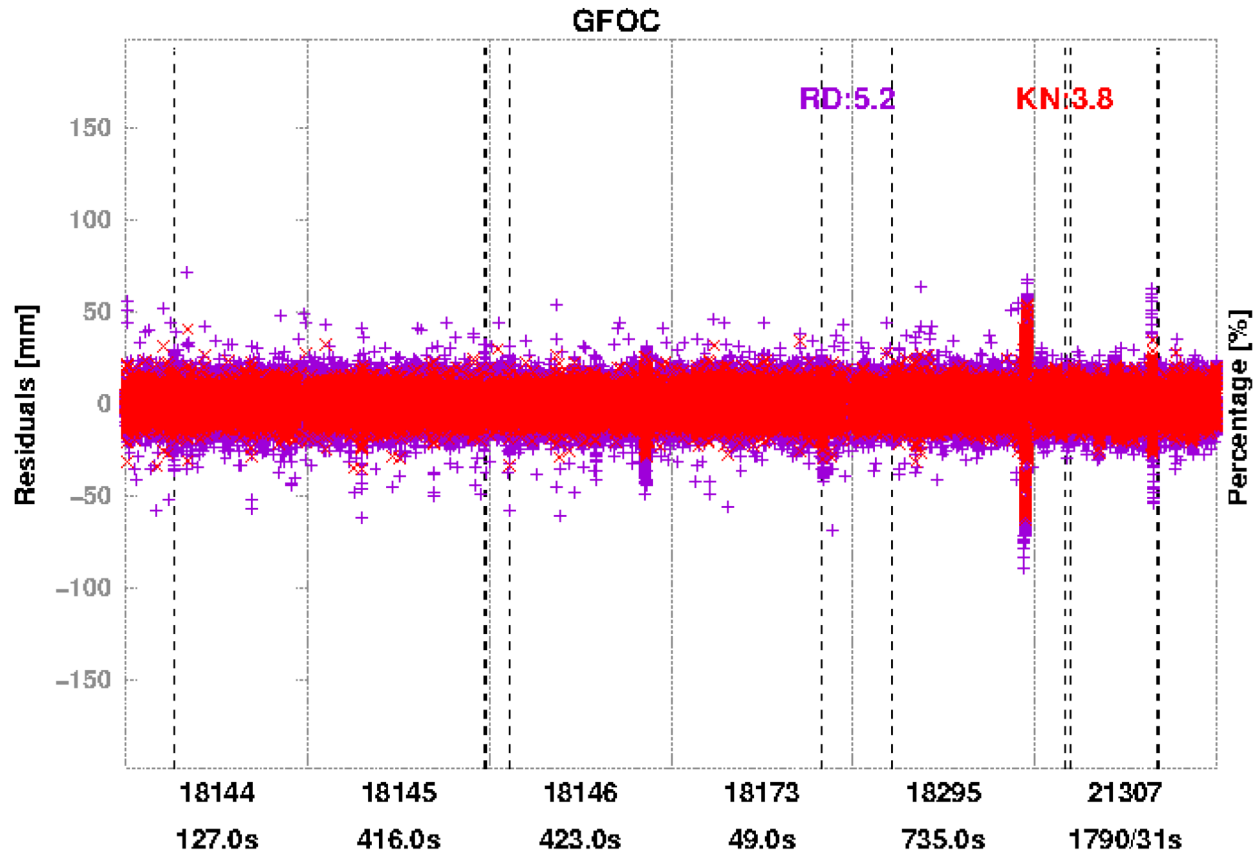
Ionosphere-free carrier-phase residuals and RMS statistics for the POD solution of Sentinel-3A maneuver and reference days.

RD: Reduced-dynamic; KN: Kinematic

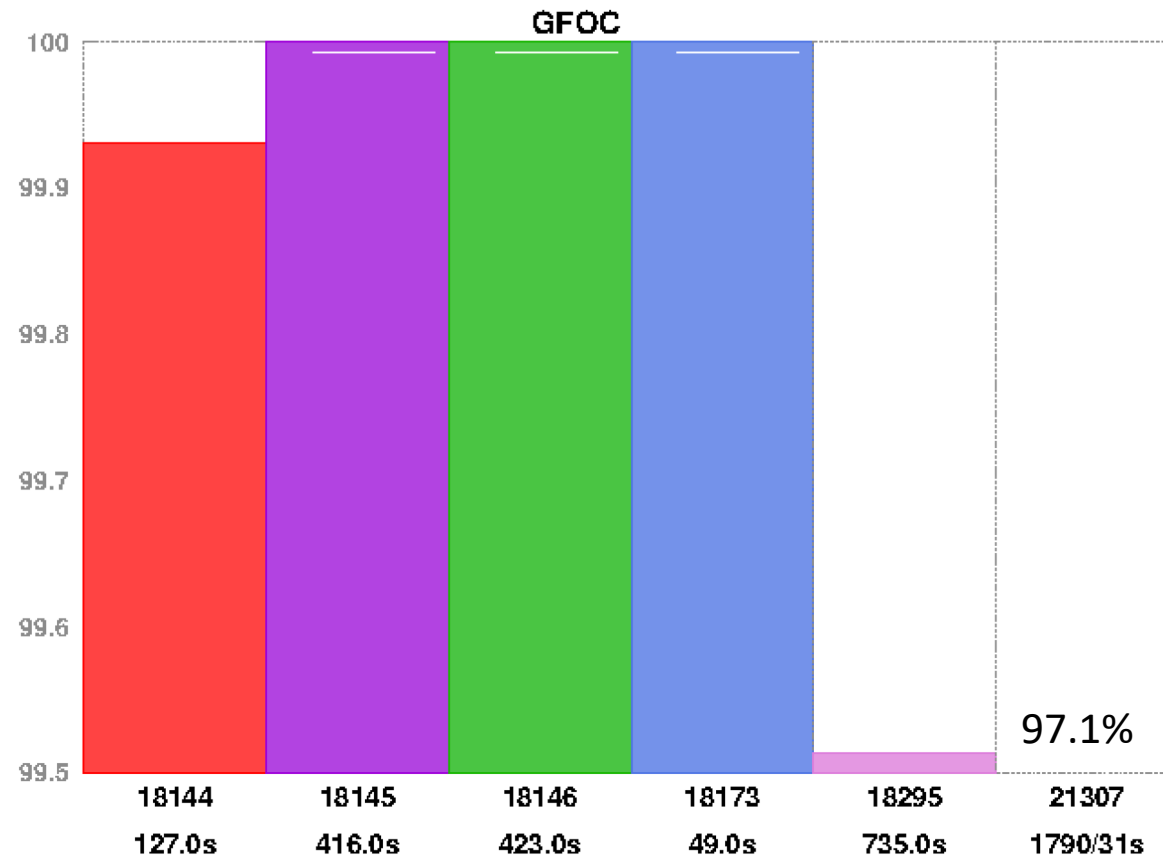
Kinematic orbit availability in 24-hrs for Sentinel-3A. The days (YYDOY) and maneuver durations ([s]) will be indicated at the x-axis in all figures

- Reduced-dynamic POD for small-maneuver days works fine, only visible impact from strong maneuvers.
- Kinematic POD has high availability and is hardly influenced by maneuvers, can be used as reference orbit.

# Internal orbit consistency: residuals



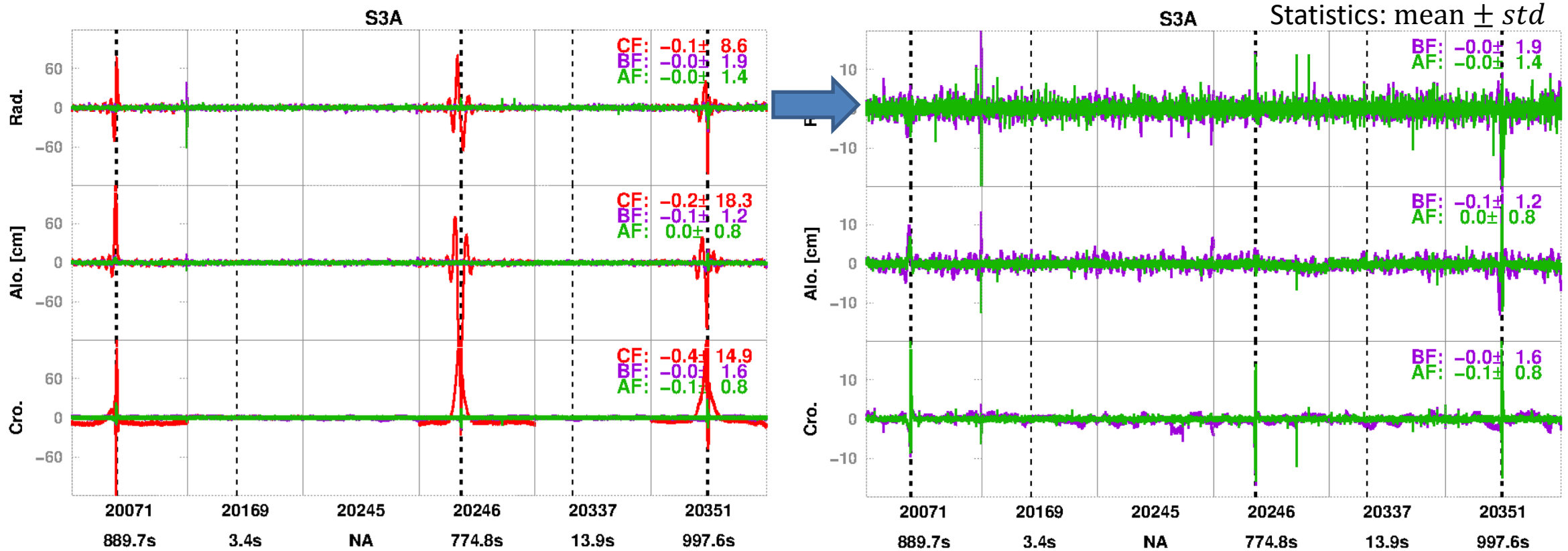
Ionosphere-free carrier-phase residuals and RMS statistics for the POD solution of GRACE-FO-C maneuver and reference days



Kinematic orbit availability in 24-hrs for GRACE-FO-C

- GRACE-FO satellites maneuvers can be better modeled due to smaller magnitude.

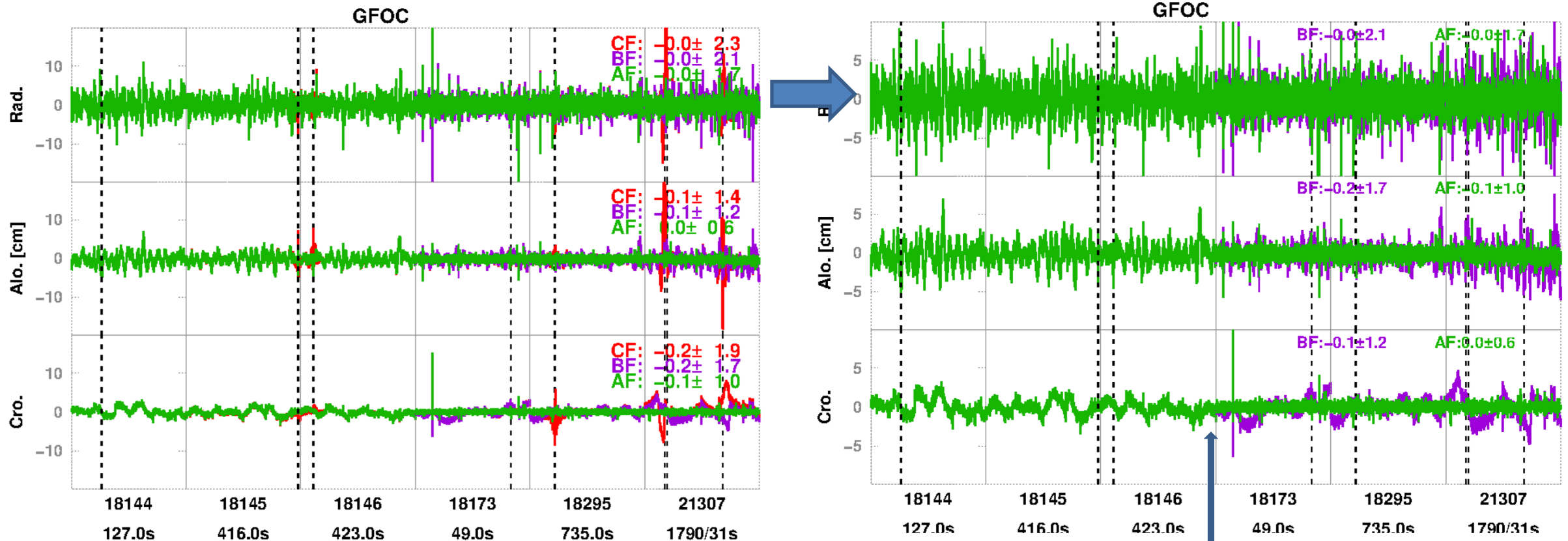
# Internal orbit consistency: RD-KN orbit



Kinematic/reduced-dynamic orbit consistency for the different Sentinel-3A orbit solutions. CF: only estimate accelerations; BF: CF + velocity pulses ( $\sigma = 1m/s$ ) depending on the maneuver duration; AF: BF + IAR, final POD result for the next analyses

- Additional velocity pulses estimation is crucial for days with strong maneuvers.
- IAR further constrains parameter estimation and enhances POD for maneuver days.

# Internal orbit consistency: RD-KN orbit

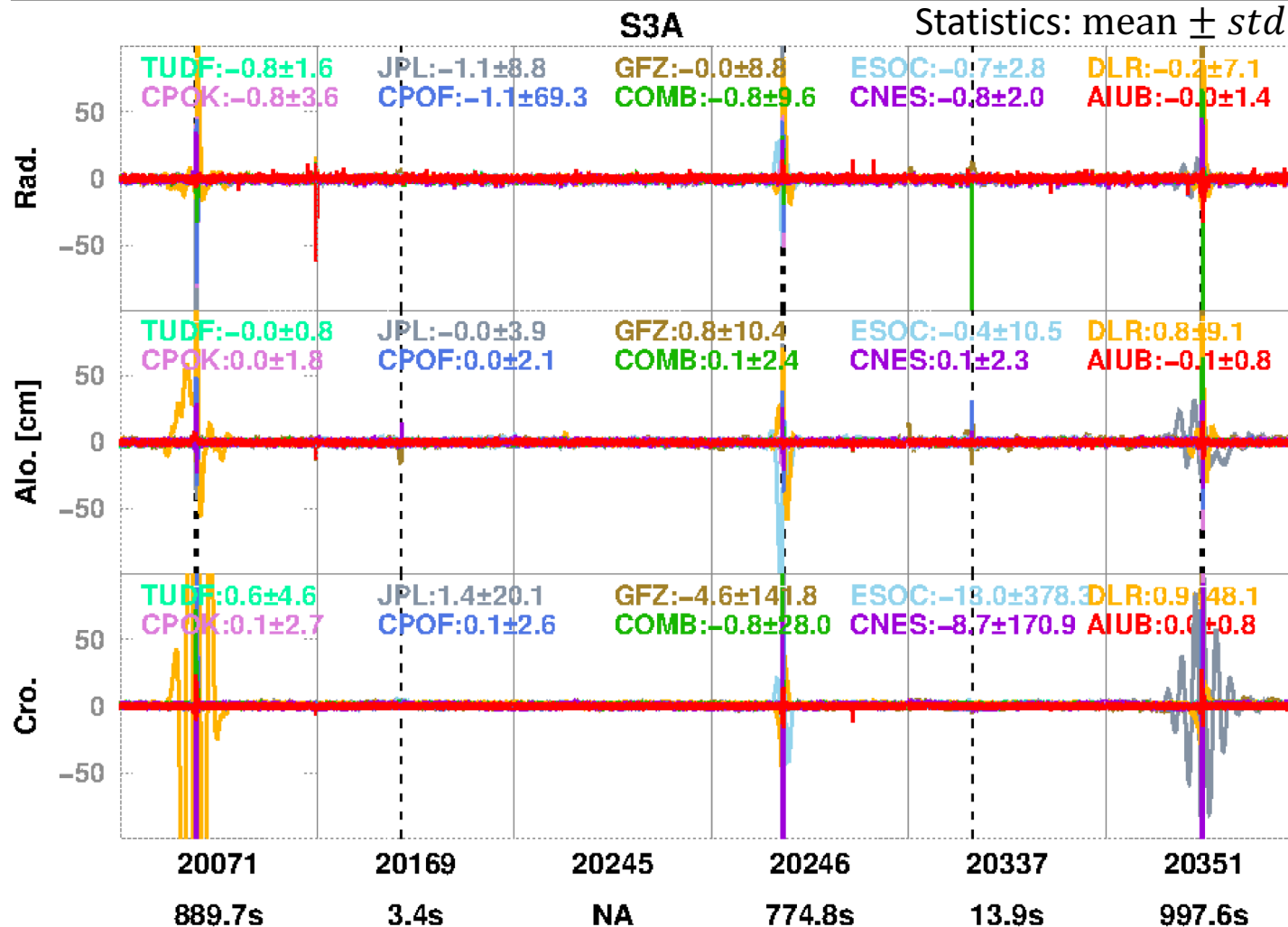


Kinematic/reduced-dynamic orbit consistency for the different GRACE-FO-C orbit solutions

**The operational CODE OSB product (for IAR) becomes available since mid-2018  
The repro products would be available longer back.**



# External orbit validation: comparisons



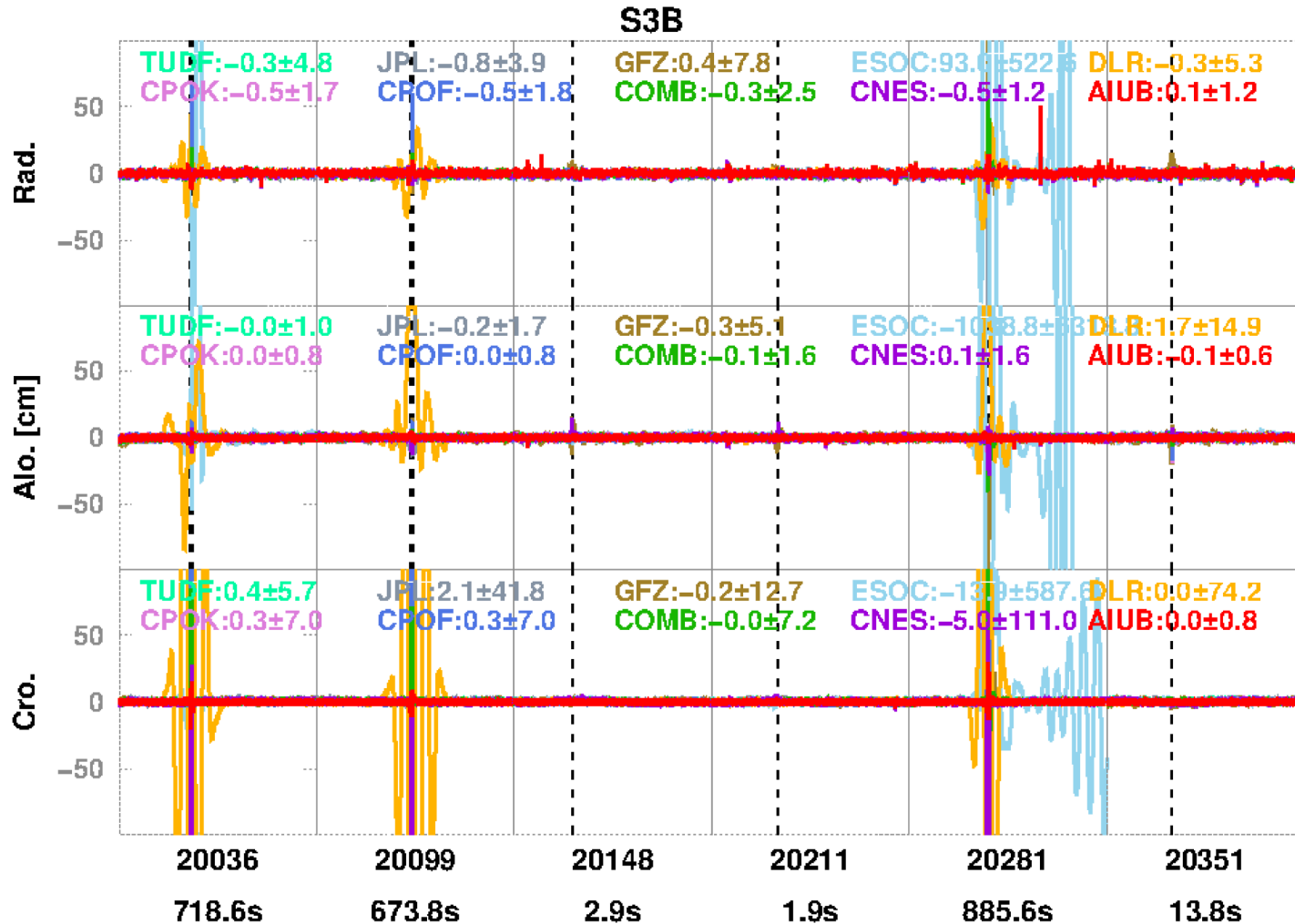
List of institutes with POD service for maneuver days (alphabet in descending order):

- TUDF: Delft University of Technology
- JPL: Jet Propulsion Laboratory
- GFZ: German Research Centre for Geosciences
- ESOC: European Space Operations Centre
- DLR: German Aerospace Centre
- CPOK: Official CPOD Orbit, kinematic
- CPOF: Official CPOD orbit, reduced-dynamic
- COMB: Combined solution of different orbits
- CNES: French Space Agency
- AIUB: Astronomical Institute, University of Bern

Consistency between the AIUB ambiguity-fixed kinematic orbit and orbits delivered by different members of the POD Quality Working Group for Sentinel-3A. No outlier screening



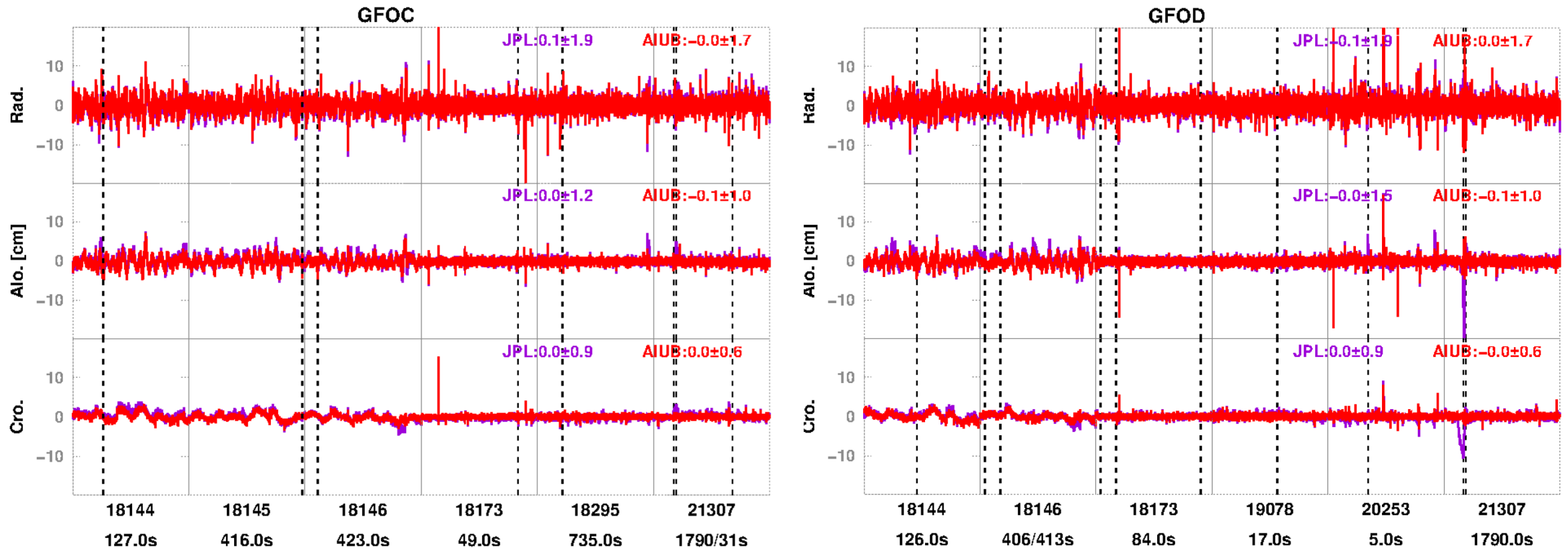
# External orbit validation: comparisons



Please notice that the operational orbits from different institutes do not necessarily make use of their best-tuned maneuver handling strategy

Consistency between the AIUB ambiguity-fixed kinematic orbit and orbits delivered by different members of the POD Quality Working Group for the Sentinel-3B. No outlier screening

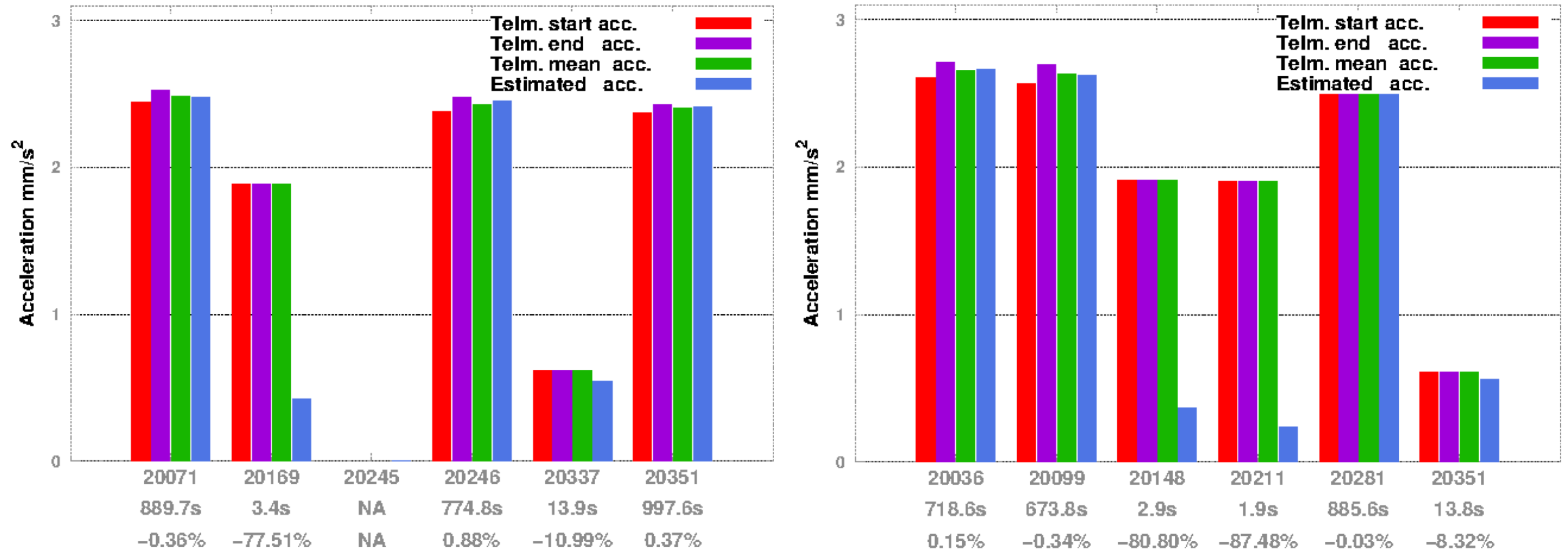
# External orbit validation: comparisons



Consistency between the AIUB ambiguity-fixed kinematic orbit, and AIUB reduced-dynamic orbits and JPL official orbits for GRACE-FO-C (left) and GRACE-FO-D (right). No outlier screening

- PODs for the maneuvering GRACE-FO satellites are more stable due to smaller maneuver accelerations.

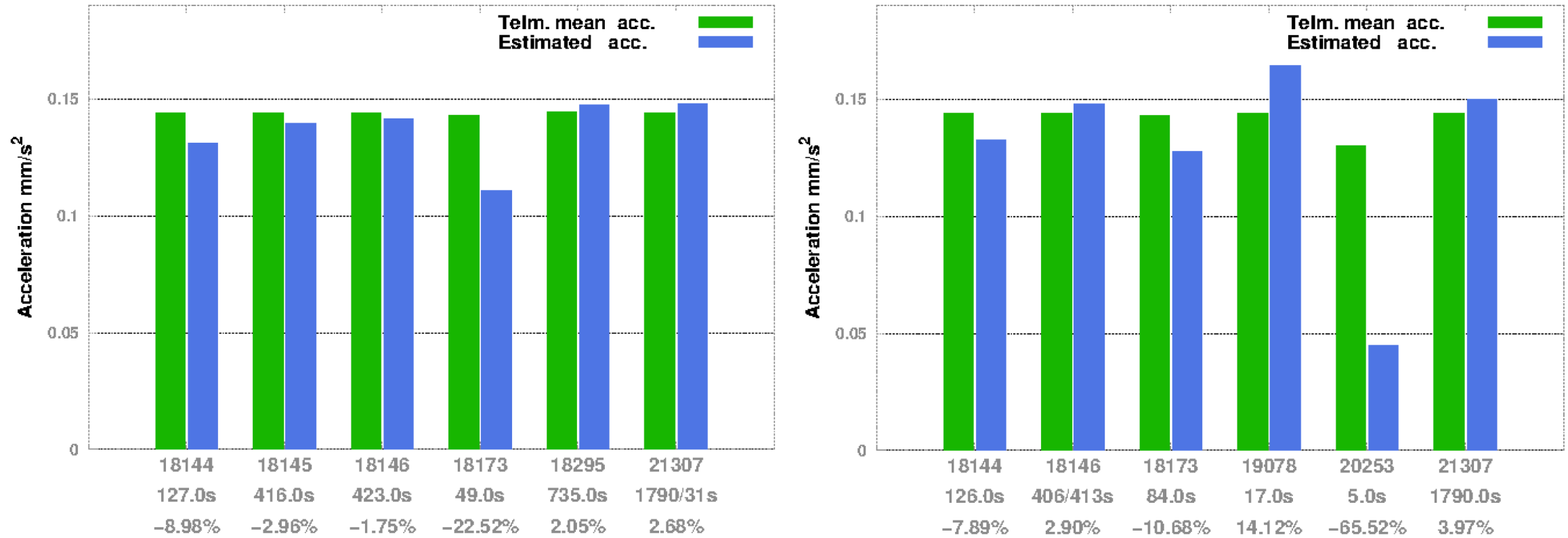
# External orbit validation: telemetry



Comparison between the start/end/mean maneuver accelerations from the telemetry data and the AIUB-estimated accelerations for Sentinel-3A (left) and Sentinel-3B (right). The differences are described as percentage ([%]) in the bottom

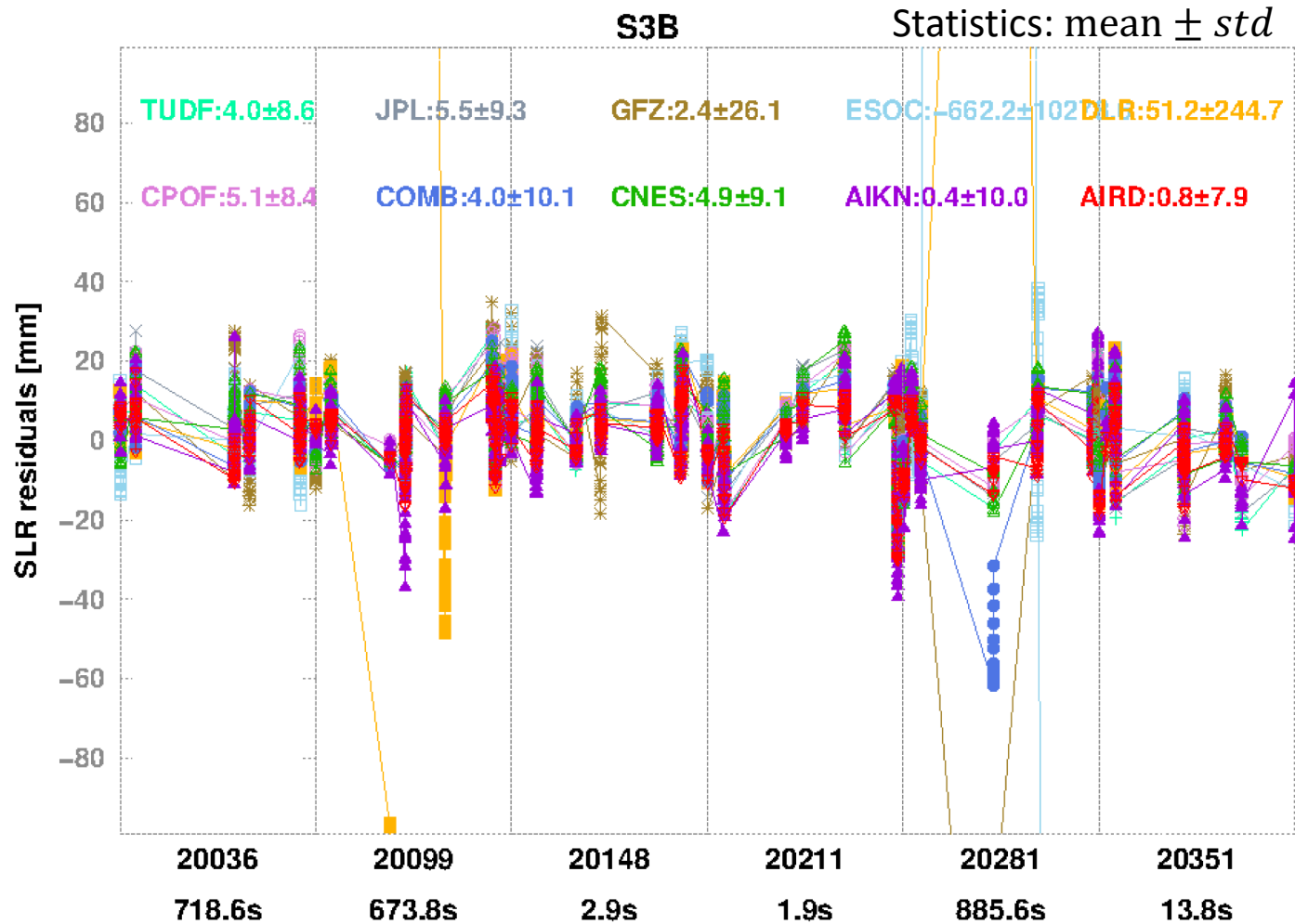
- For days with strong and long maneuver, the estimated accelerations agree well with the telemetry data.
- For days with small and short maneuver, the estimated accelerations clearly differ from the telemetry data.

# External orbit validation: telemetry



Comparison between the mean maneuver accelerations from the telemetry data and the AIUB-estimated accelerations for GRACE-FO-C (left) and GRACE-FO-D (right). The differences are described as percentage ([%]) in the bottom

# External orbit validation: SLR

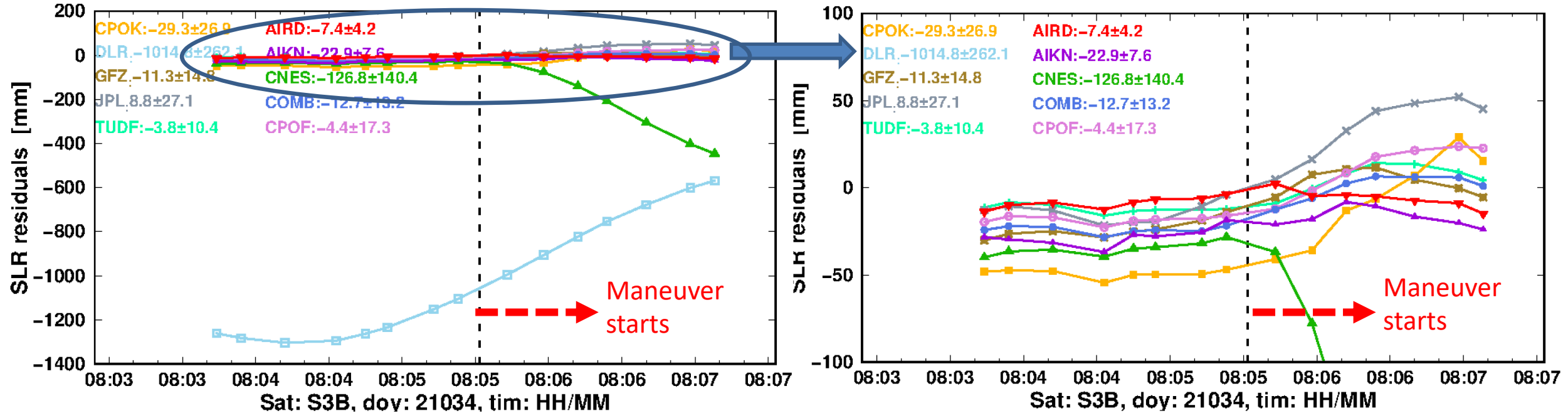


SLR validations to the different CPOD institute orbits for Sentinel-3B.  
10 selected stations, no data screening

Luckily, SLR validations are available for all the Sentinel-3B maneuvering days.

SLR validations show that some orbits can be significantly influenced due to maneuver processing that influences periods outside of maneuvers.

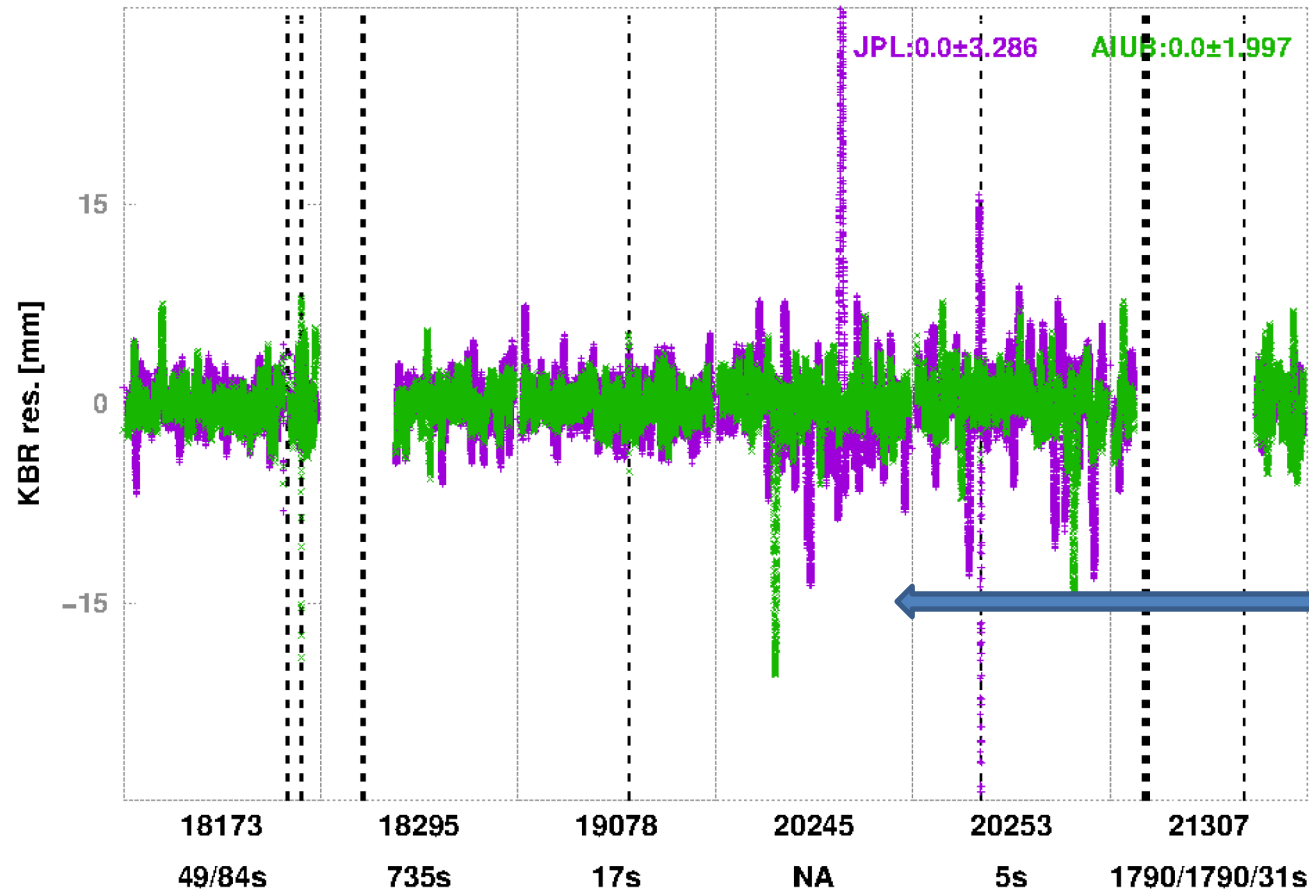
# External orbit validation: SLR



A single SLR tracking pass crossing the maneuver period is available for Sentinel-3B from the Tahiti SLR station on day 21034, with a strong maneuver lasting for 774.3s

- AIUB orbit is among the best in terms of agreement with SLR measurements crossing maneuvers.

# External orbit validation: KBR



Again, take day 20245 as reference.

Please note the receivers suffered from the switched on of flex power mode IV since 14-Feb-2020. Issues solved after 22-Jul-2021.

K-Band radar validations to the AIUB GRACE-FO orbit solutions and the JPL official orbit

- AIUB orbit solutions show reliable POD quality for the maneuver days.



# Conclusions

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- Kinematic orbit is free from satellite dynamics, can be used as a good reference orbit.
- Additional velocity pulses estimation is crucial for days with strong and long maneuvers, in particular for the Sentinel-3 satellites.
- Integer ambiguity resolution further constrains parameter estimation and enhances POD for maneuver days.
- The estimated accelerations agree well with telemetry data for days with long and strong maneuvers, but show large discrepancy for days with short and small maneuvers.
- SLR and KBR validations can be used to check the POD performances during maneuvers.

# References

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- Allende-Alba, G., Montenbruck, O., Ardaens, J.S., Wermuth, M., Hugentobler, U., 2017: Estimating maneuvers for precise relative orbit determination using GPS. *Advances in Space Research*, Vol. 59 (1), pp.45-62, 2017. DOI 10.1016/j.asr.2016.08.039.
- Arnold, D., O. Montenbruck, S. Hackel, K. Sośnika; 2018: Satellite laser ranging to low Earth orbiters: orbit and network validation. *Journal of Geodesy*, Vol. 93(11), pp 2315-2334, 2018. DOI 10.1007/s00190-018-1140-4.
- Ju, B., Gu, D., Herring, T.A., Allende-Alba, G., Montenbruck, O., Wang, Z., 2017: Precise orbit and baseline determination for maneuvering low earth orbiters. *GPS solutions*, Vol. 21(1), pp.53-64, 2017. DOI 10.1007/s10291-015-0505-x.
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- Schaer, S., A. Villiger, D. Arnold, R. Dach, L. Prange, A. Jäggi; 2021: The CODE ambiguity-fixed clock and phase bias analysis products: generation, properties, and performance. *Journal of Geodesy*, Vol. 95 (8), 2021. DOI 10.1007/s00190-021-01521-9.

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