

# Combination of GNSS and SLR using satellite co-location

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**Session 2:** Strengths, weaknesses, modelling standards and processing strategies  
of space geodetic techniques

# Overview

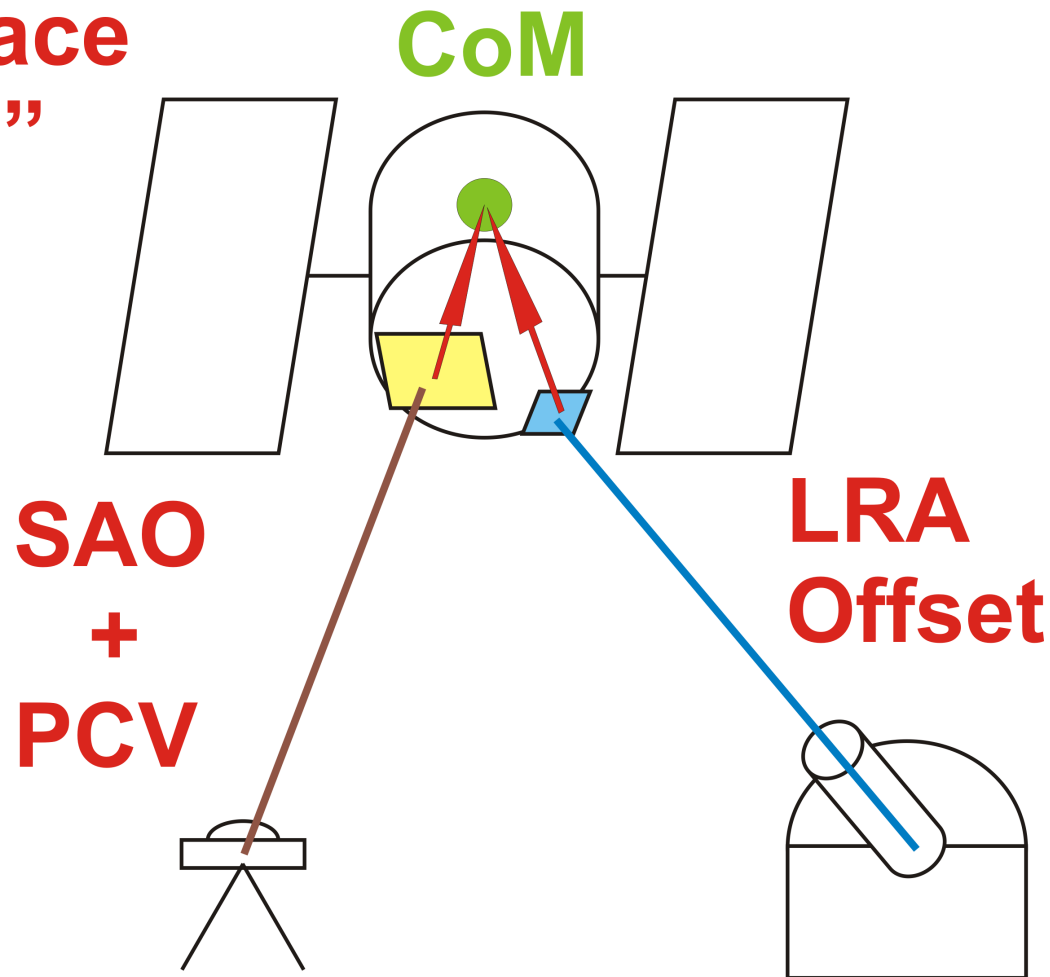
1. **Co-location** of GNSS and SLR at GNSS satellites
2. **Results** from combined GNSS-SLR analysis using satellite co-location:
  - Station coordinates / TRF
  - GNSS satellite antenna offsets
  - Biases between GNSS and SLR
3. **Conclusions** and **outlook**

# Co-location for GNSS and SLR

**Co-location at GNSS satellites** = Common orbit parameters from GNSS microwave and SLR range data

→ **Vectors** of GNSS and SLR reference points **w.r.t. satellite CoM** needed

**“Space Tie”**

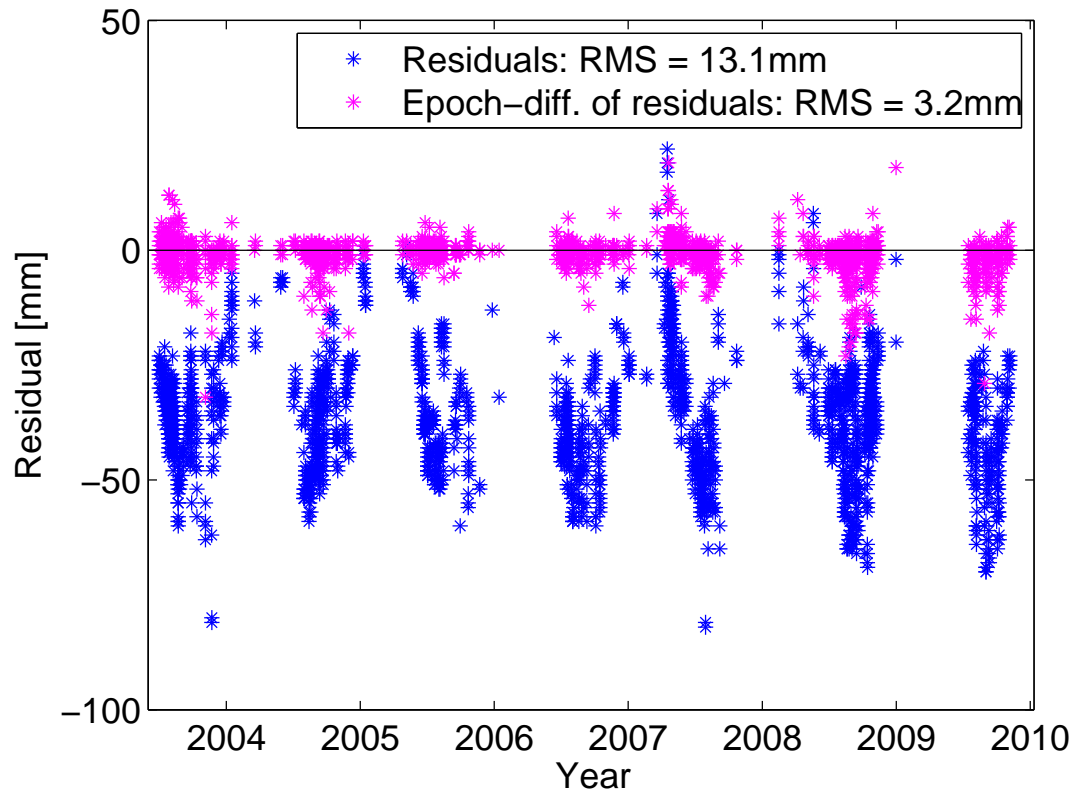


***Space Tie*** =

1. GNSS Satellite Antenna Offsets (**SAO**) w.r.t. CoM
2. GNSS Phase Center Variations (**PCV**)
3. Offsets for Laser Retroreflector Array (**LRA**) w.r.t. CoM

# SLR residuals to GNSS-only orbits

SLR residuals for station 7839 11001S002, satellite G06

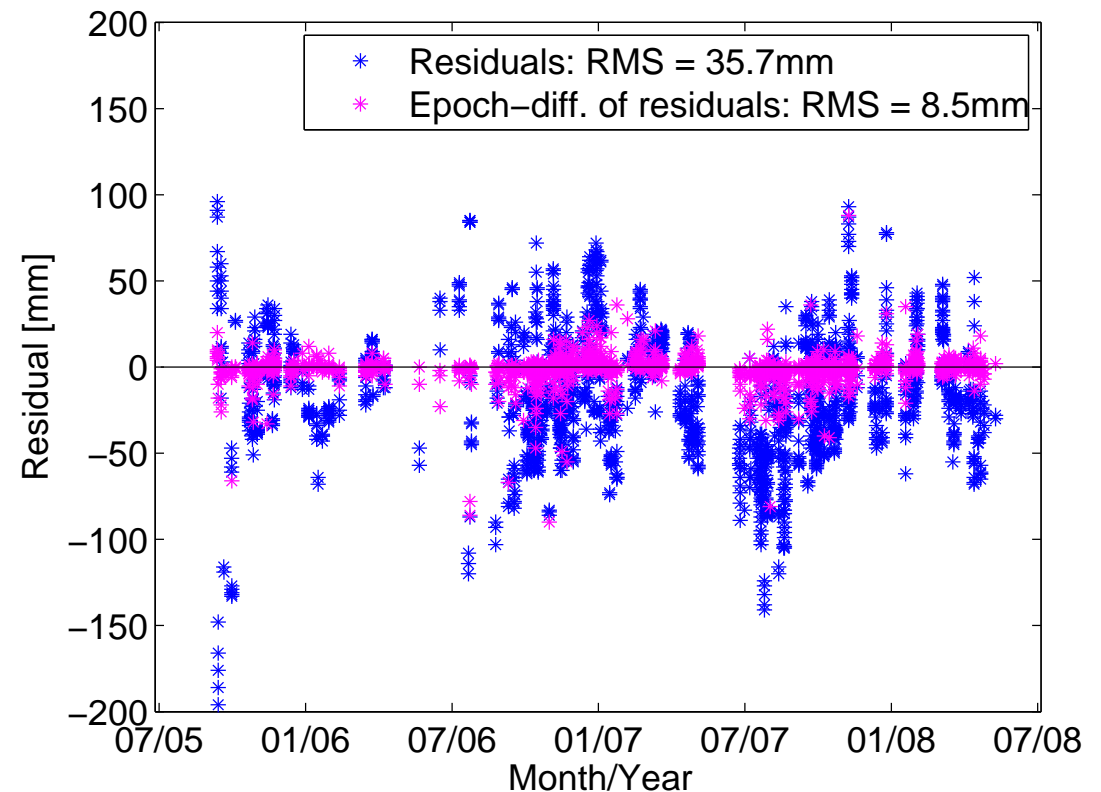


1) Biases in SLR range residuals  
(cm-level)

2) Epoch-differences of SLR range  
residuals have a much smaller RMS

⇒ systematic effects

SLR residuals for station 7839 11001S002, satellite R07



# Systematic effects between SLR and GNSS

## Possible reasons for systematic effects in SLR range residuals:

SLR station coordinates (fixed to SLRF2005)

TRF (scale, geocenter)

Offset for GNSS satellite antenna (SAO from igs05.atx)

Offset for laser reflector array (LRA from ILRS web site)

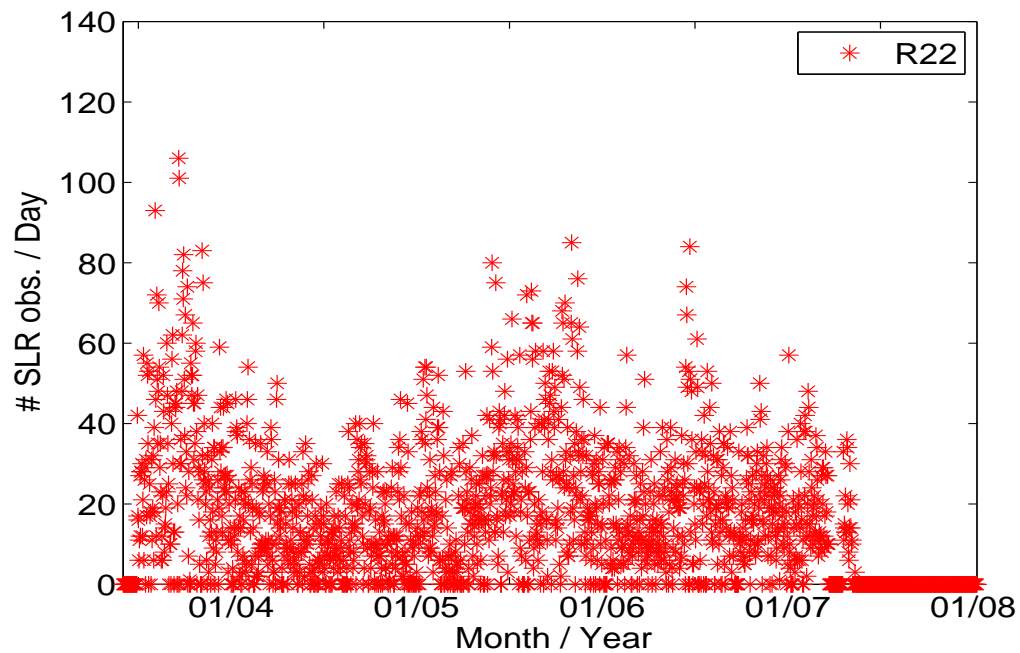
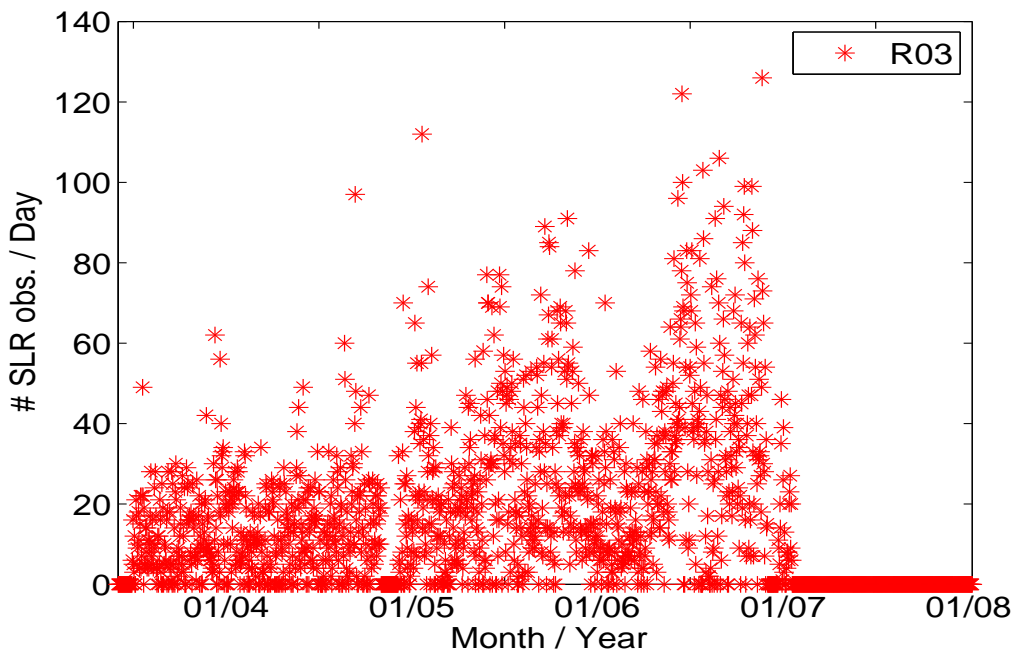
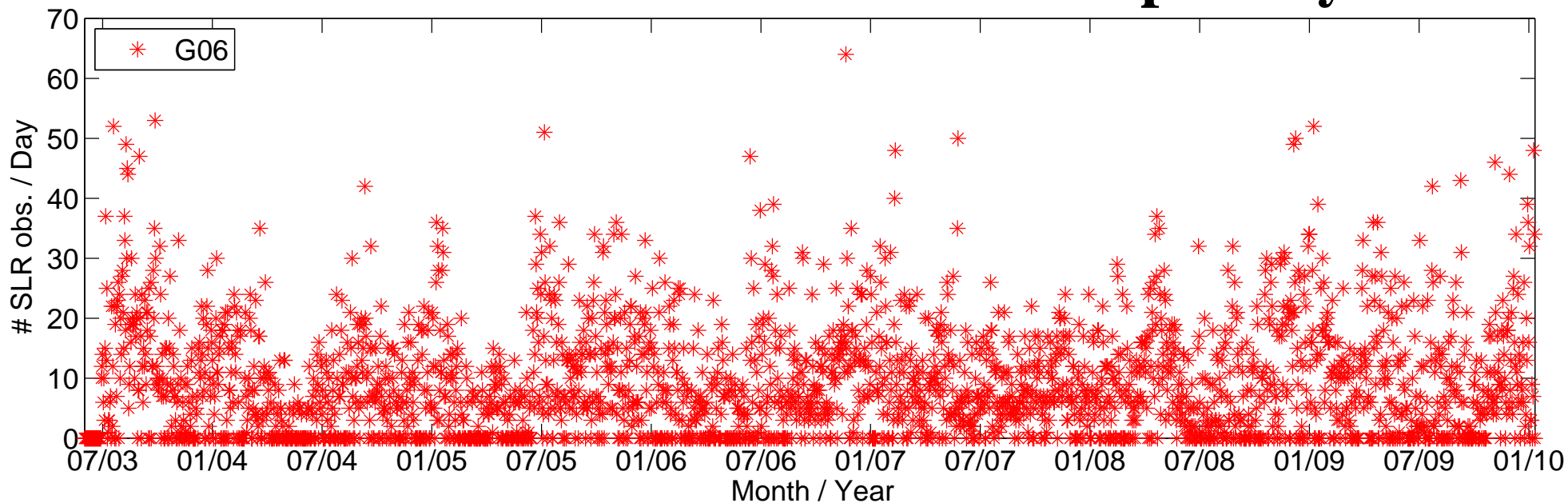
SLR range biases (unknown for GNSS satellites)

GNSS orbit modelling (solar radiation pressure)

## ⇒ Must be handled in combined solution:

- use known / better values
- **Estimation**

# Number of SLR observations per day



# Combined analysis of GNSS and SLR

SLR station coordinates

→ **estimate + inclusion of LAGEOS**

TRF scale (and geocenter)

→ **use from SLR**

Offset for GNSS satellite antenna (SAO from igs05.atx)

→ **estimate**

Offset for laser reflector array (LRA from ILRS web site)

→ **estimate**

SLR range biases (unknown for GNSS satellites)

→ **estimate + inclusion of LAGEOS**

GNSS has rank-deficiency w.r.t. scale if SAO are estimated

Estimation of 1 bias parameter per station / per GNSS satellite

⇒ **GNSS-microwave + SLR@GNSS + SLR@LAGEOS for 2006-2009**

# SLR station coordinates

## SLR station network

- Not included in the datum definition (no-net-rotation, no-net-translation)
- No local ties applied
- Only appended via the „space ties“ (common orbit parameters)

## Validation of SLR station coordinates: Helmert transformation

		SLRF2005	Lageos-only	
<b>RMS</b>	<b>Comb: SLR@GNSS</b>	<b>54.40</b>	54.22	[mm]
	<b>Comb: + Lageos</b>	<b>6.70</b>	2.95	[mm]
	<b>Lageos-only</b>	<b>7.49</b>		[mm]

- Agreement is at the **cm-level** if only SLR@GNSS is used
- **Inclusion of Lageos** improves the coordinate estimates
- Connection by using space ties only is feasible



# SLR station coordinates

## SLR station network:

- Not included in the datum definition (no-net-rotation, no-net-translation)
- No local ties applied
- Only appended via the „space ties“ (common orbit parameters)

## Validation of SLR station coordinates: Helmert transformation

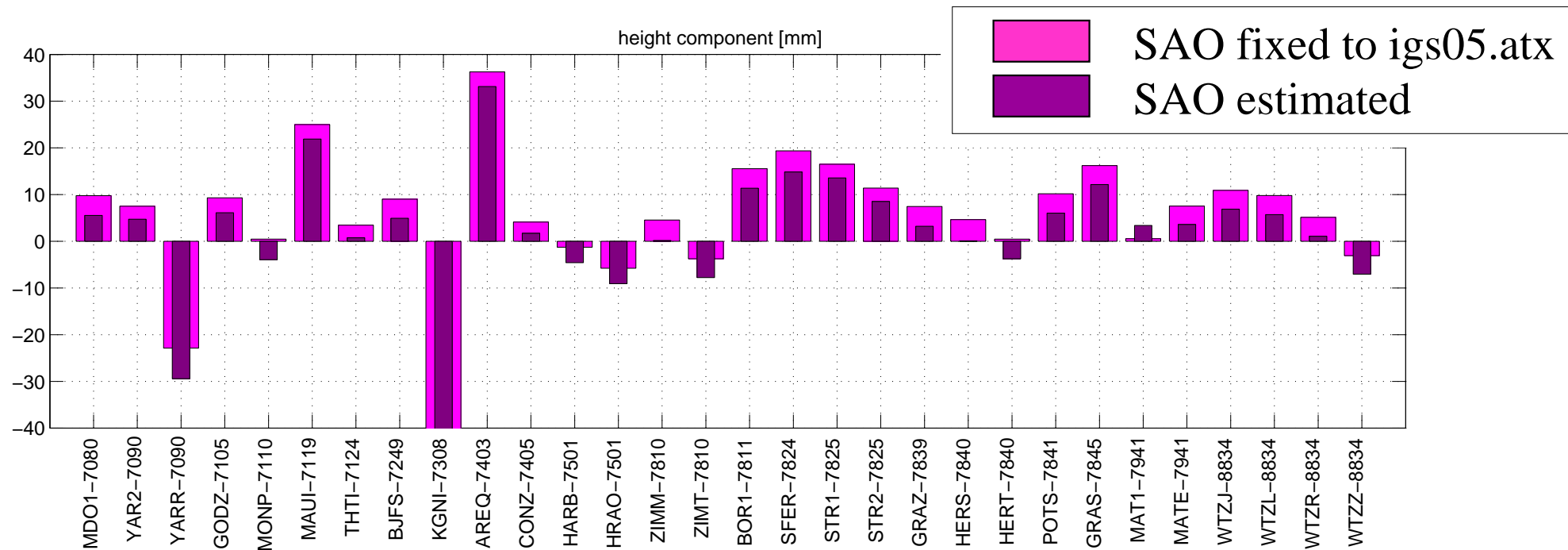
		SLRF2005	Lageos-only	
<b>Scale</b>	<b>Comb: SLR@GNSS</b>	<b>1.06 +- 2.76</b>	2.34 +- 2.75	[ppb]
	<b>Comb: + Lageos</b>	<b>1.02 +- 0.34</b>	0.25 +- 0.15	[ppb]
	<b>Lageos-only</b>	<b>1.28 +- 0.38</b>		[ppb]

→ Scale of SLR is defined well

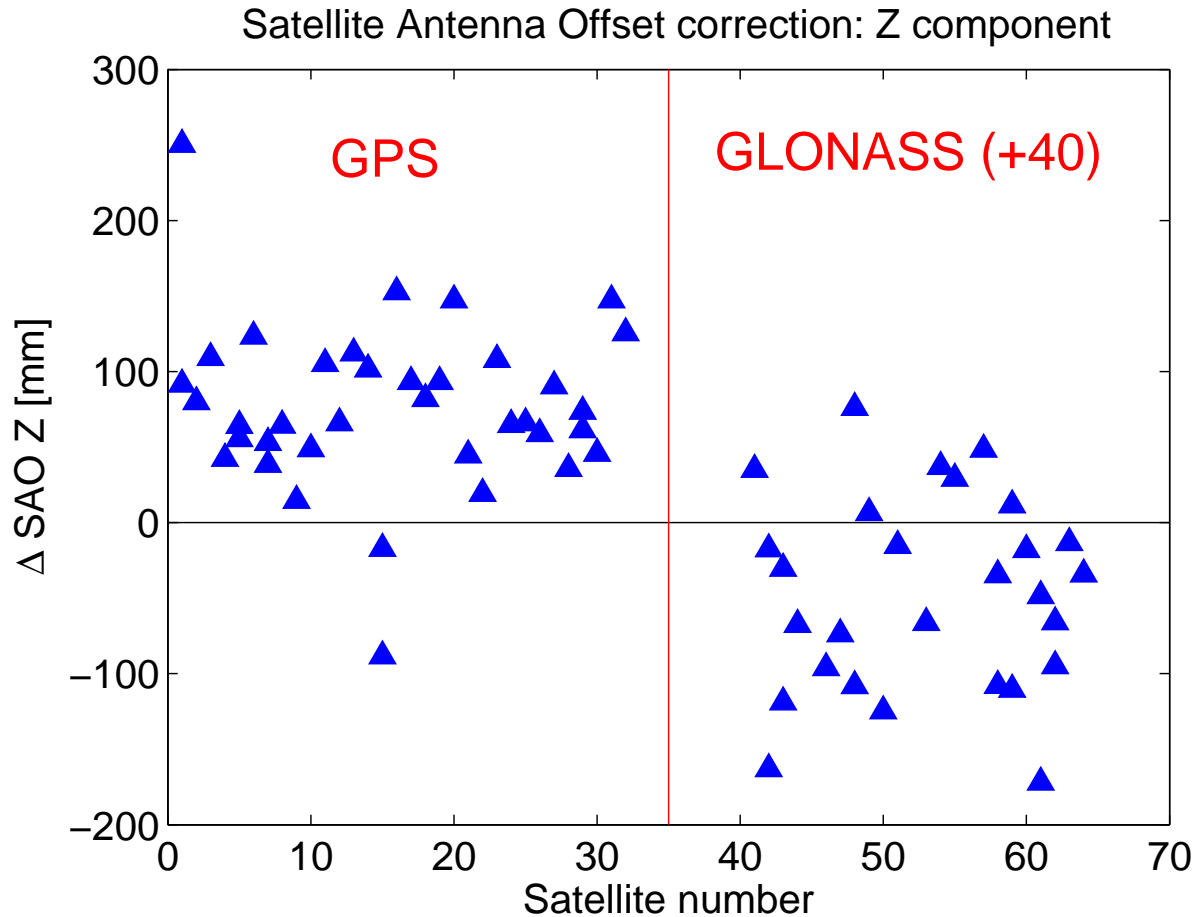
→ **Inclusion of Lageos** improves the coordinate estimates

# Comparison with local ties

1. Estimated SLR and GNSS station coordinates  $\Rightarrow \Delta\text{CRD\_estimate}$
  2. Local tie between SLR and GNSS reference points:  $\Delta\text{CRD\_LT}$
- $\Rightarrow \Delta\text{CRD\_estimate} - \Delta\text{CRD\_LT}$ : Height component
- $\Rightarrow$  Agreement between GNSS and SLR sites better if GNSS SAO are estimated (i.e. using the SLR scale)



# SLR-GNSS biases and GNSS SAO



Mean  $\Delta Z$  for GPS:  
**76.4 mm**

Mean  $\Delta Z$  for GLONASS:  
**-47.7 mm**

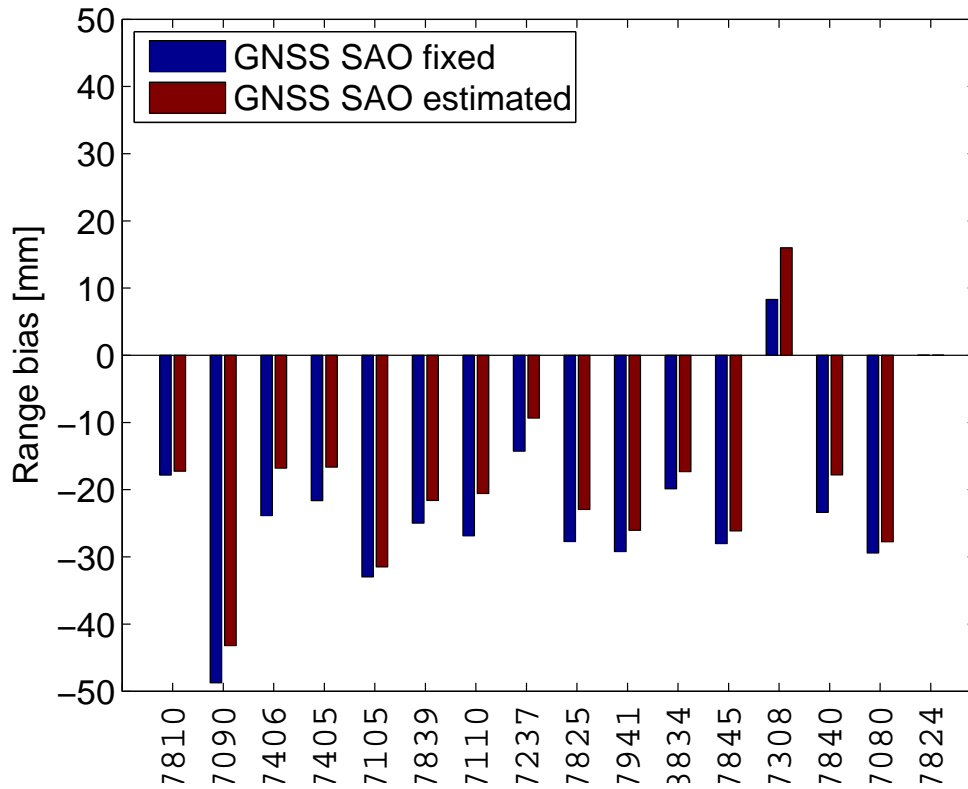
$\Delta$ Scale for GNSS network:  
**0.59 ppb**

$\Delta$ Scale for SLR network:  
**0.00 ppb**

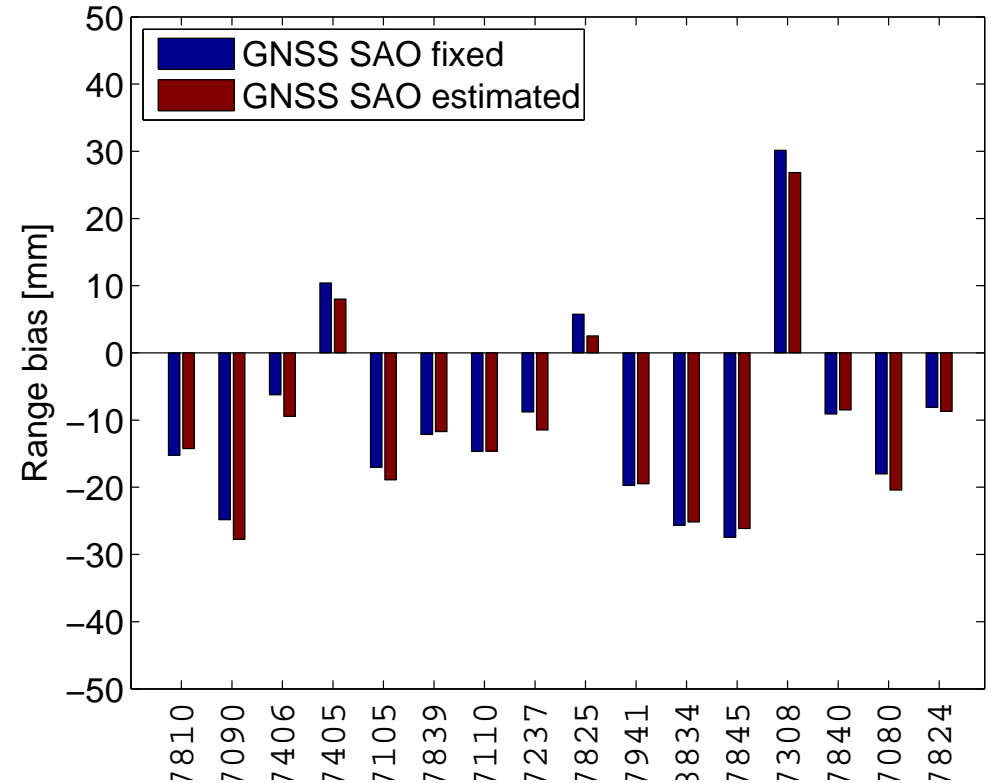
No general shift of SAO estimates  
 $\Rightarrow$  Scale of SLR is transferred properly to GNSS

# SLR-GNSS biases and GNSS SAO

SLR range biases for satellite G06



SLR range biases for satellite R15



Impact of GNSS-SAO estimation  
on SLR-GNSS „range“ biases:  
< 5 mm

## Conclusions and outlook

- Inclusion of SLR@GNSS works properly
- *LAGEOS* data should be included in order to derive stable solutions
- *Scale from SLR* can be transferred to GNSS very well
  - allows the estimation of GNSS satellite antenna offsets
- GNSS SAOs from *igs05.atx* do not fit to the *SLR scale* (0.59 ppb)
- Connection via „*space ties*“ is possible (without local ties)  
***BUT:***  
*Accurate ties* (in space and on sites) required for combination
- *Separation* of SLR range biases and errors in *LRA offsets* is still needed