

SLR observations to spherical and GNSS satellites and their combined analysis with GNSS microwave observations

Daniela Thaller

Astronomical Institute, University of Bern, Switzerland

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Overview

- SLR analysis for spherical satellites
- SLR residual analysis for GNSS satellite orbits
- Combined GNSS–SLR analysis

SLR analysis for spherical satellites

- *Bernese GPS Software (BSW)* has been extended:
 - Orbit modelling for **spherical satellites**
 - Handling / analysis of **SLR observations**
- **Cooperation with BKG** (Frankfurt/Main, Germany):
 - BKG is **ILRS Analysis Center**
 - Contribution of BKG to the ILRS is based on *BSW* since **July 2010**



SLR analysis for spherical satellites

Typical parameter set-up in weekly SLR solutions:

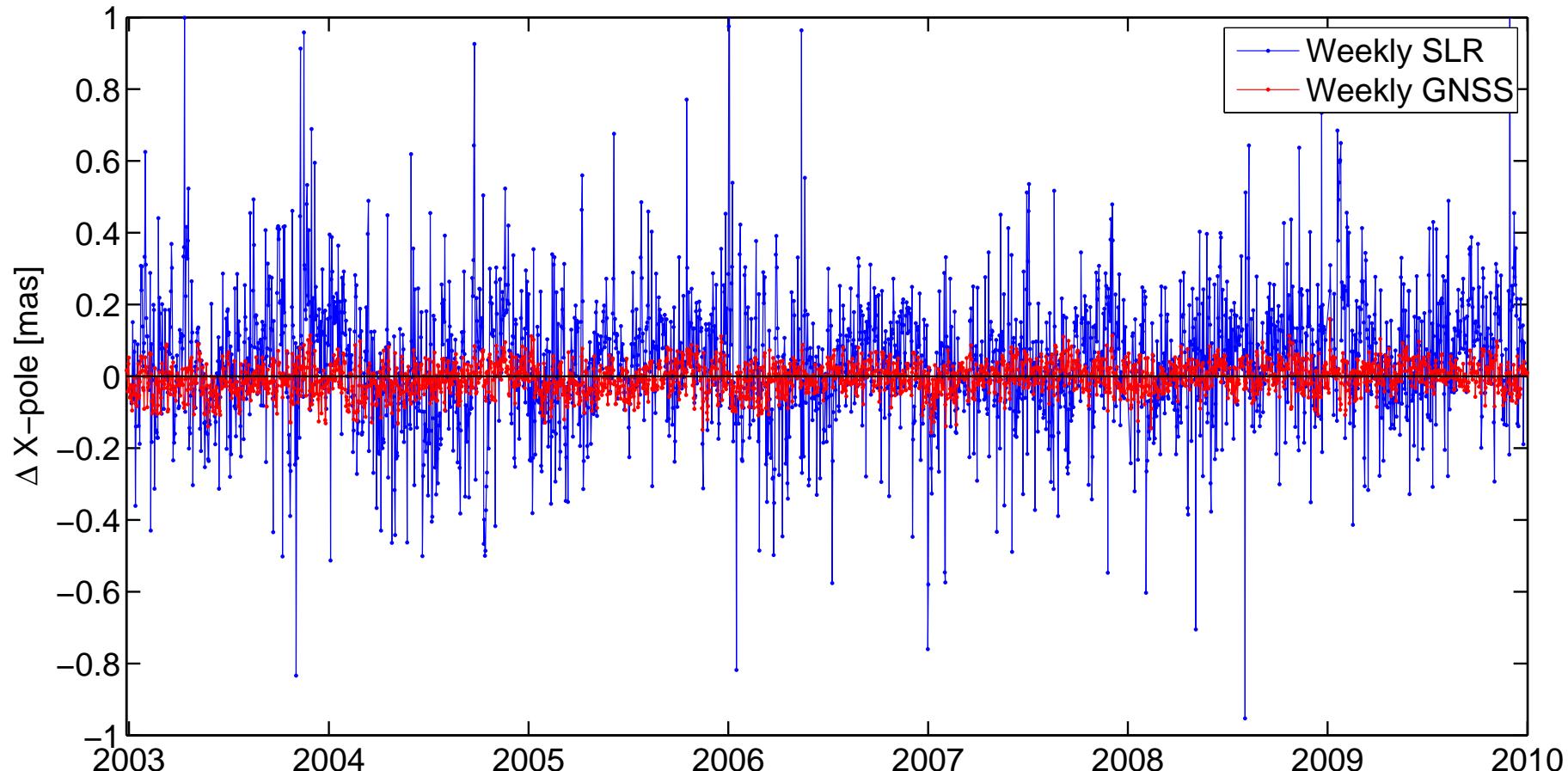
- Station coordinates
- Earth Rotation Parameter:
 - Polar motion
 - Length of Day (LOD)
- Satellite orbits:
 - 6 Osculating elements
 - Empirical orbit parameters:
 - Constant along-track acceleration
 - Once-per-revolution along-track parameters
 - Once-per-revolution cross-track parameters
- Range biases (for selected sites)



~ 120 – 140
Parameters
per week

SLR analysis for spherical satellites: ERP

Comparison with IERS-08-C04



Mean Bias = 36 μas

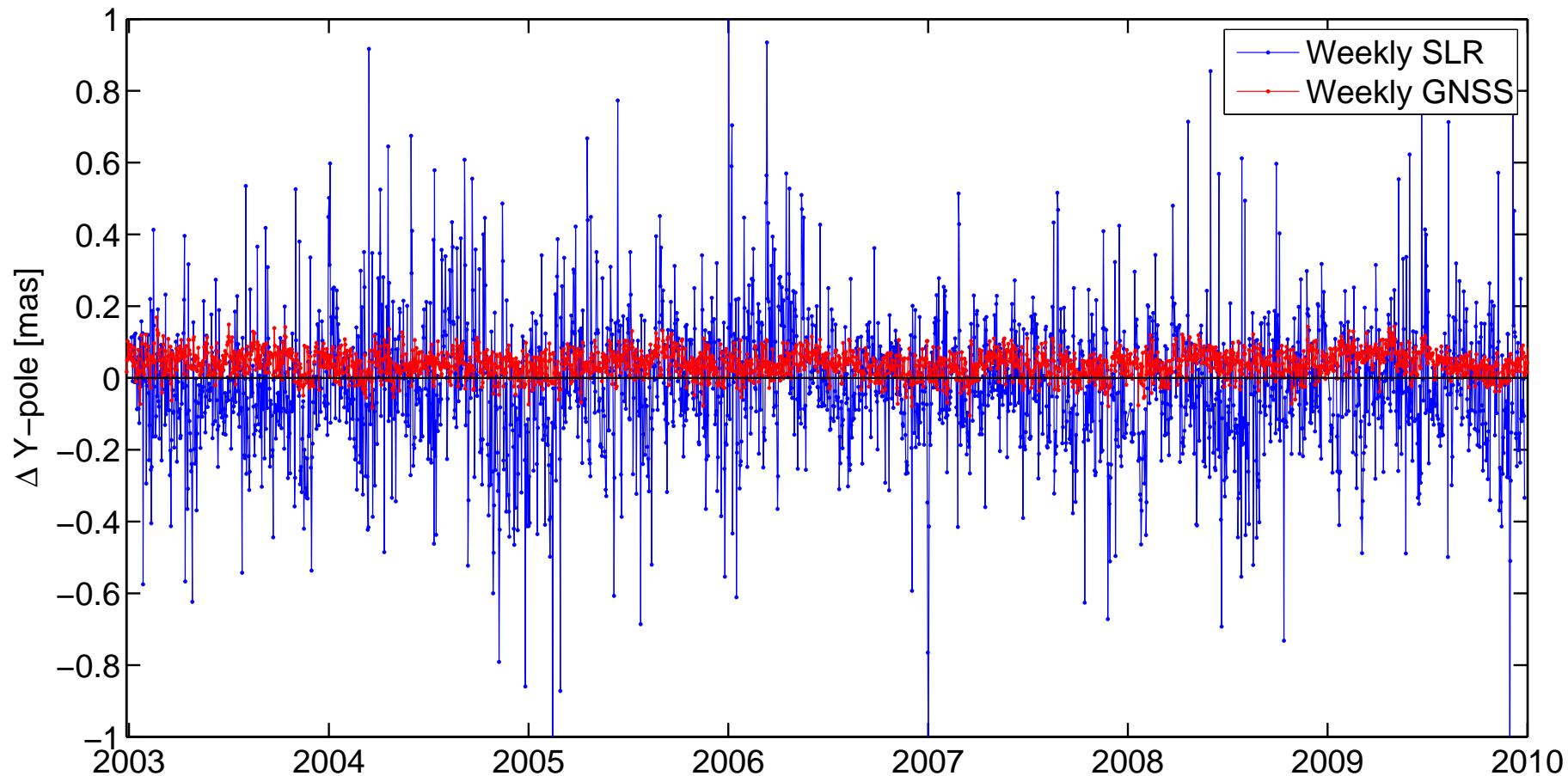
-6 μas

RMS = 141 μas

46 μas

SLR analysis for spherical satellites: ERP

Comparison with IERS-08-C04



Daniela Thaller: SLR and combined SLR-GNSS analysis at AIUB
Séminaire at Observatoire de Paris, 4. June 2012

Mean Bias = $-21 \mu\text{as}$

$42 \mu\text{as}$

RMS = $145 \mu\text{as}$

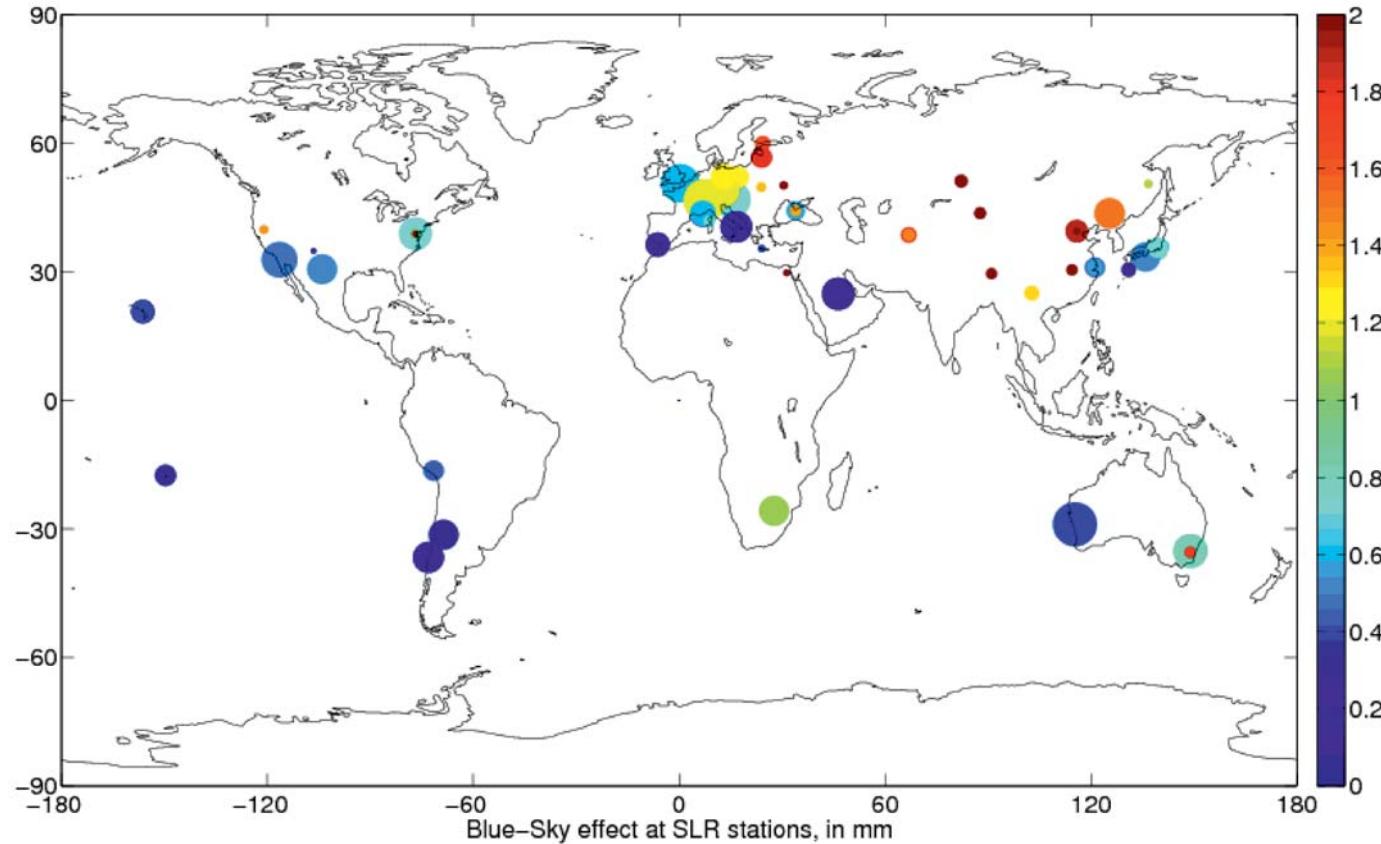
$40 \mu\text{as}$

SLR analysis: «Blue–Sky Effect»

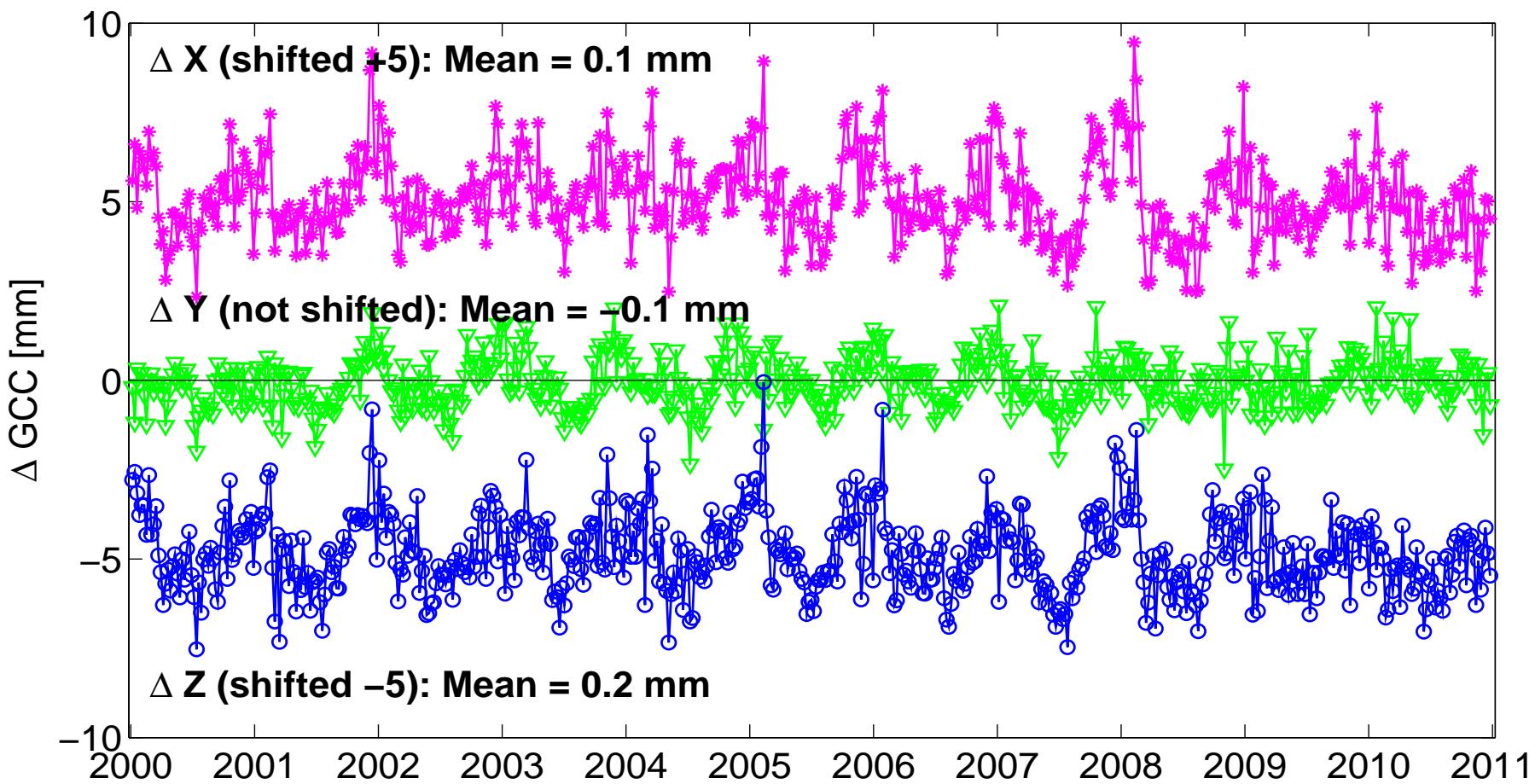
SLR observations are possible only at cloudless sky

= usually high pressure

⇒ Systematic **atmospheric loading** on SLR stations: up to **2 mm**



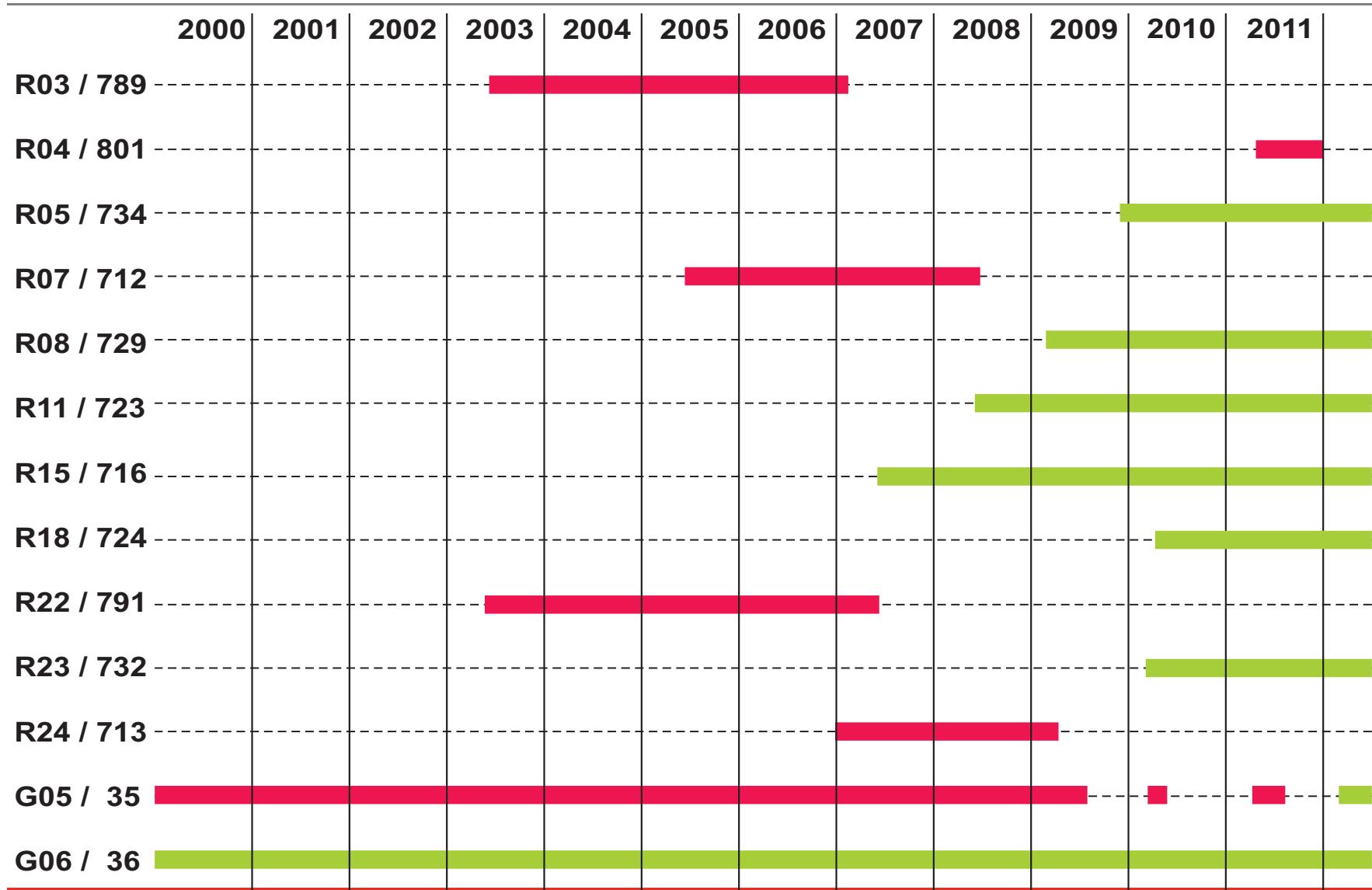
Impact of atmospheric loading



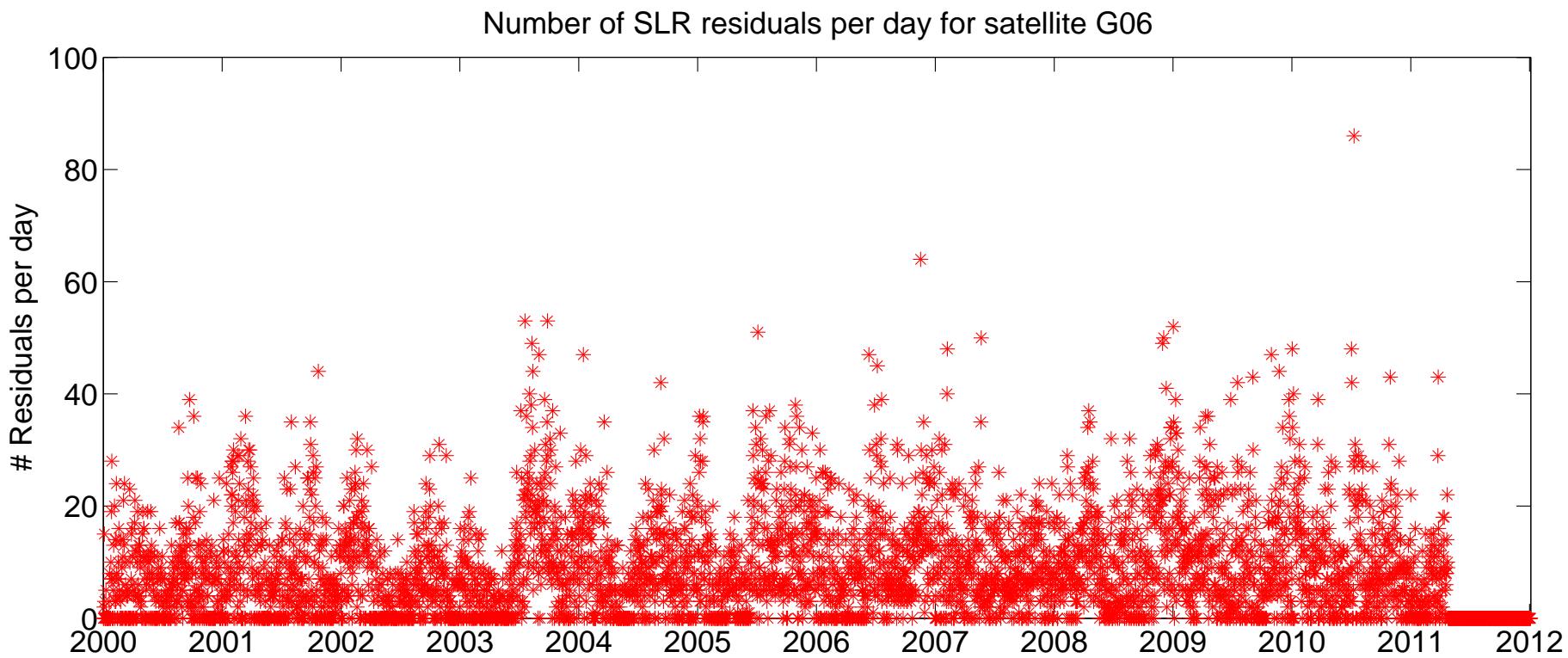
SLR tracking of GNSS satellites

- Several GNSS satellites are tracked by SLR:
 - **Independent validation** of the orbit computation based on microwave data
 - **Combined GNSS–SLR** analysis (satellite co-location)
- SLR residual computation at AIUB:
 - GNSS satellite orbits (and ERPs) computed at the CODE Analysis Center of the IGS
 - SLCF2008 station coordinates
 - A daily report is sent to the ILRS

SLR tracking of GNSS satellites



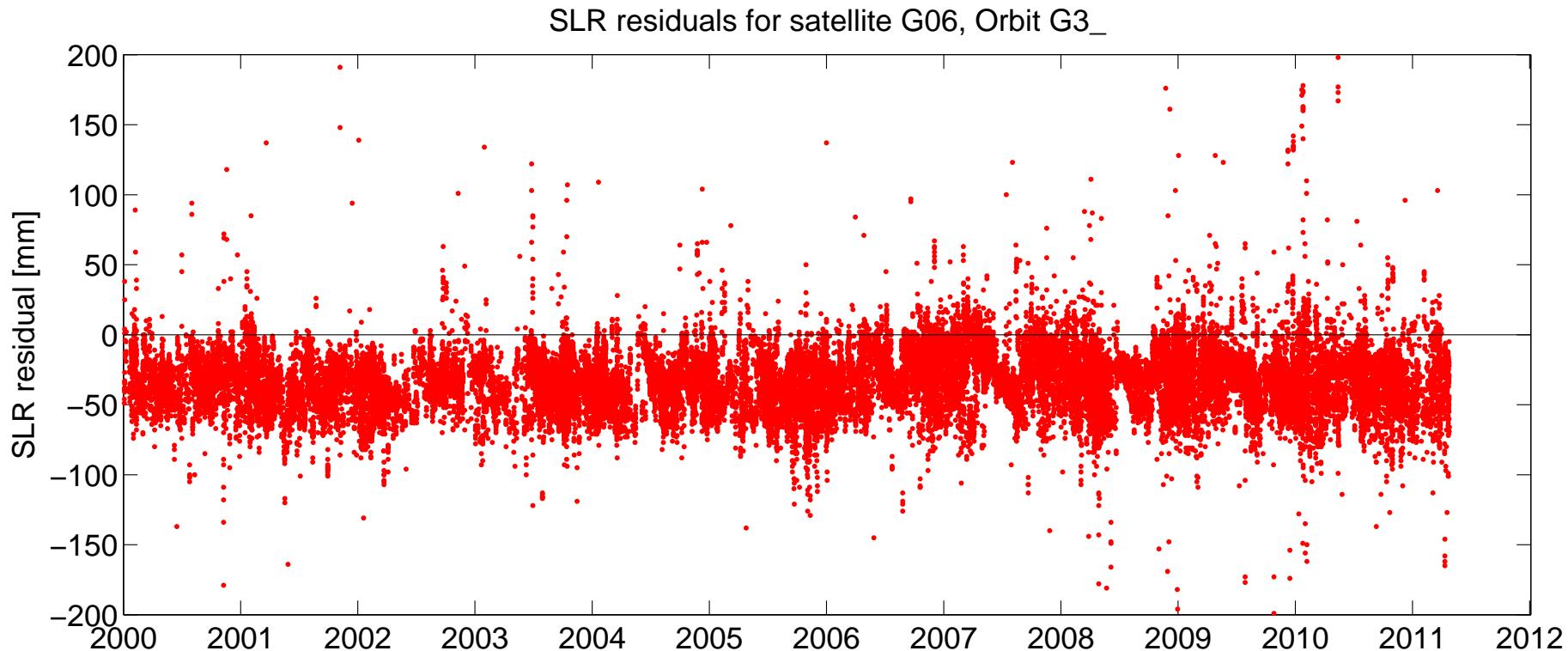
SLR tracking of GNSS satellites



Number of observations per day / per satellite is very small:

- GPS: ~ 10 – 15
- GLONASS: ~ 20 – 30

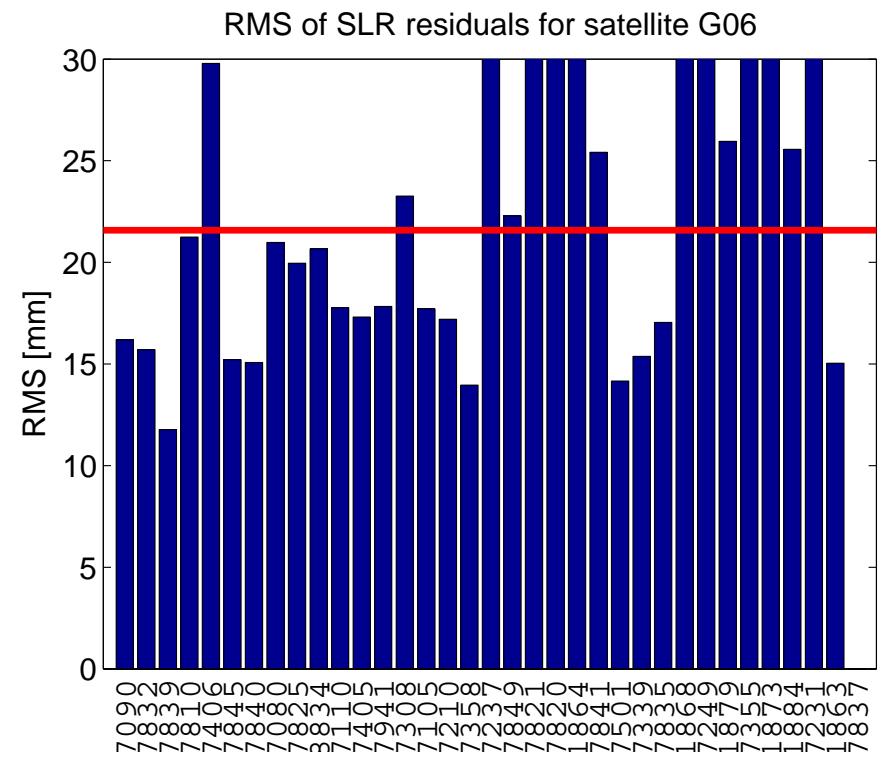
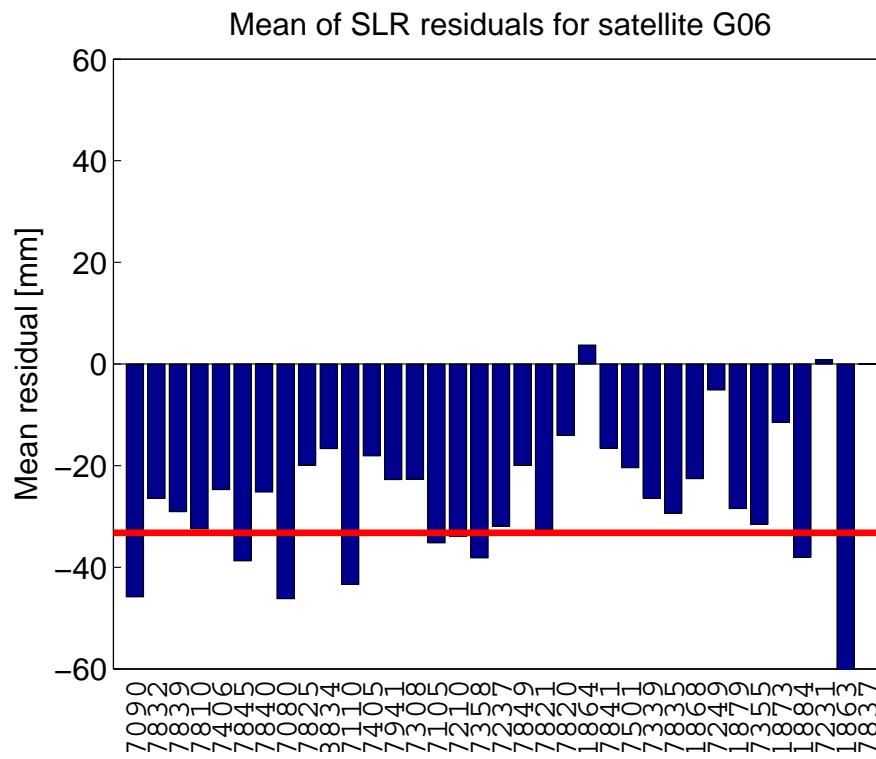
SLR residual analysis for GNSS orbits



- Overall Mean Bias = -33.2 mm
- Overall RMS = 21.6 mm

But: Bias and RMS are **station-dependent**

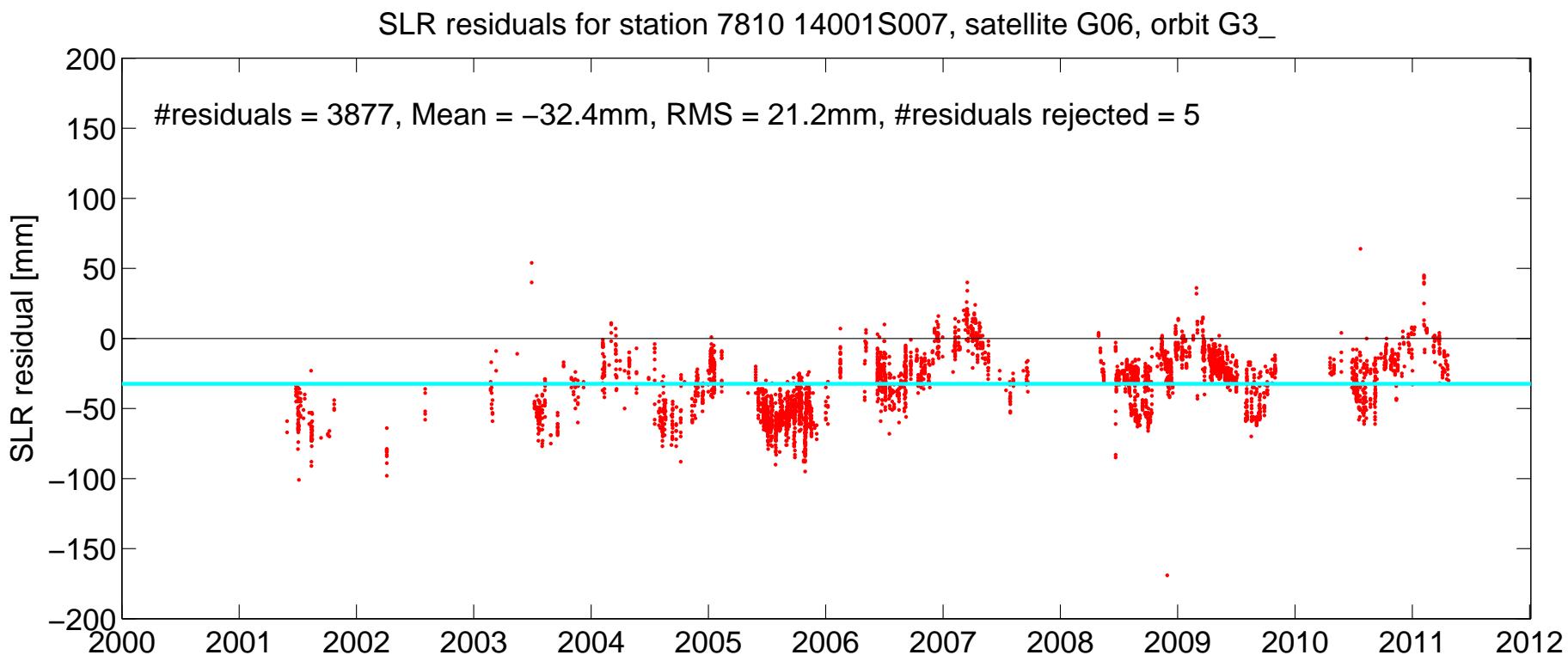
SLR residual analysis for GNSS orbits



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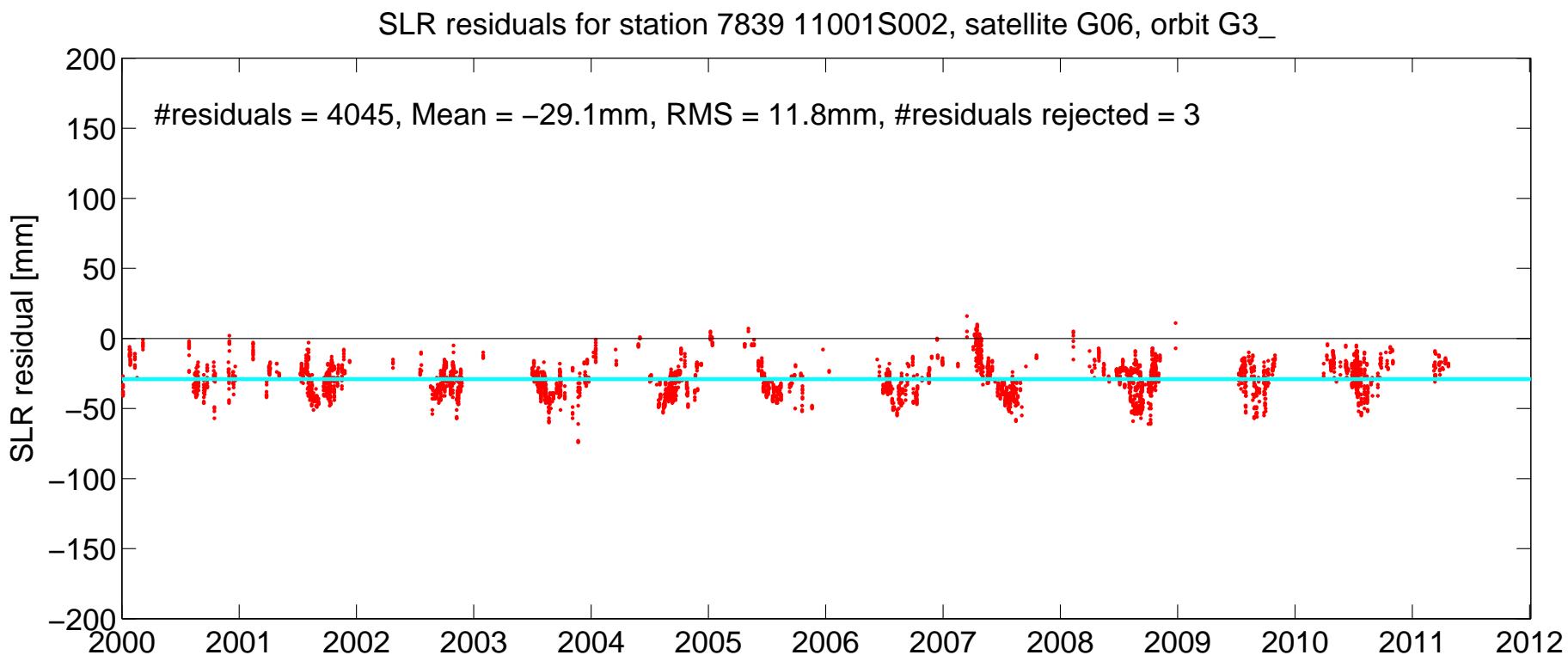
But: Bias and RMS are **station-dependent**

SLR residual analysis for GNSS orbits



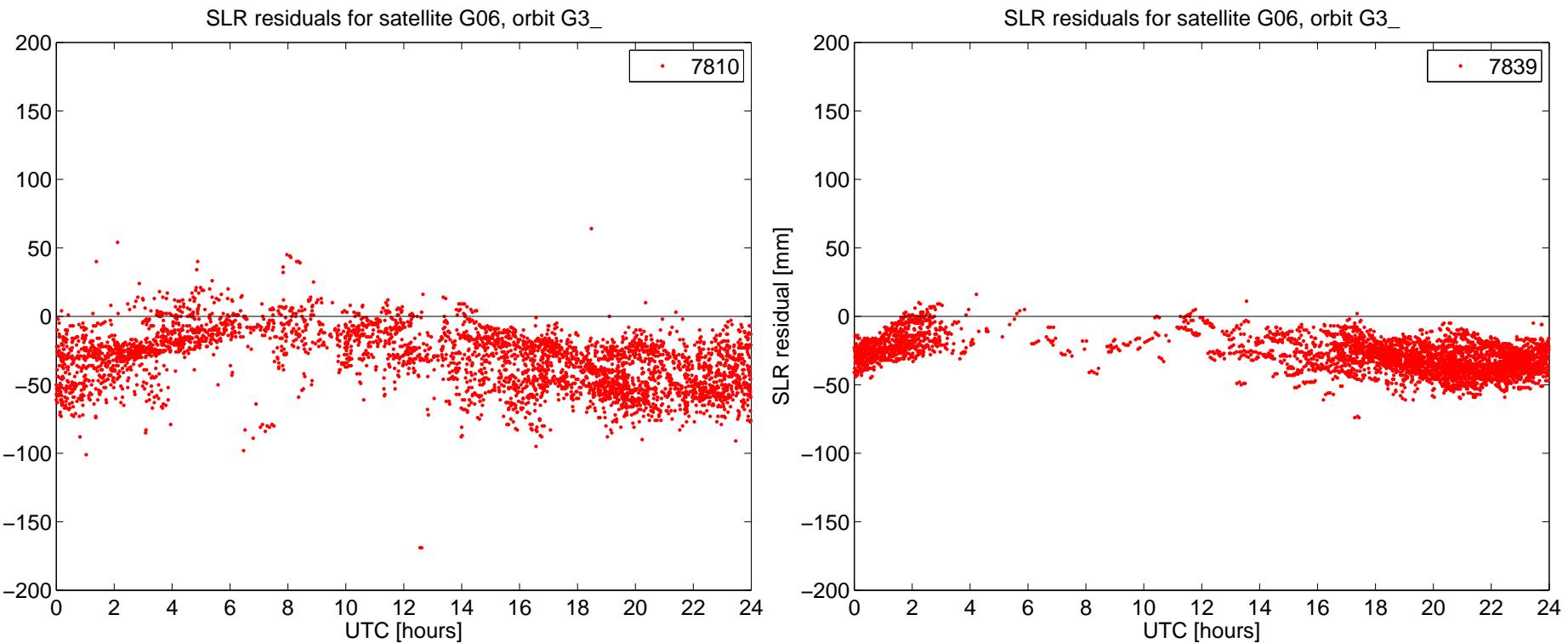
- Even time-dependent variations are visible:
 - Station upgrades
 - Seasonal

SLR residual analysis for GNSS orbits



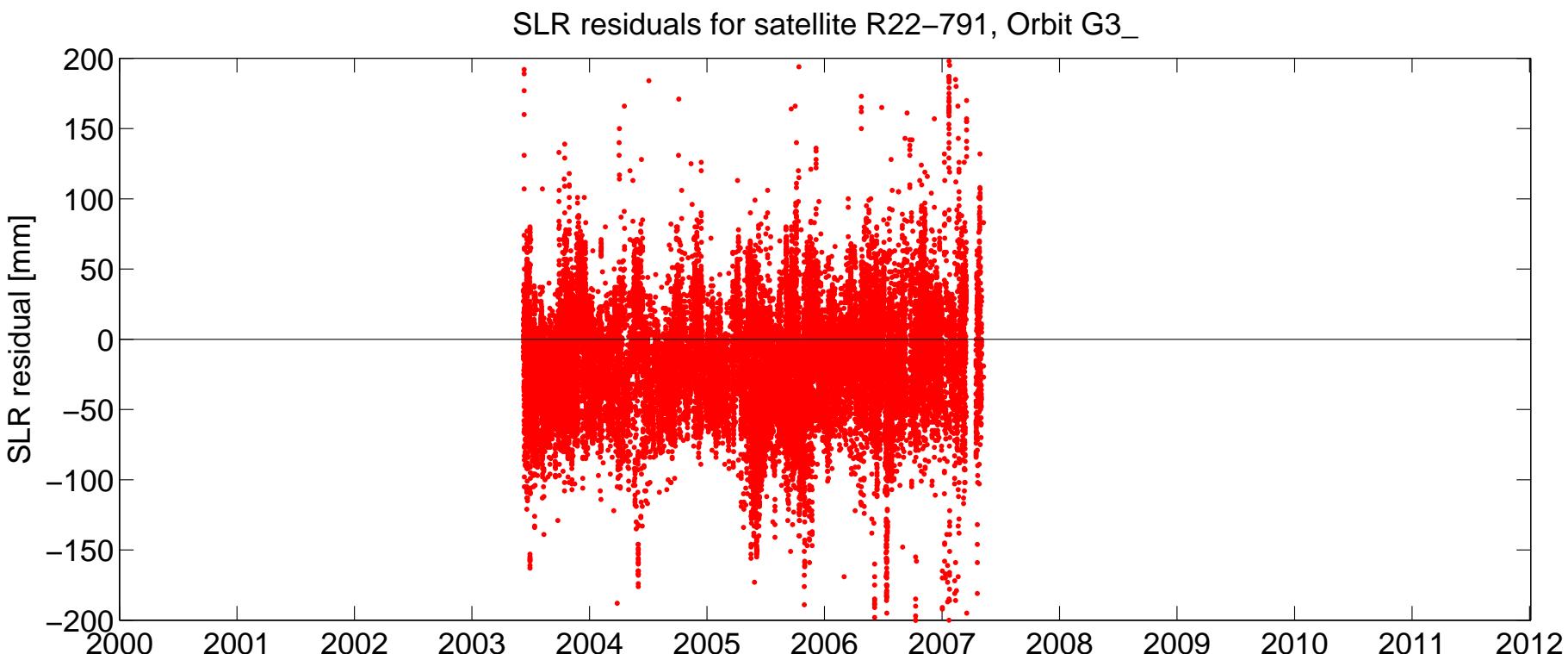
- Even time-dependent variations are visible:
 - Seasonal

SLR residual analysis for GNSS orbits



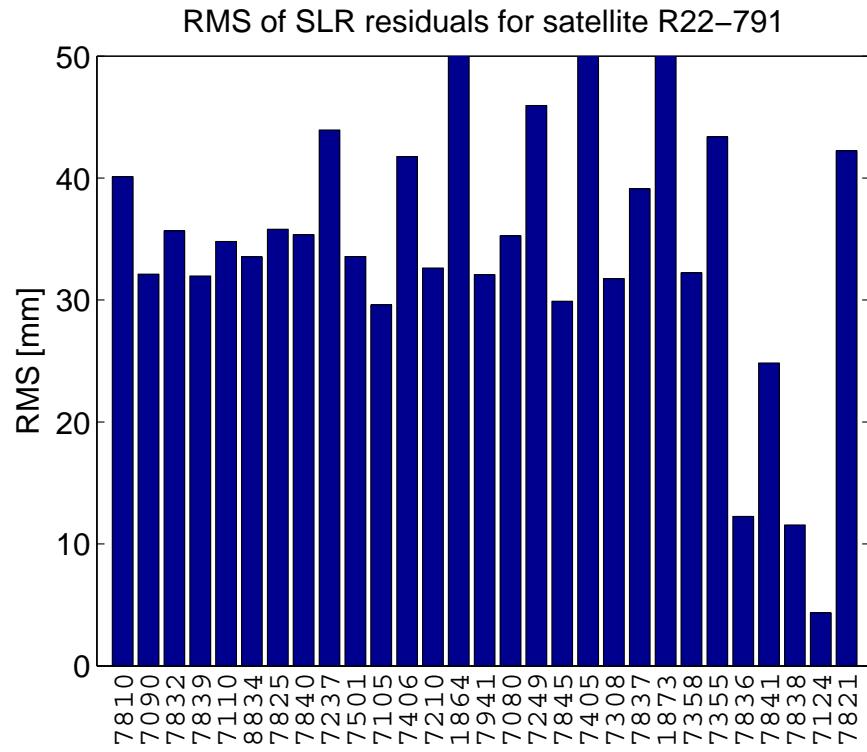
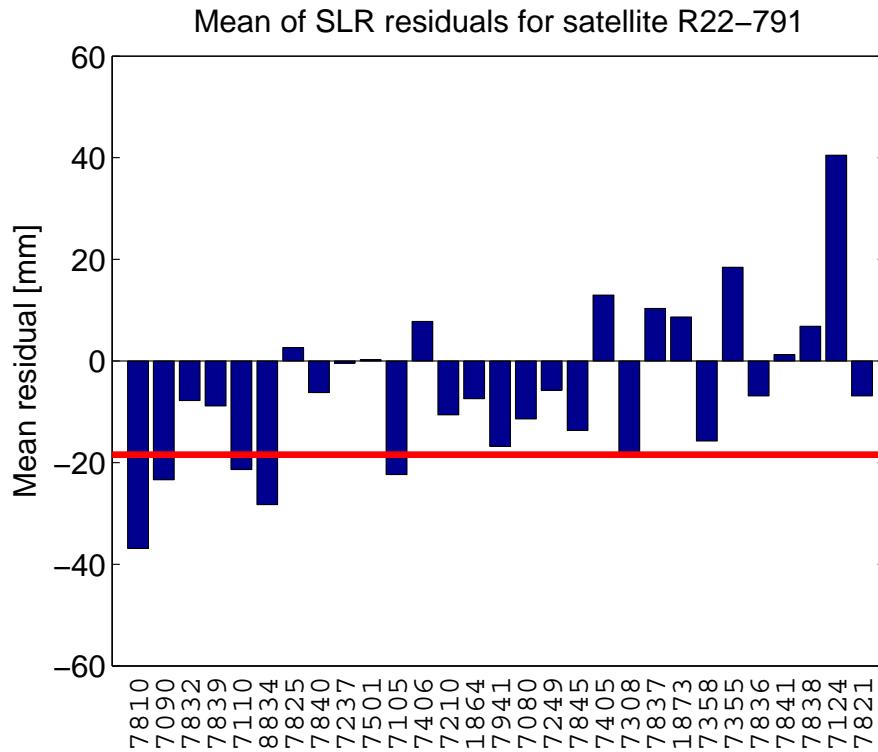
- Even time-dependent variations are visible:
 - Daily

SLR residual analysis for GNSS orbits

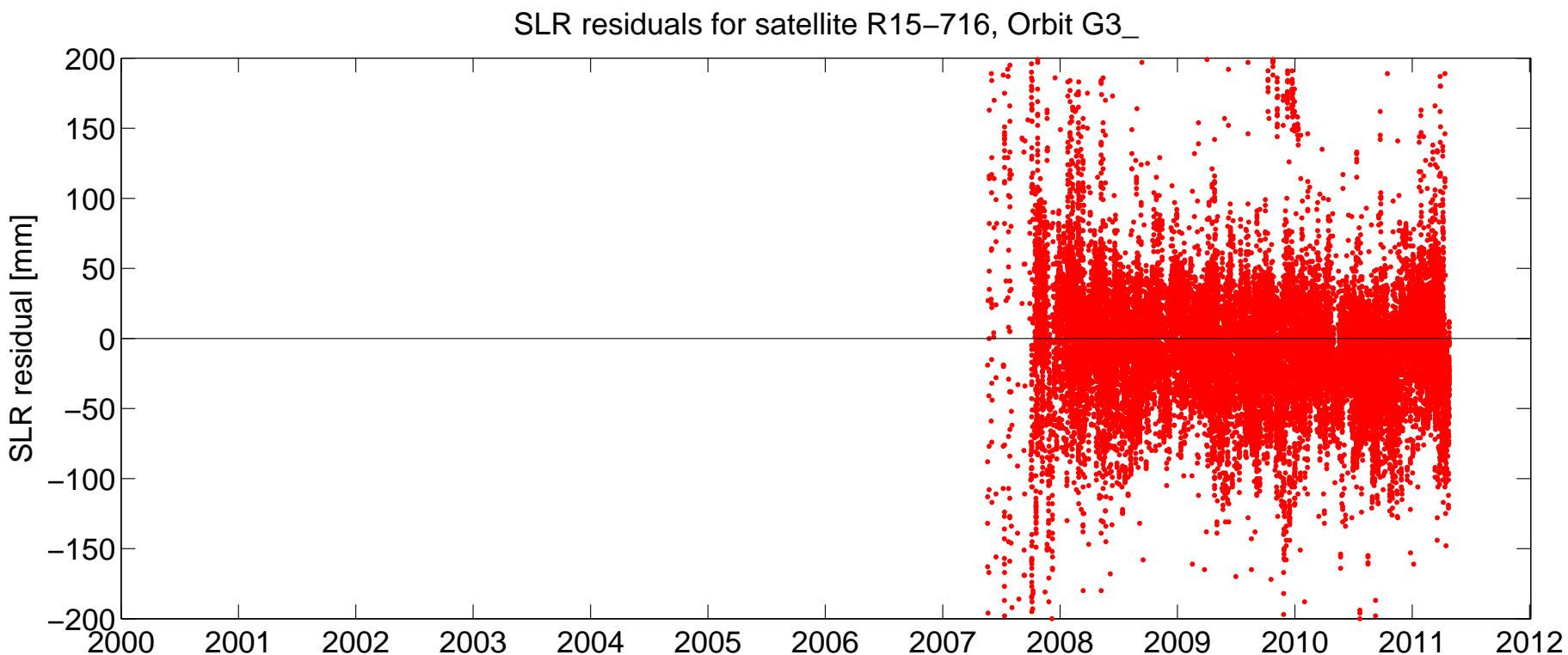


- Overall Mean Bias = -18.4 mm
- Overall RMS = 38.9 mm

SLR residual analysis for GNSS orbits

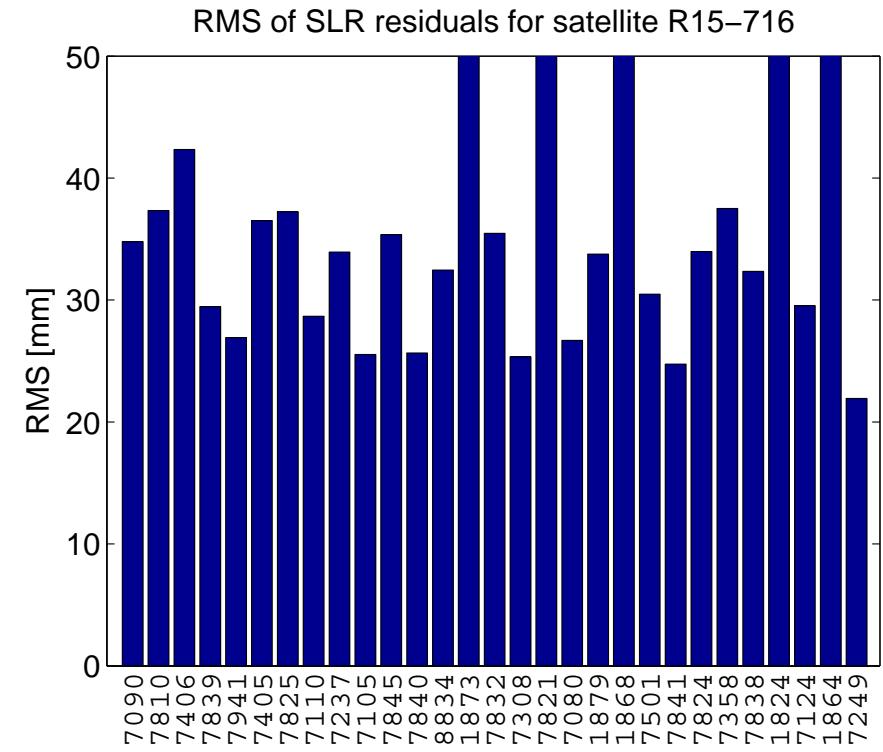
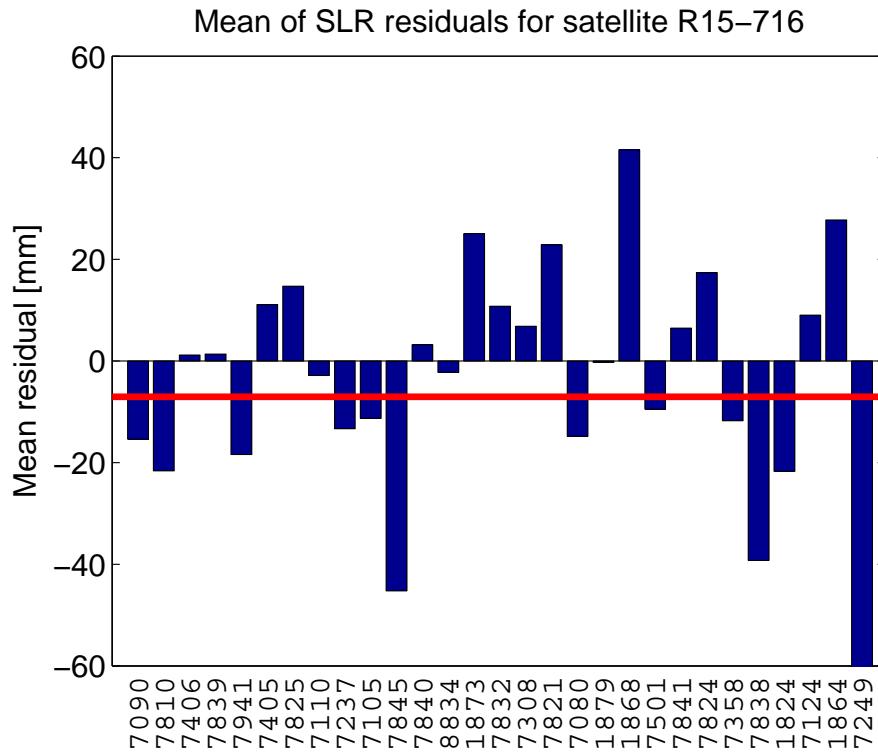


SLR residual analysis for GNSS orbits



- Overall Mean Bias = -7.0 mm
- Overall RMS = 40.3 mm

SLR residual analysis for GNSS orbits



- Overall Mean Bias = -7.0 mm
- Overall RMS = 40.3 mm

SLR residual analysis for GNSS orbits

Satellite PRN-SVN	# SLR observations	Overall mean bias [mm]	Overall RMS [mm]
G06- 36	37124	-33. 21	21. 58
G05- 35	32981	-31. 53	20. 03
R22-791	30047	-18. 42	38. 86
R15-716	29899	- 7. 03	40. 33
R03-789	29059	-17. 79	41. 89
R07-712	21317	-12. 30	38. 64
R11-723	20873	-28. 01	37. 23
R08-729	20273	-33. 15	32. 04
R24-713	17626	-19. 72	43. 59
R23-732	7006	-16. 77	31. 87
R05-734	4245	-12. 92	28. 63
R18-724	3412	-12. 83	30. 84

SLR residual analysis for GNSS orbits

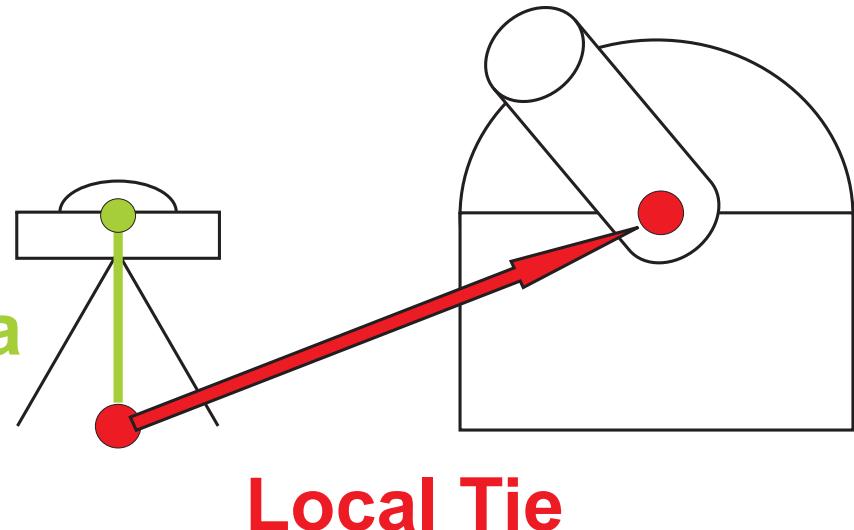
What is influencing the SLR residuals?

- Errors in SLR station coordinates
 - Errors in offsets of the laser reflector array (LRA)
 - Un-calibrated SLR range biases for high satellites
 - Quality of GNSS orbits:
 - Problems in satellite orbit modelling
 - Satellite antenna offsets (and phase center variations)
 - Network used to determine orbits (\Rightarrow GLONASS issue)
 - Inconsistencies in GNSS and SLR reference frame
- Combined analysis including estimation of parameters for possible error sources

Combined GNSS–SLR analysis: Co-locations

Station co-location
vs.
Satellite co-location

Phase
Center
+
Antenna
Height



Co-location at stations (e.g., for actual ITRF computation):

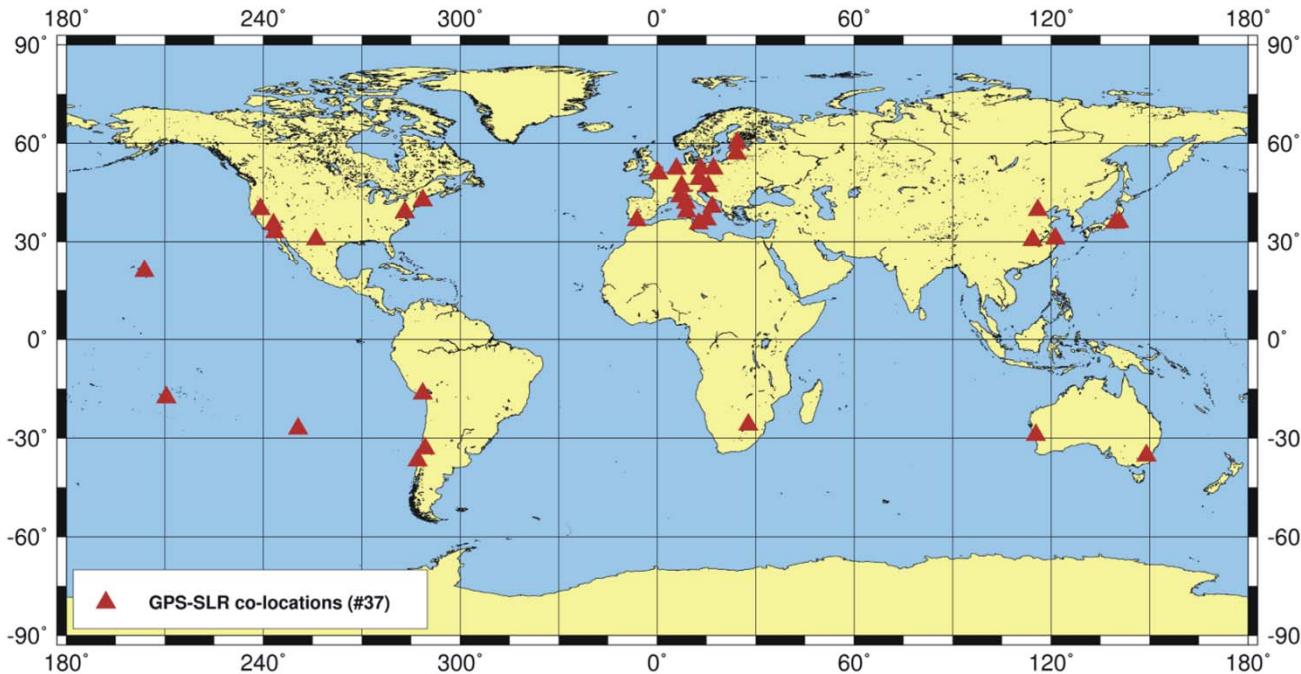
- Application of known **local tie** values
- GNSS observations of ground network
- SLR observations to LAGEOS etc.

- Independent of **satellite** tracked
- **Local ties** from terrestrial measurements

Combined GNSS–SLR analysis: Co-locations

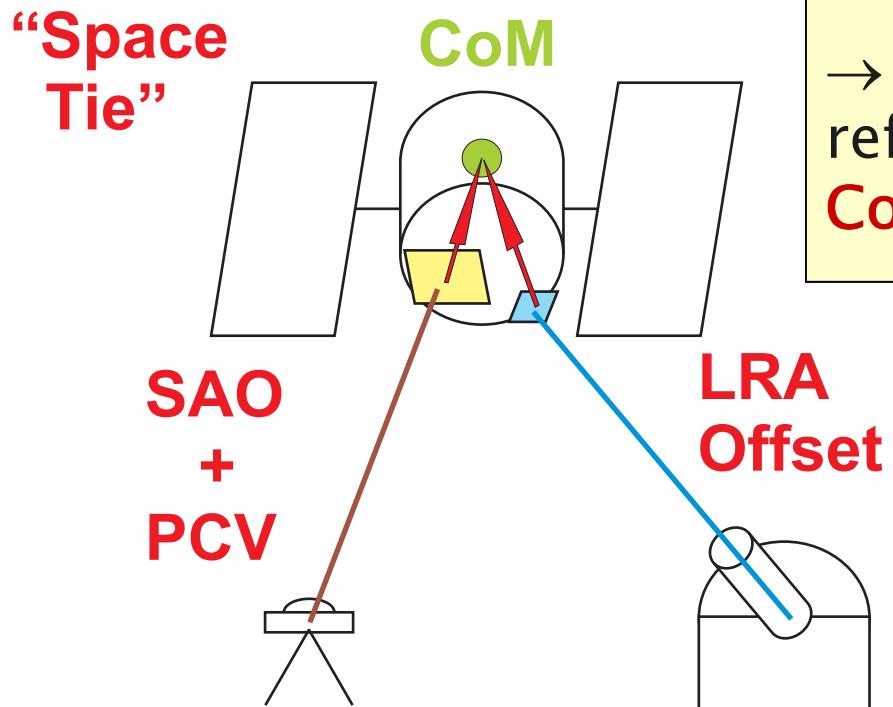
Station co-location vs. Satellite co-location

- bad **global distribution** of co-located sites
- only **few** co-locations (37)
- questions concerning **accuracy, transformation** local→global



Combined GNSS–SLR analysis: Co-locations

Station co-location
vs.
Satellite co-location



Co-location at GNSS satellites

=

Common orbit parameters from
GNSS microwave and SLR range
data

→ Vectors of GNSS and SLR
reference points w.r.t. satellite
CoM needed

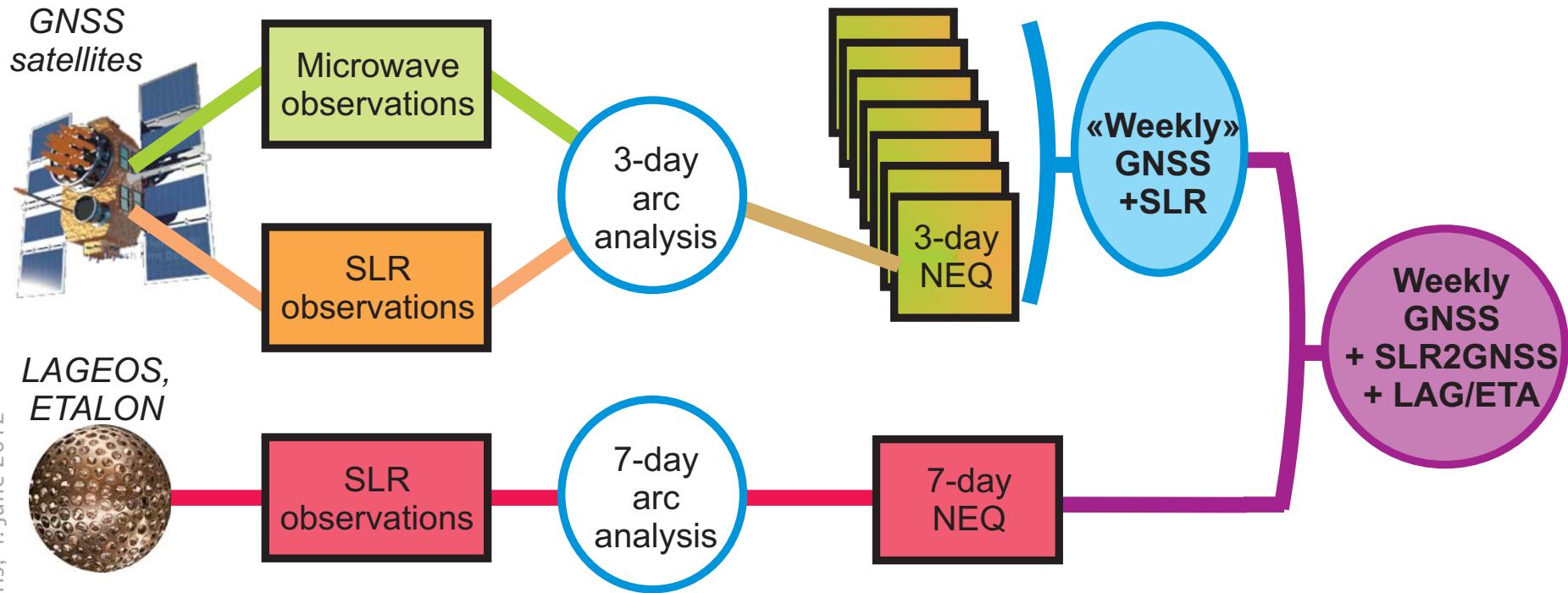
Combined GNSS–SLR analysis

Common parameters for combination:

- Direct combination
- Indirect combination by applying correction terms («Local ties»)

Parameter	GNSS microwave	SLR@GNSS	SLR spherical satellites
Station coordinates	GNSS	SLR	SLR
ERP	X	X	X
Orbits GNSS satellites	X	X	
Orbits spherical satellites			X
Geocenter	X	X	X
Microwave SAO	X		
LRA offsets		X	
Range biases		X	X

Combined GNSS-SLR analysis



- Reprocessing 2000.0 – 2011.0:
 - CODE GNSS reprocessing using IGS08 models
 - SLR reprocessing
- *Bernese GNSS Software* for all processing steps:
 - Equivalent to combination at observation level

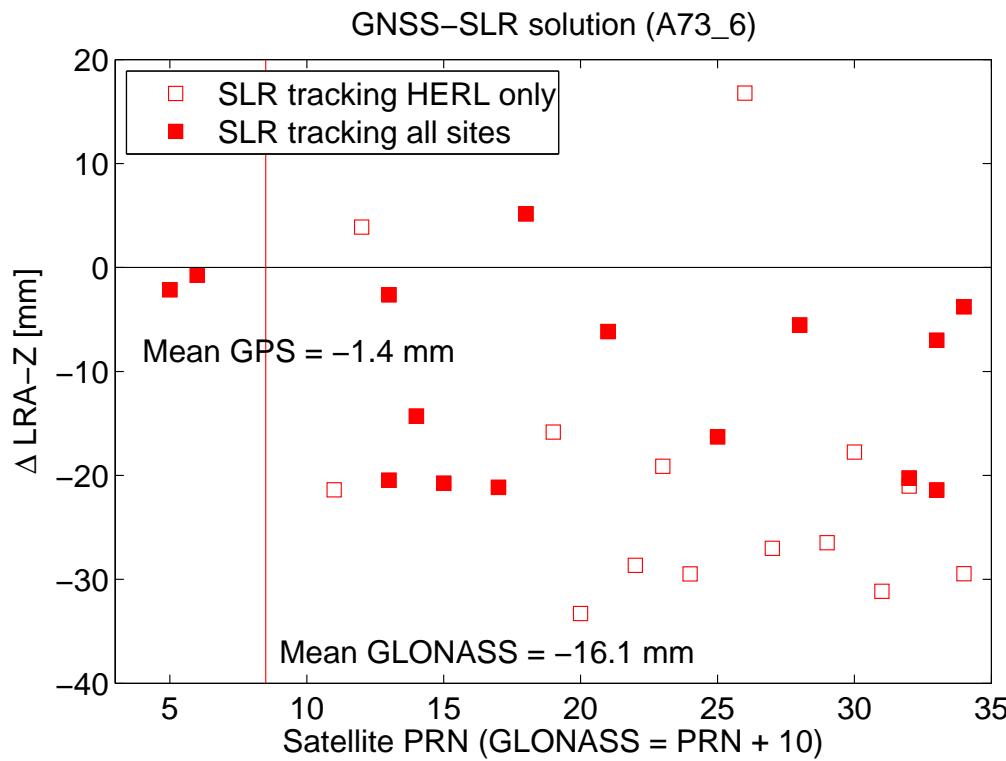
Combined GNSS–SLR analysis

	MW @GNSS	SLR @GNSS	SLR @Lageos
Radiation pressure ↔ Geocenter	Problems in RPR modelling	Problems in RPR modelling	RPR well modelled
GNSS satellite antenna phase center ↔ Scale	Problems in phase center modelling	independent	-
Range biases ↔ Scale	-	Decorrelated if different elevation angles	For a few sites only

SLR @GNSS:

- ⇒ **Geocenter** is affected as well ⇒ LAGEOS needed
- ⇒ **Scale** is transferred to GNSS ⇒ LAGEOS helps for decorrelation

Combined GNSS–SLR analysis: LRA

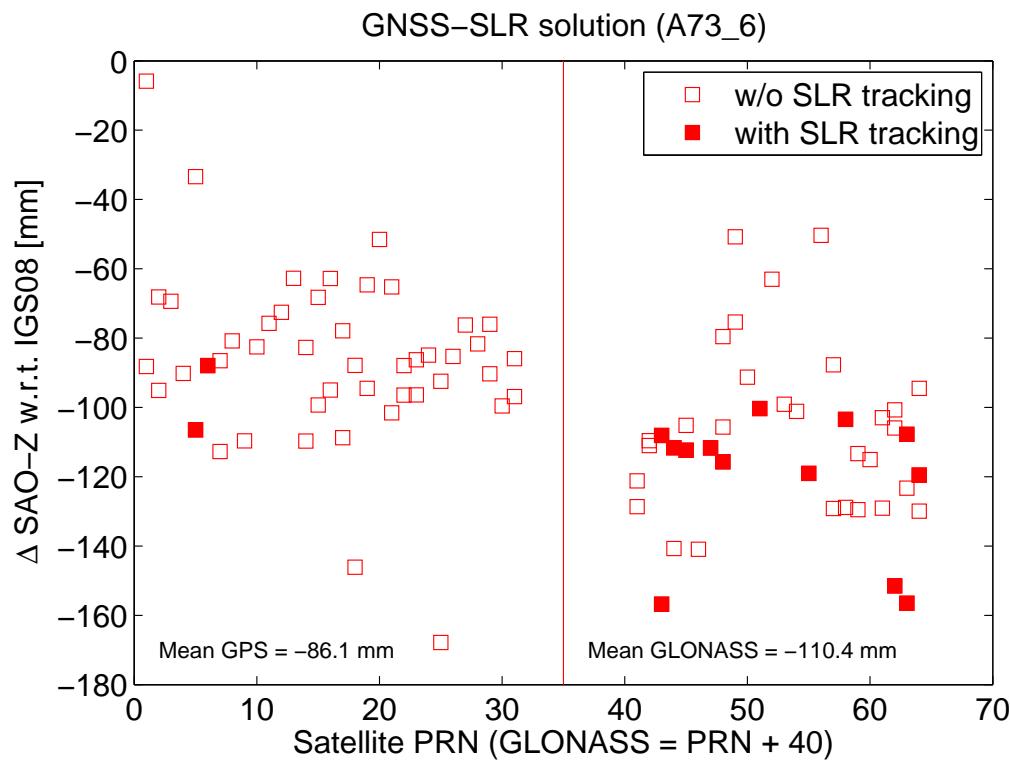


Corrections to ILRS values:

GPS: -1.4 mm

GLONASS: -16.1 mm

Combined GNSS-SLR analysis: SAO



$$\Delta \text{scale [ppb]} = -7.8 \times \Delta \text{SAO}_Z [\text{m}]$$

Corrections to IGS08 values:

GPS: -86.1 mm

GLONASS: -110.4 mm

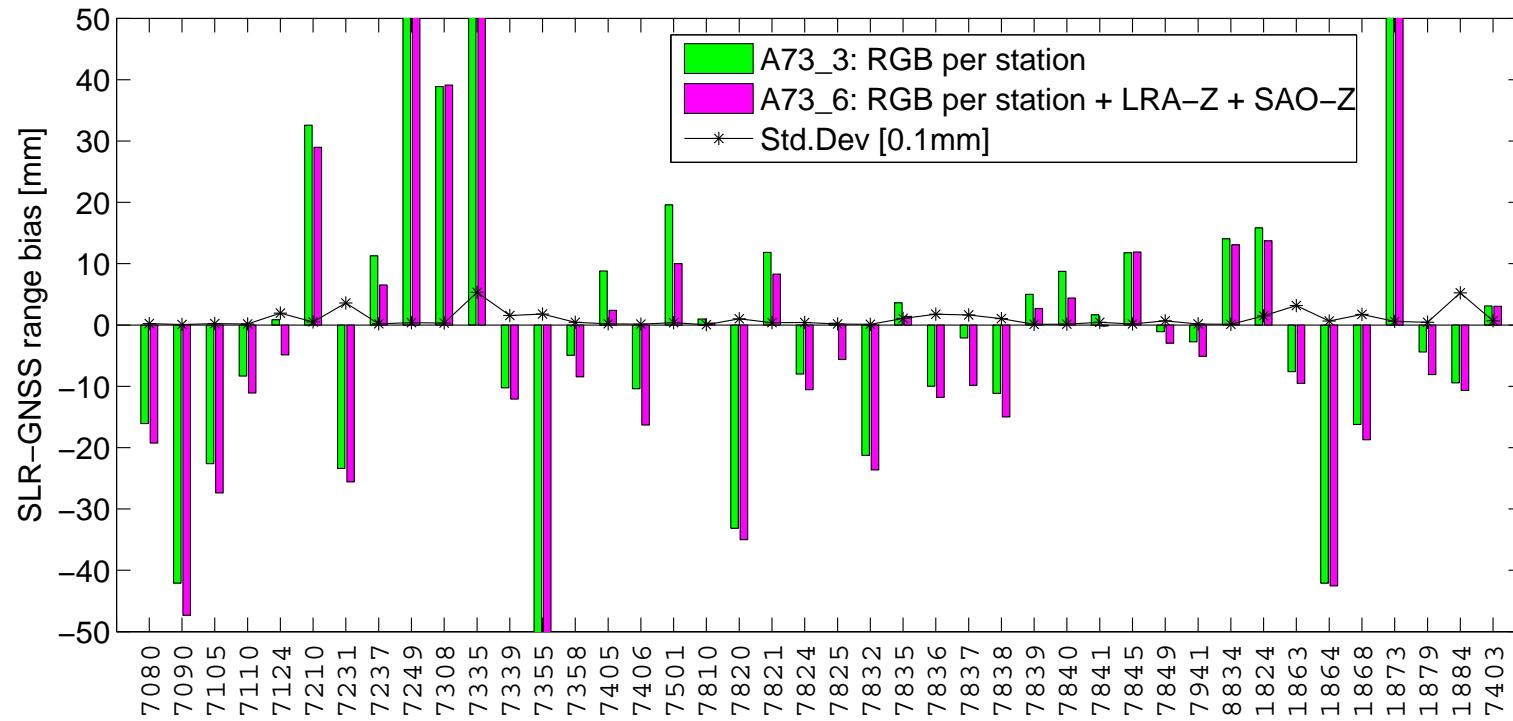
\Rightarrow 0.67 ppb

\Rightarrow 0.86 ppb

Combined GNSS–SLR analysis: Range biases

1 RGB per station (for all satellites) estimated:

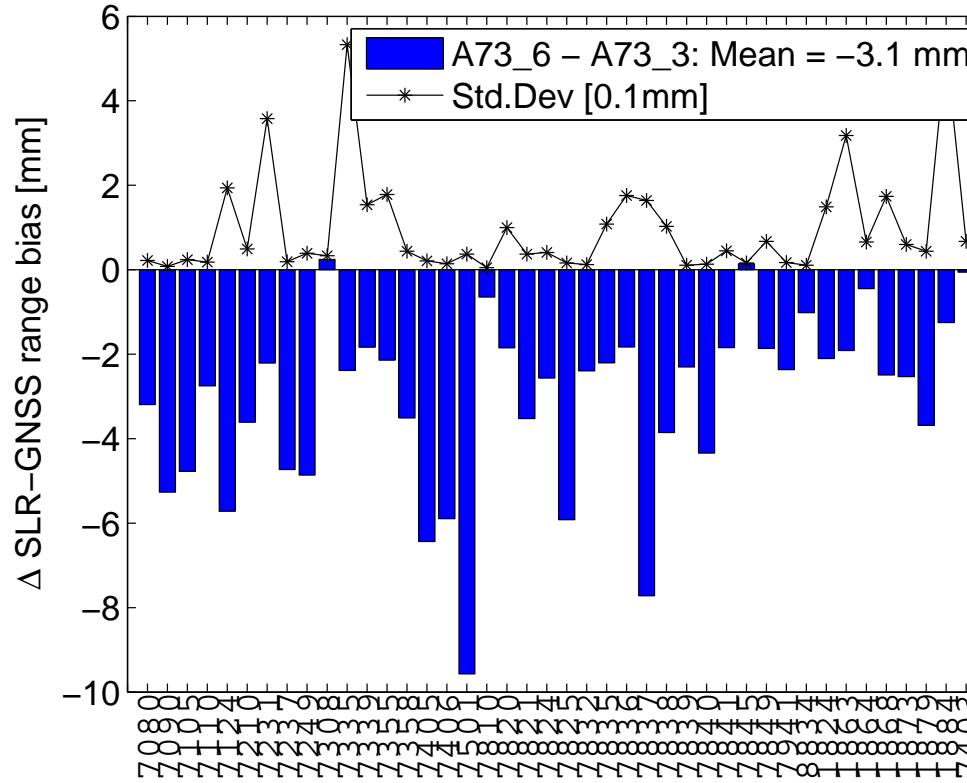
- Big differences between stations (+- few centimeters)
- Correlations with other parameters?



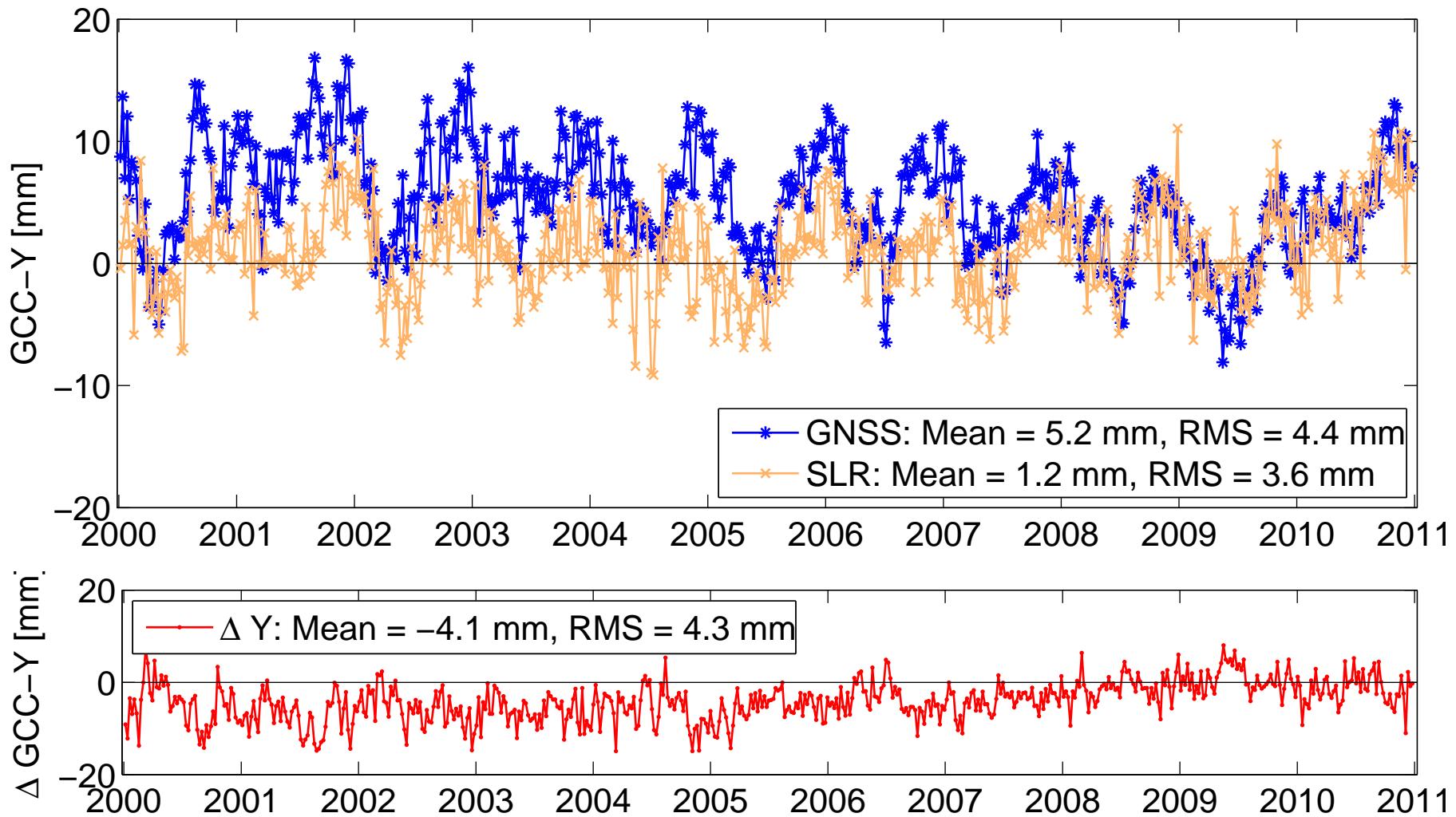
Combined GNSS–SLR analysis: Range biases

Correlations with other parameters?

- Additional estimation of SAO and LRA offset corrections causes differences in RGB estimates of **a few mm** only
- Not critical

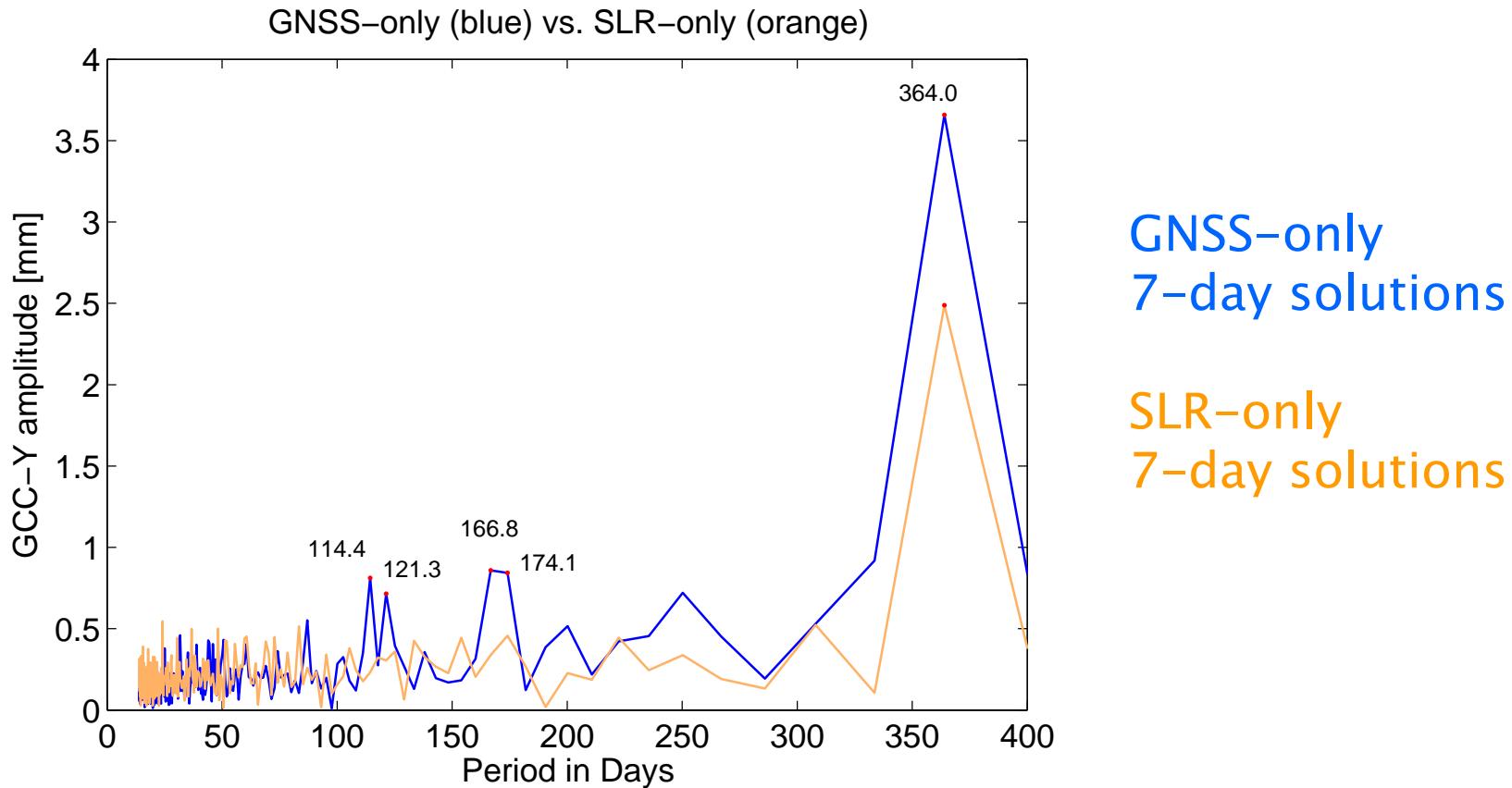


Geocenter: SLR-only and GNSS-only series



➤ Comparable series from GNSS and SLR (except for shift 4 mm)

Geocenter: SLR-only and GNSS-only series

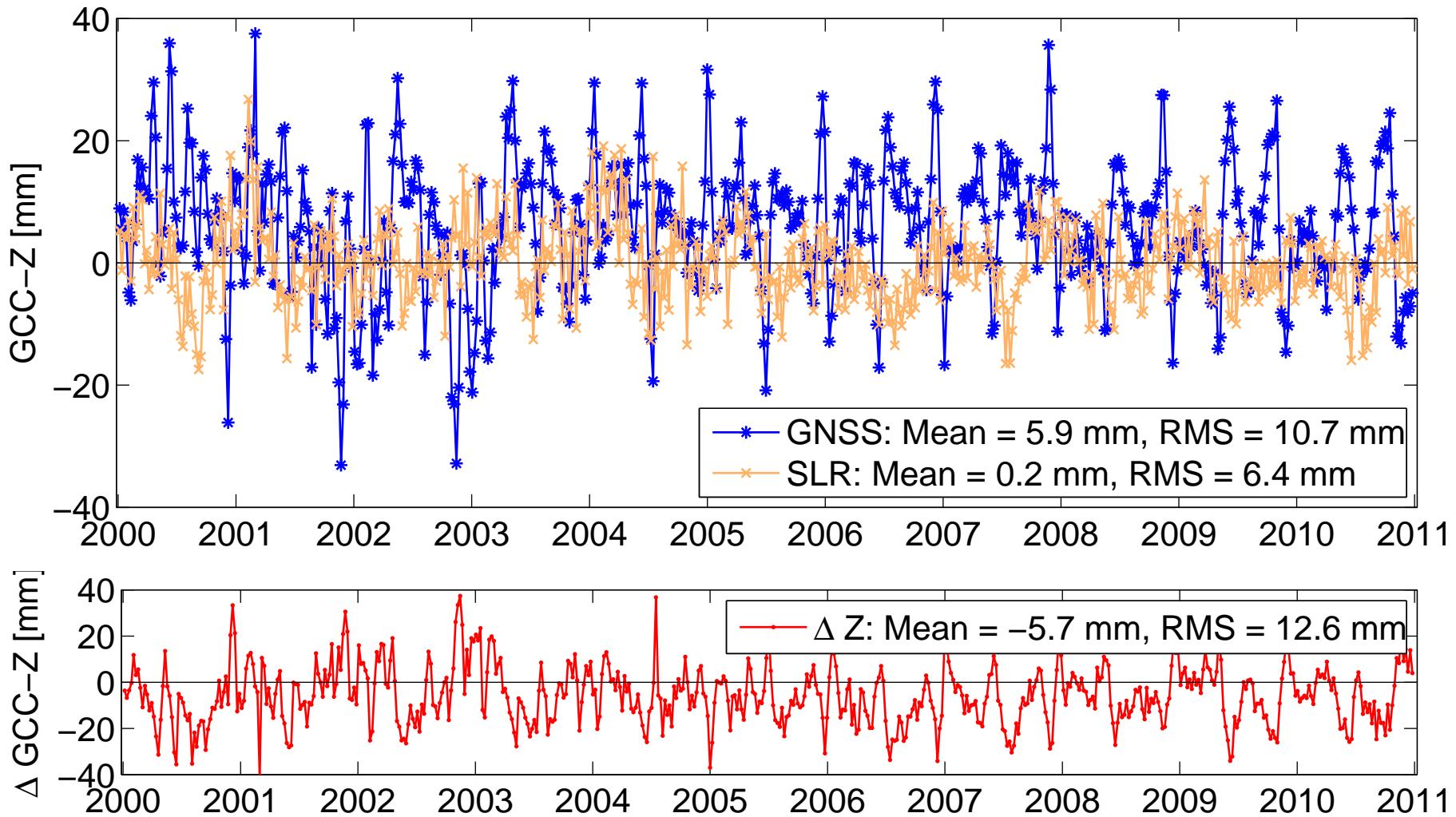


GNSS-only
7-day solutions

SLR-only
7-day solutions

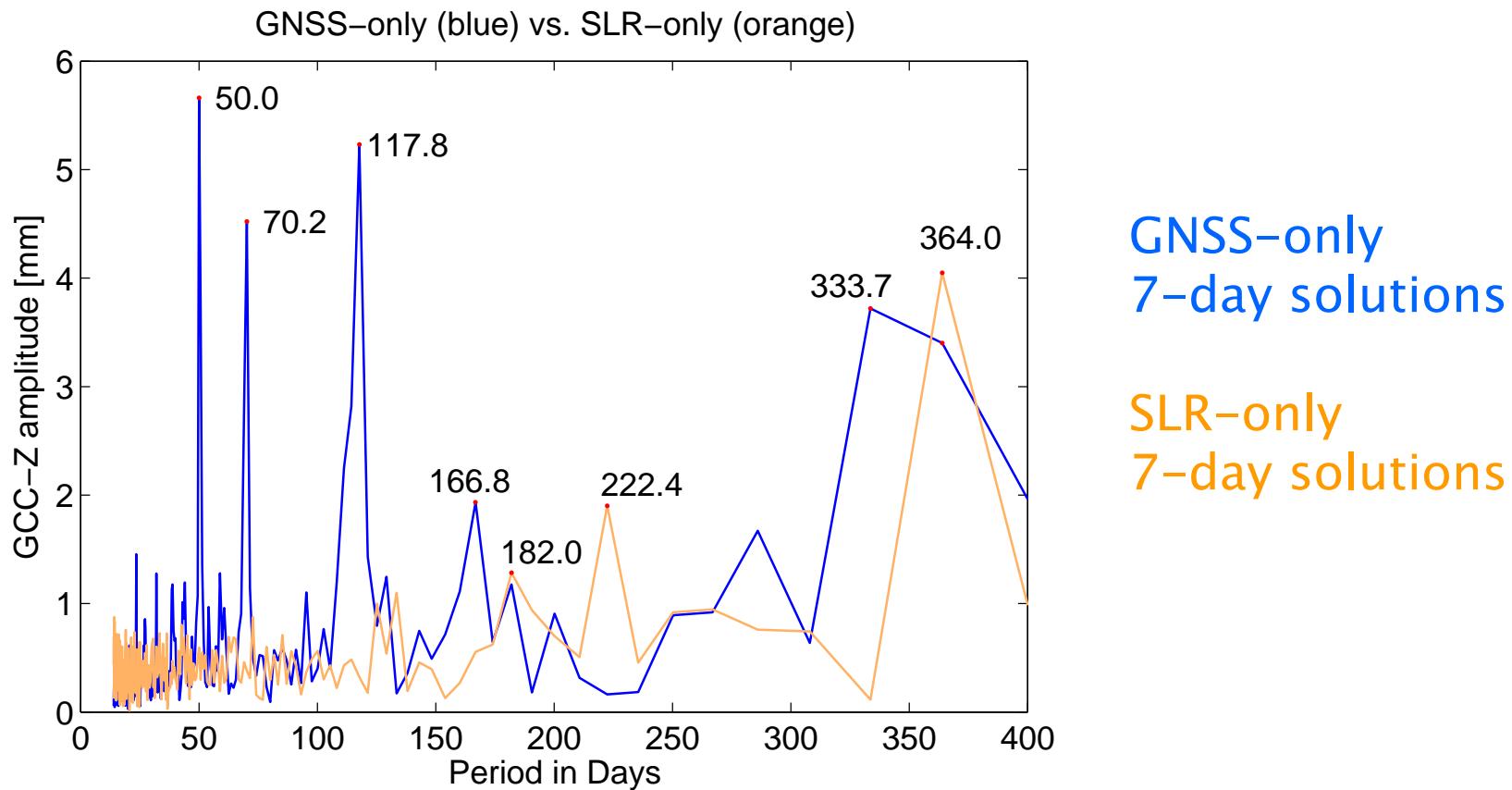
- Mainly annual signal visible
- Amplitudes are slightly different for GNSS and SLR series
- Few periods in GNSS series seem to be artifacts

Geocenter: SLR-only and GNSS-only series



➤ SLR shows clearly fewer variations than GNSS

Geocenter: SLR-only and GNSS-only series

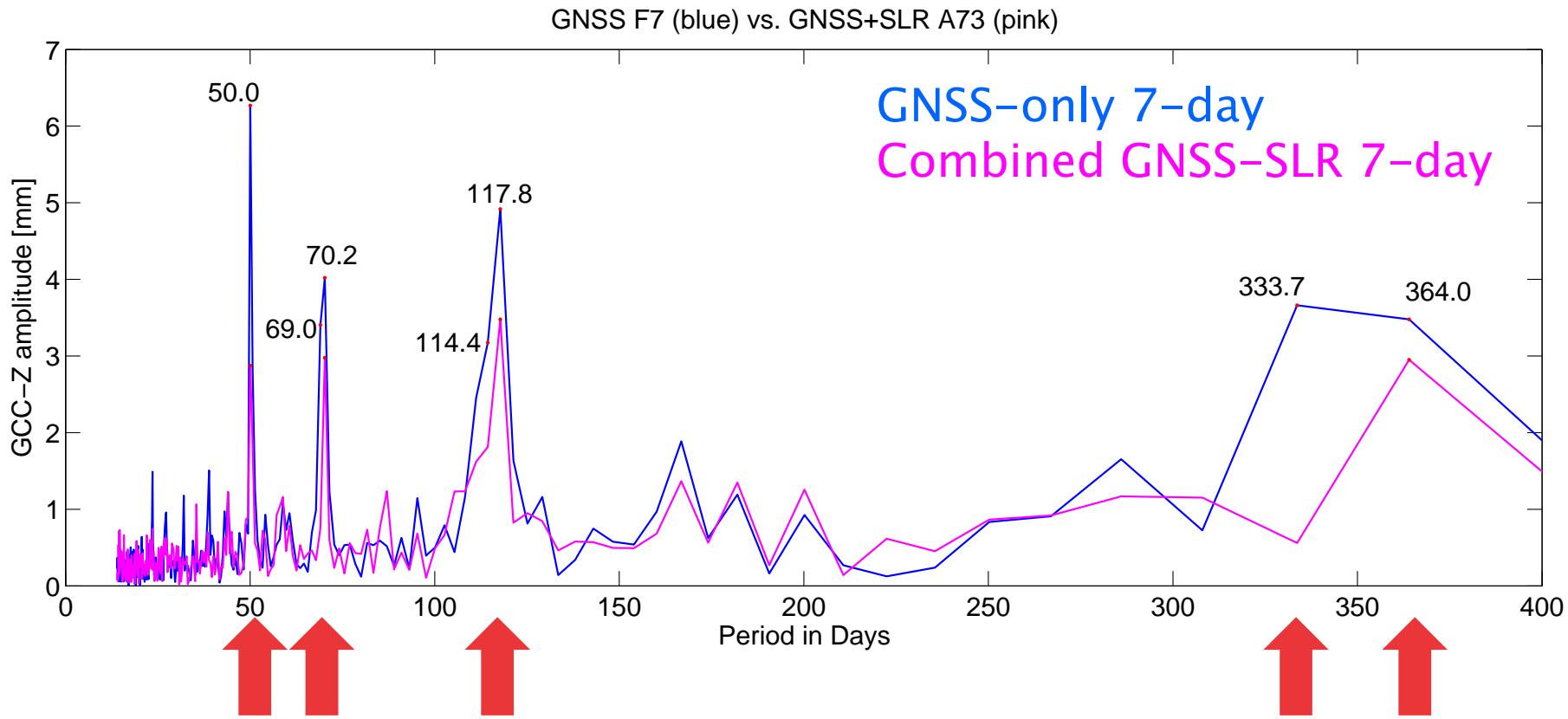


GNSS-only
7-day solutions

SLR-only
7-day solutions

- Draconitic year is clearly visible: $\text{GNSS} = 352 \text{ d}$, $\text{LAG-2} = 222 \text{ d}$
- Annual and draconitic signal are not distinguishable for GNSS
- Big amplitudes at harmonics of draconitic year for GNSS

Geocenter: Combined SLR–GNSS series



- Annual signal remains; draconitic GNSS signal vanishes
- Harmonics of draconitic GNSS year are reduced but not eliminated

Summary

- GNSS and SLR analysis is done at AIUB
- Identical software package for the analysis and the combination
 - ⇒ Combination at observation level
- SLR data to GNSS satellites included in the combination
 - ⇒ «Space Tie»
- Components of the «Space Tie» can be evaluated:
 - Microwave antenna offsets (SAO)
 - Laser reflector array offsets (LRA)
- All parameters benefit from the combination (e.g. geocenter coordinates)

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Thanks for your attention !

