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# **SLR-Beobachtungen zu LAGEOS und GNSS-Satelliten und die gemeinsame Auswertung mit GNSS-Beobachtungen**

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# Gliederung

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1. Prozessierung der **LAGEOS**-Daten am AIUB
2. Allgemeine Aspekte der **Kombination von GNSS und SLR**
  - Stationen als Kolokation
  - Satelliten als Kolokation
3. **SLR-Tracking der GNSS-Satelliten** (GPS und GLONASS)
4. **Resultate** der kombinierten GNSS-SLR-Auswertung
  - Stationskoordinaten / TRF
  - GNSS satellite antenna offsets
  - Biases zwischen GNSS und SLR
5. **Zusammenfassung** und **Ausblick**

# Prozessierung von LAGEOS am AIUB

*Bernese GPS Software (BSW)* wurde erweitert:

- Orbit-Modellierung für Kugelsatelliten
- Handling von SLR-Beobachtungen

Zusammenarbeit mit *Bundesamt für Kartographie und Geodäsie (BKG)*:

- *ILRS Analysis Center*
- BKG-Beiträge basierend auf *BSW* seit **Juli 2010**

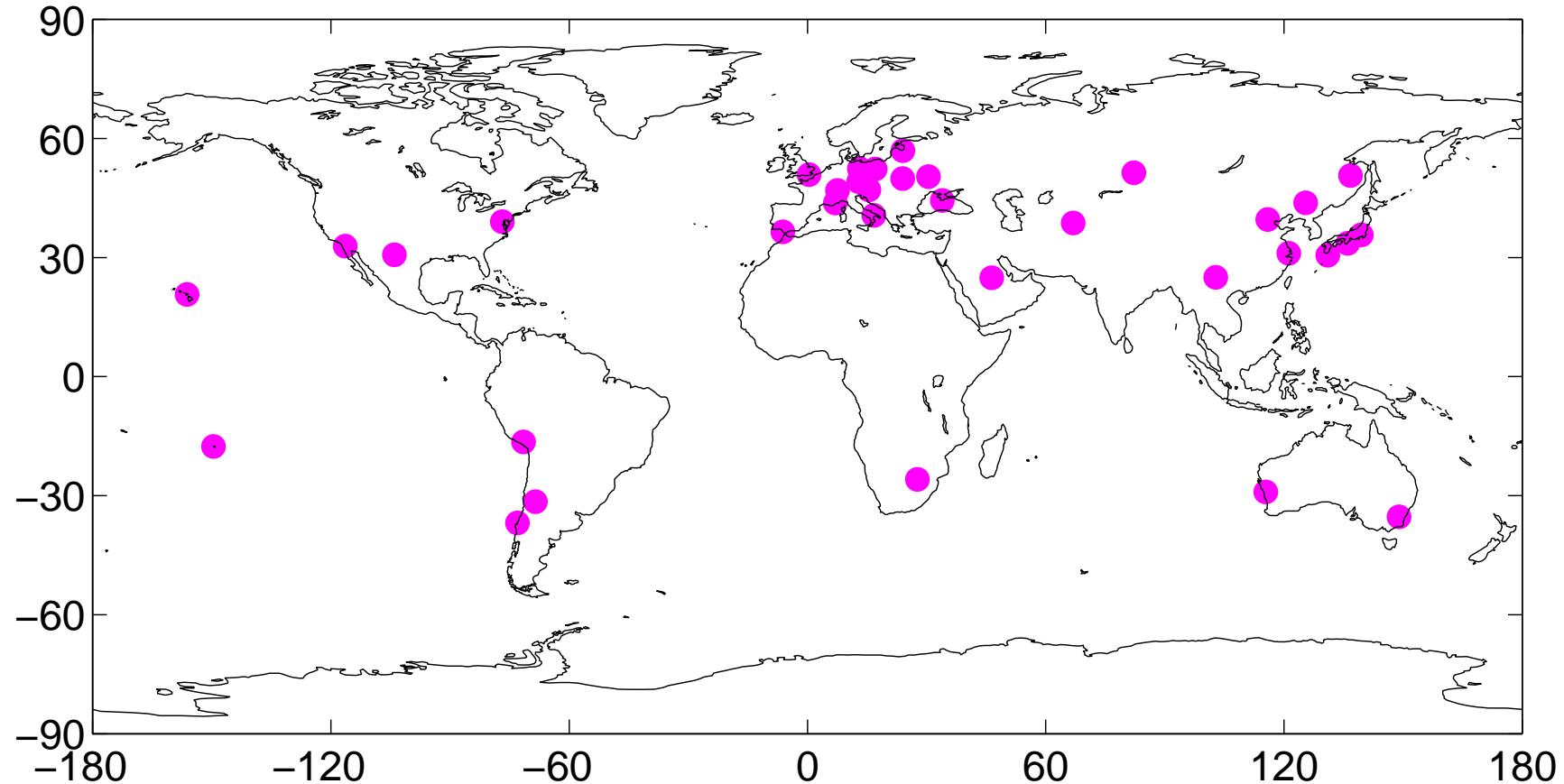
Analyse der LAGEOS-Daten am *AIUB*:

- **2 Satelliten: LAGEOS-1 / -2**
- **Wochenlösungen für 2006 – 2010**



# SLR tracking of LAGEOS

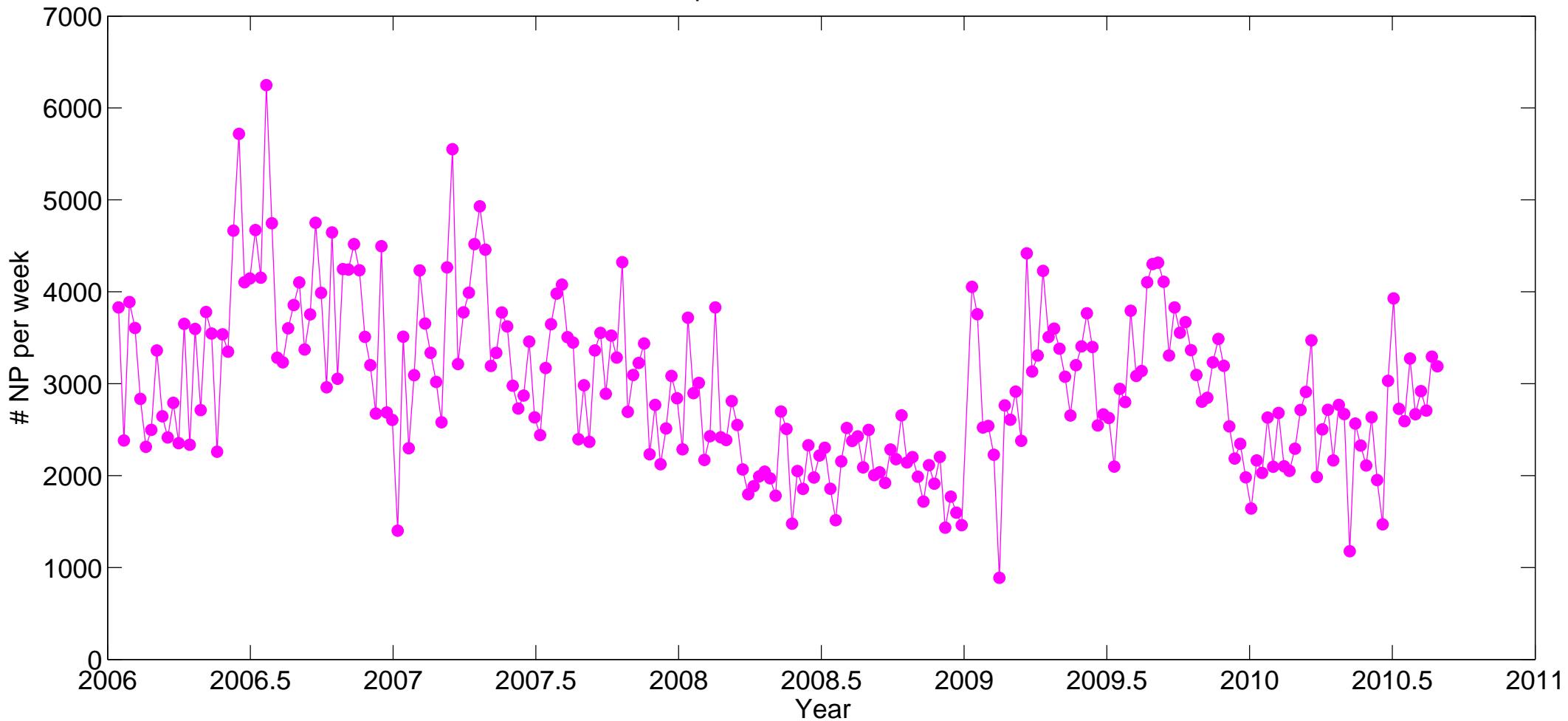
SLR network for 2007 – 2009 (Lageos tracking)



- Geographical distribution is not ideal!
- **Total** for 2006 – 2009: **35 stations**; 11 stations for datum definition
- Number of stations **per week**: **12 – 26** (datum definition: 7 – 11)

# SLR tracking of LAGEOS

Number of NP per week: LAGEOS-1 + LAGEOS-2

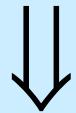


Total number of observations (normal points) per week for both satellites: **~ 3000**

# Weekly LAGEOS solutions

*Estimated parameters for weekly ILRS solution:*

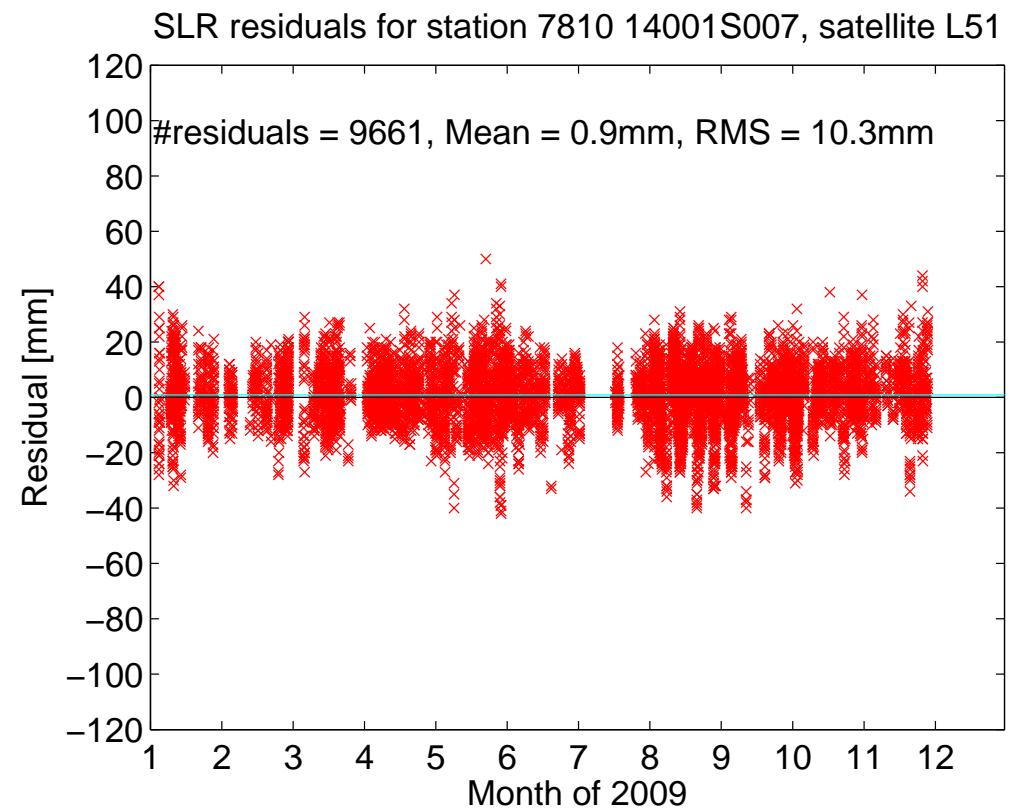
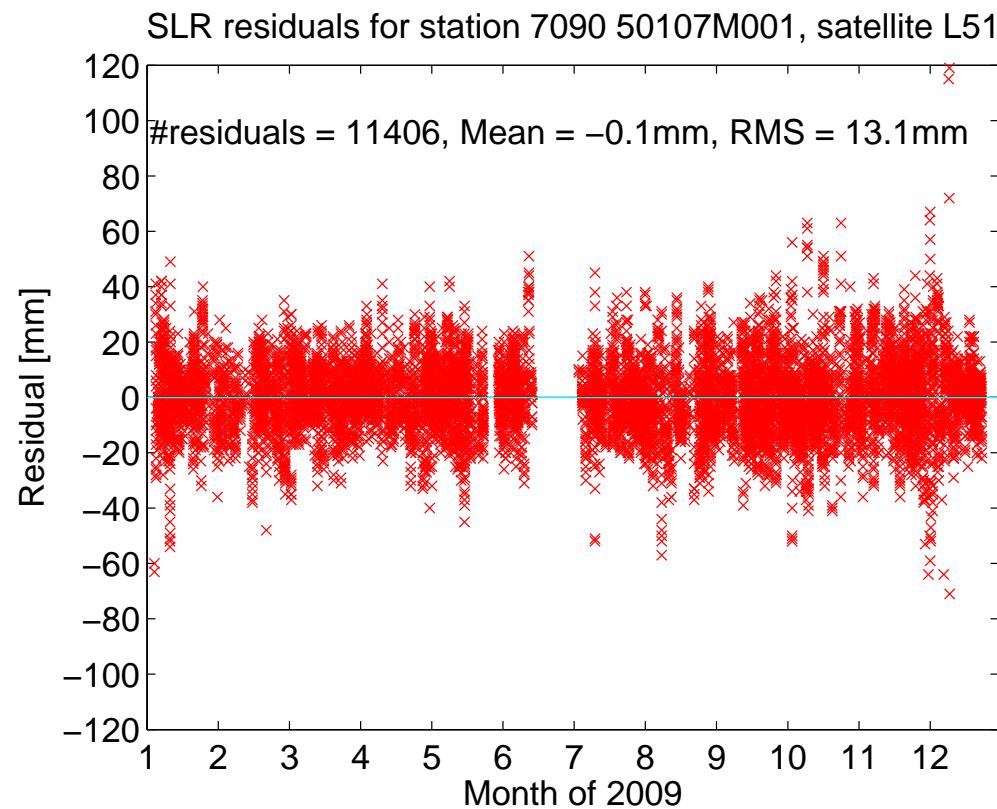
- Station coordinates
- Satellite orbits: 1 arc per week
  - 6 osculating elements
  - Dynamic orbit parameters:
    - Constant acceleration in along-track
    - Once-per-rev in along-track
    - Once-per-rev in cross-track
- Earth rotation:
  - Polar motion (constant per day)
  - Length of Day (LOD)
- Range biases for selected sites (1 – 3 stations per week)



~ **120 – 140**  
parameters  
per week

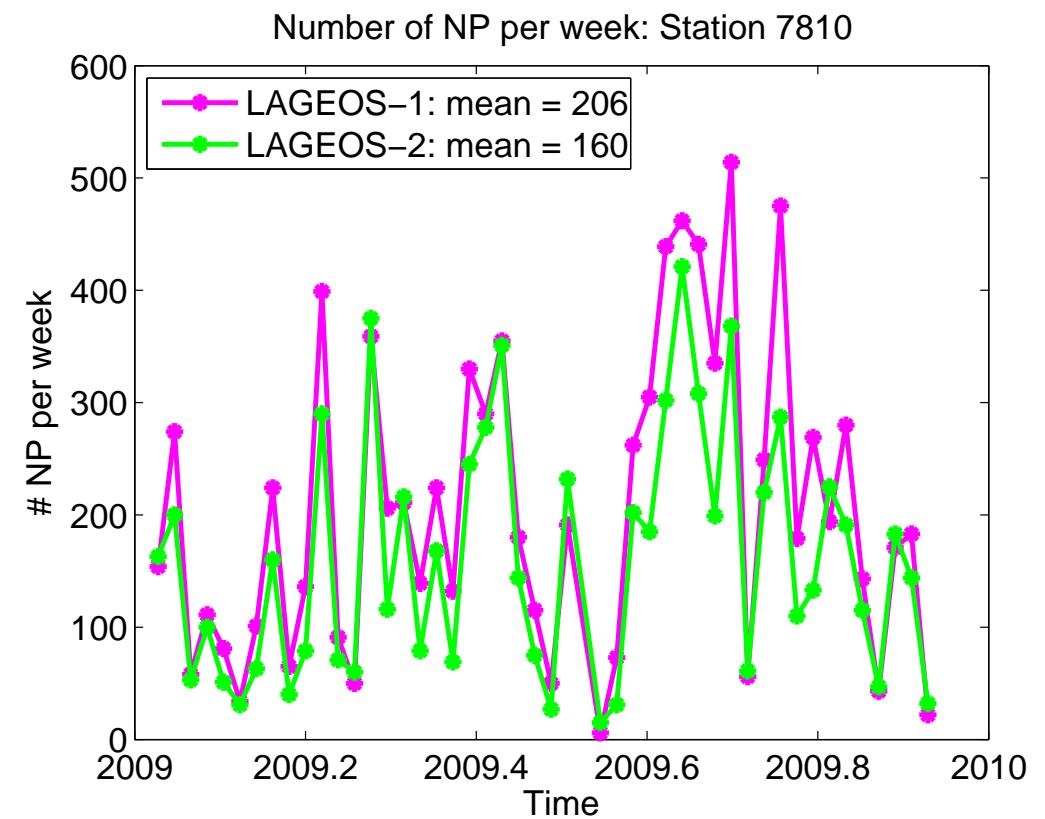
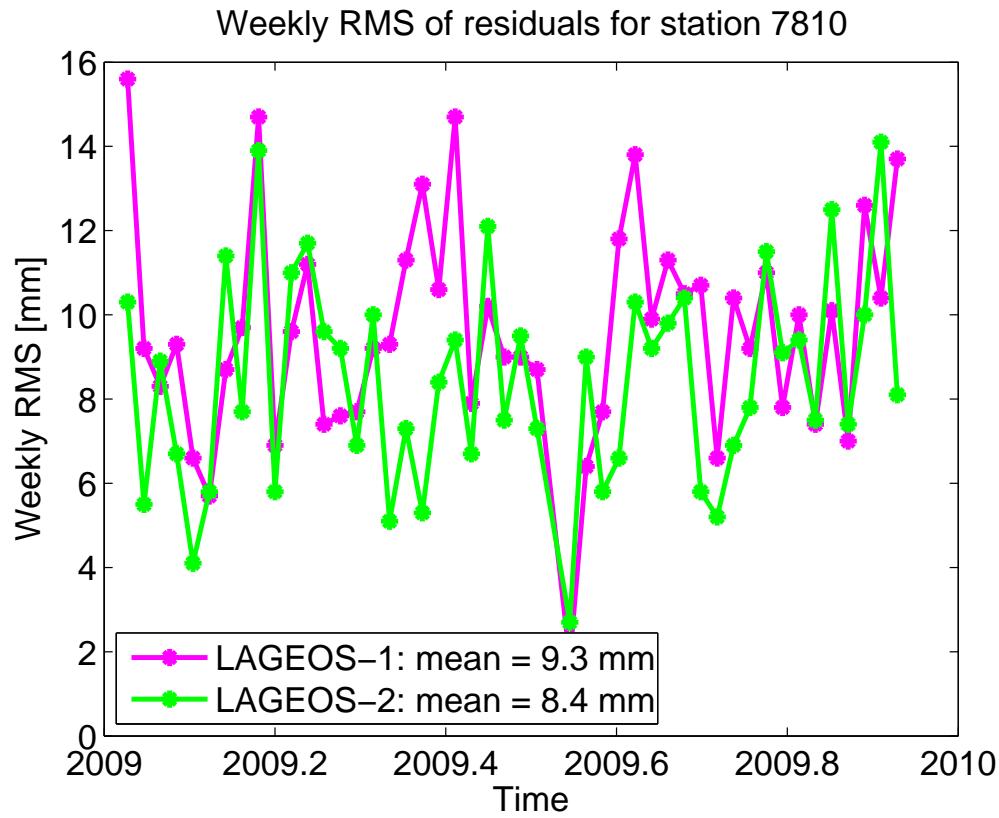
# Weekly LAGEOS solutions

**Residuals** for LAGEOS-1 after least squares adjustment:  
→ Yarragadee  
→ Zimmerwald



# Weekly LAGEOS solutions

Weekly RMS after least squares adjustment for Zimmerwald

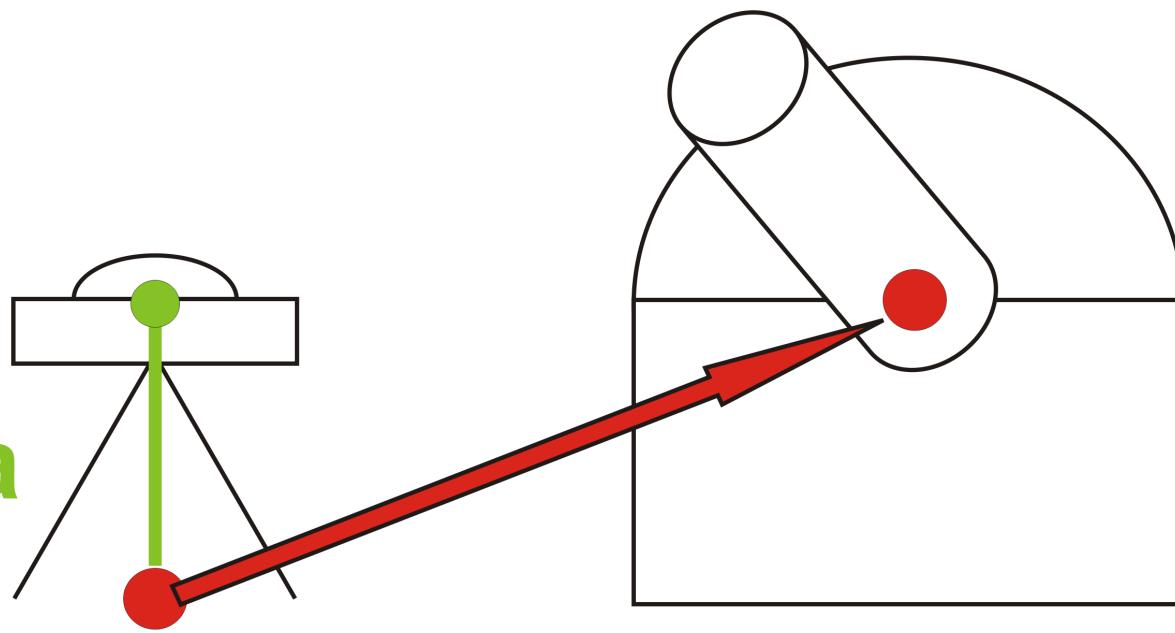


# Co-locations for GNSS and SLR

**Co-location at stations (e.g., for actual ITRF computation):**

- Application of known **local tie** values
- GNSS observations of ground network; SLR observations to Lageos etc.
  
- Independent of **satellite** tracked
- **Local ties** from terrestrial measurements

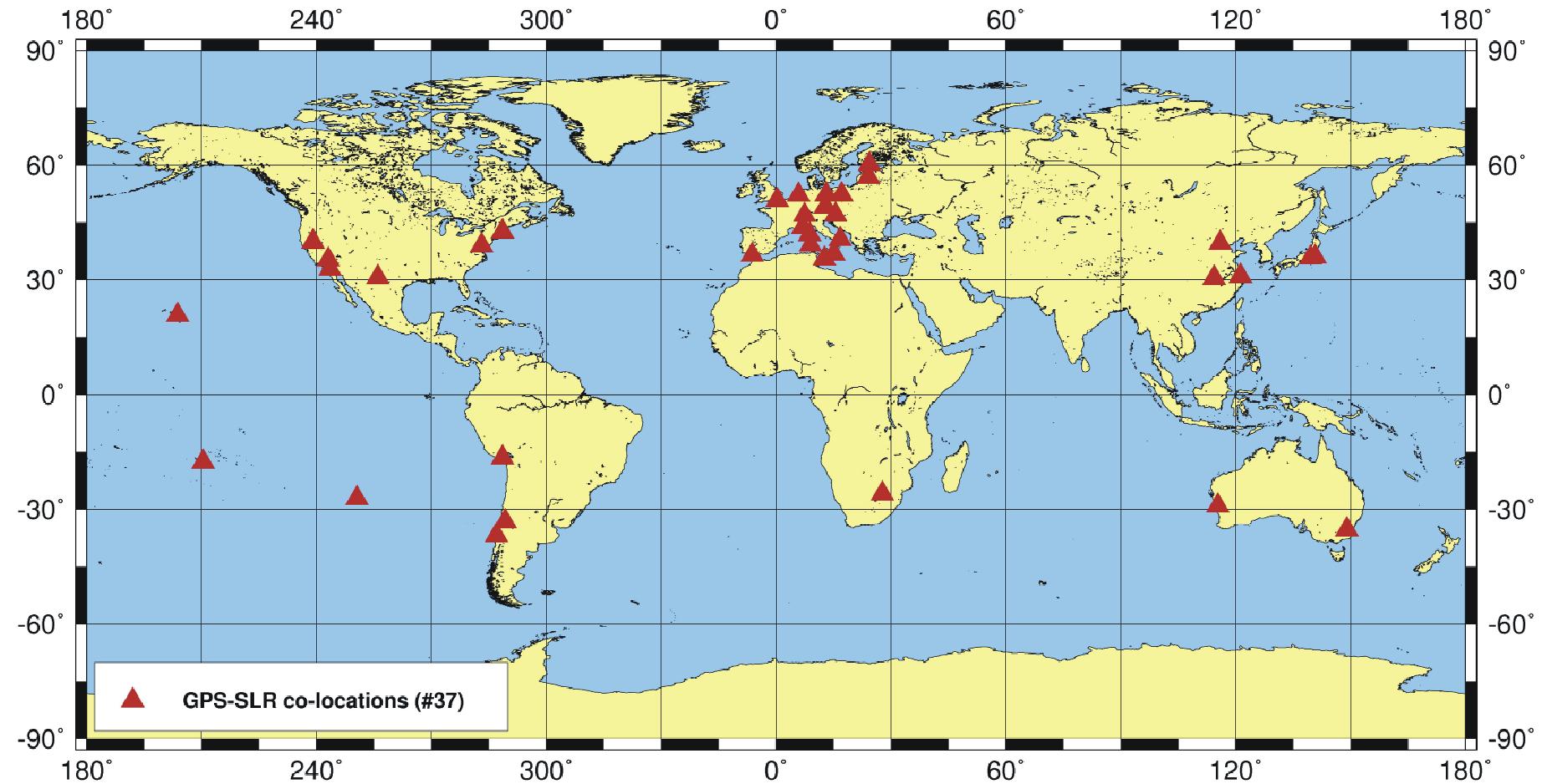
**Phase  
Center**  
+  
**Antenna  
Height**



**Local Tie**

# Co-locations for GNSS and SLR

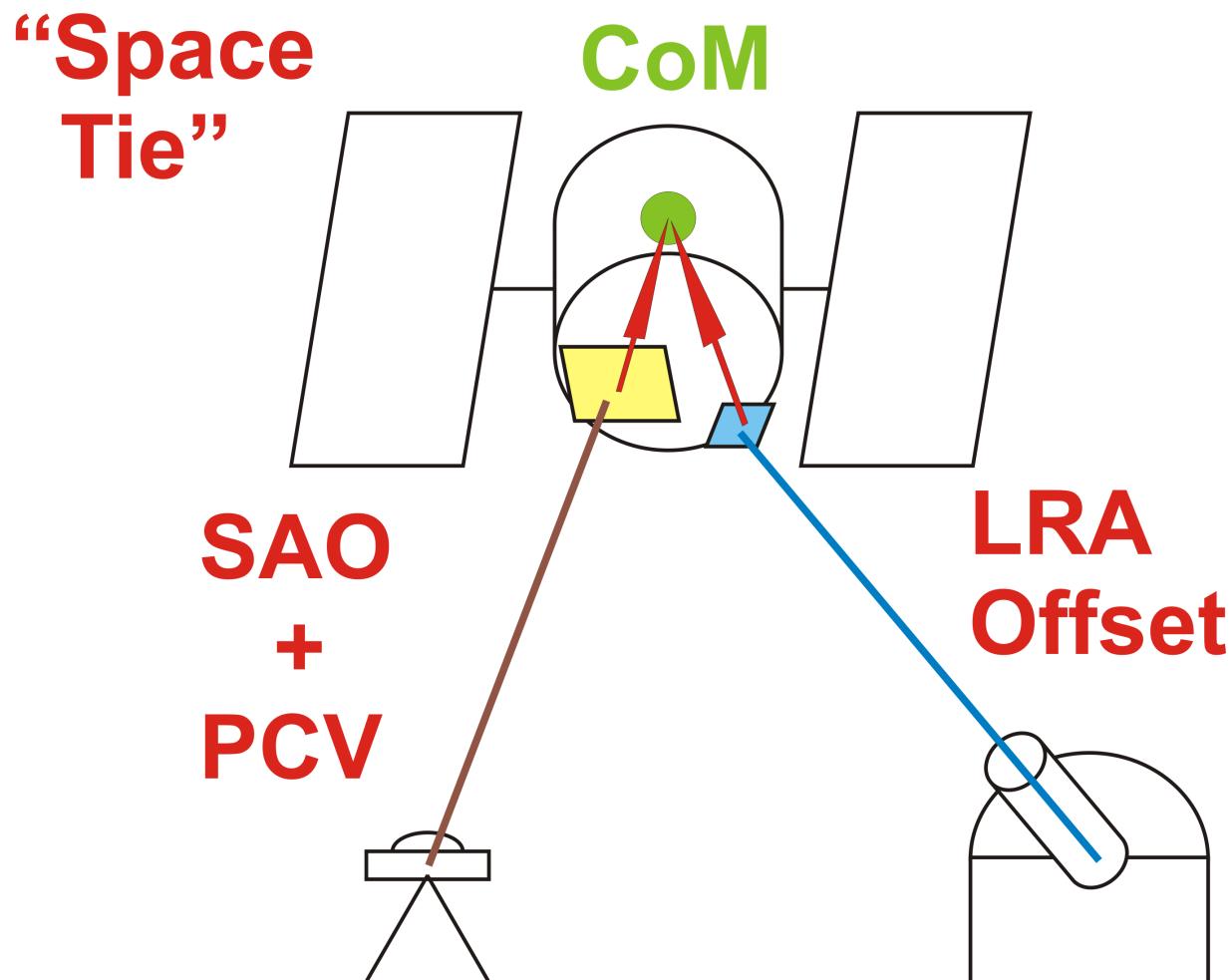
- bad **global distribution** of co-location sites
- only **few** co-locations (37)
- questions concerning **accuracy, transformation** local measurements → global



*from ITRF2008-D solution (provided by M. Seitz, DGFI)*

# Co-locations for GNSS and SLR

**Co-location at GNSS satellites** = Common orbit parameters from GNSS microwave and SLR range data  
→ Vectors of GNSS and SLR reference points w.r.t. satellite CoM needed



*Space Tie* =

1. GNSS Satellite Antenna Offsets (SAO) w.r.t. CoM
2. GNSS Phase Center Variations (PCV)
3. Offsets for Laser Retroreflector Array (LRA) w.r.t. CoM

# Expectation from combined analysis

|  | GNSS @GNSS                            | SLR @GNSS  | SLR @Lageos             |
|--|---------------------------------------|--|-------------------------|
| <b>Radiation pressure<br/>↔ Geocenter</b>                  | Problems in RPR<br>modelling          | Problems in RPR<br>modelling                     | RPR well<br>modelled    |
| <b>GNSS satellite<br/>antenna phase center<br/>↔ Scale</b> | Problems in phase<br>center modelling | independent                                      | -                       |
| <b>Range biases<br/>↔ Scale</b>                            | -                                     | Decorrelated if<br>different elevation<br>angles | For a few sites<br>only |

## SLR @GNSS:

⇒ **Geocenter** is affected as well ⇒ LAGEOS needed

⇒ **Scale** is transferred to GNSS ⇒ LAGEOS helps for decorrelation

# SLR tracking of GNSS satellites

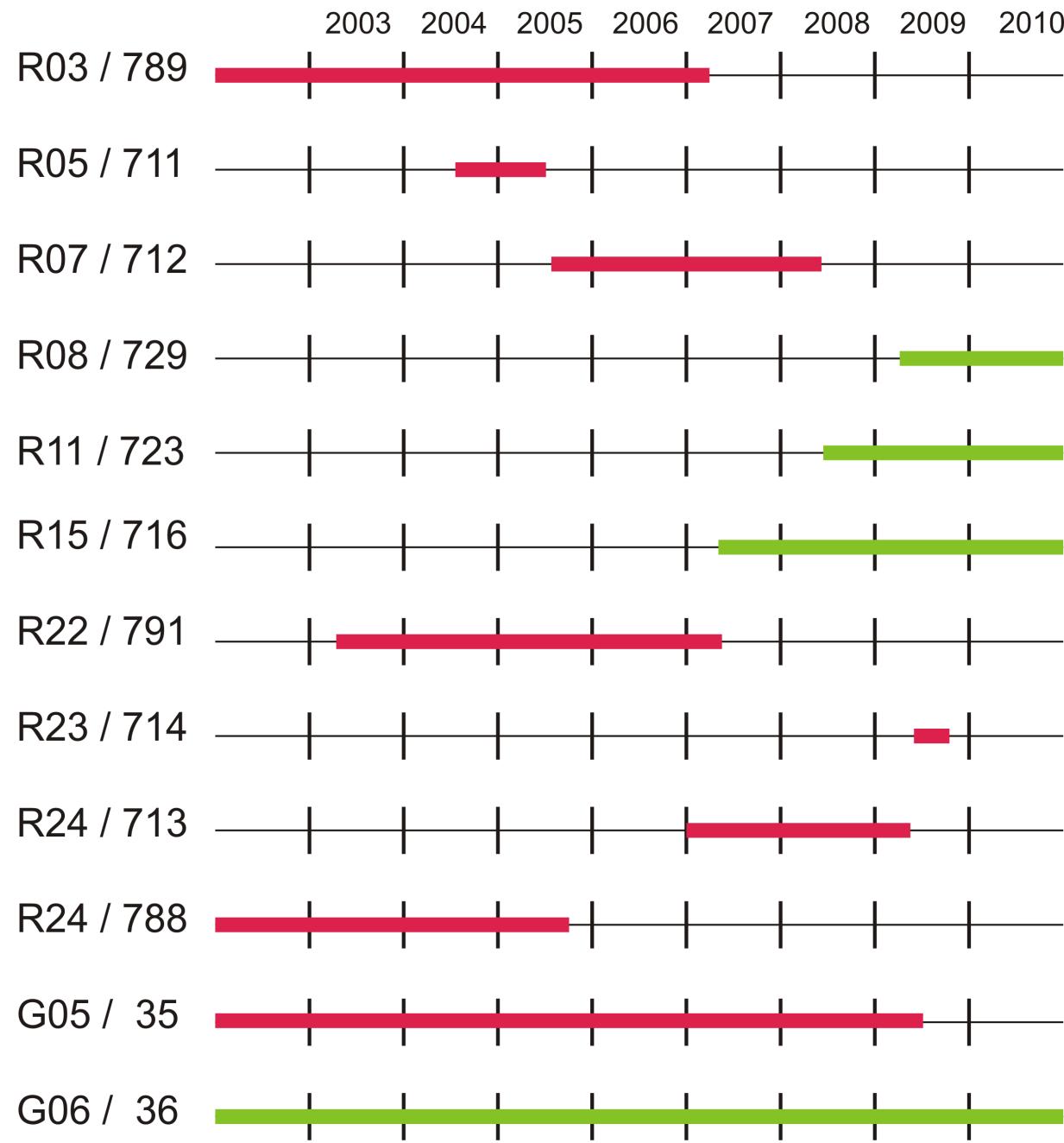
→ Only **2 GPS satellites** are equipped with retro-reflector arrays (G05, G06)

→ **All GLONASS satellites** are equipped with retro-reflector arrays

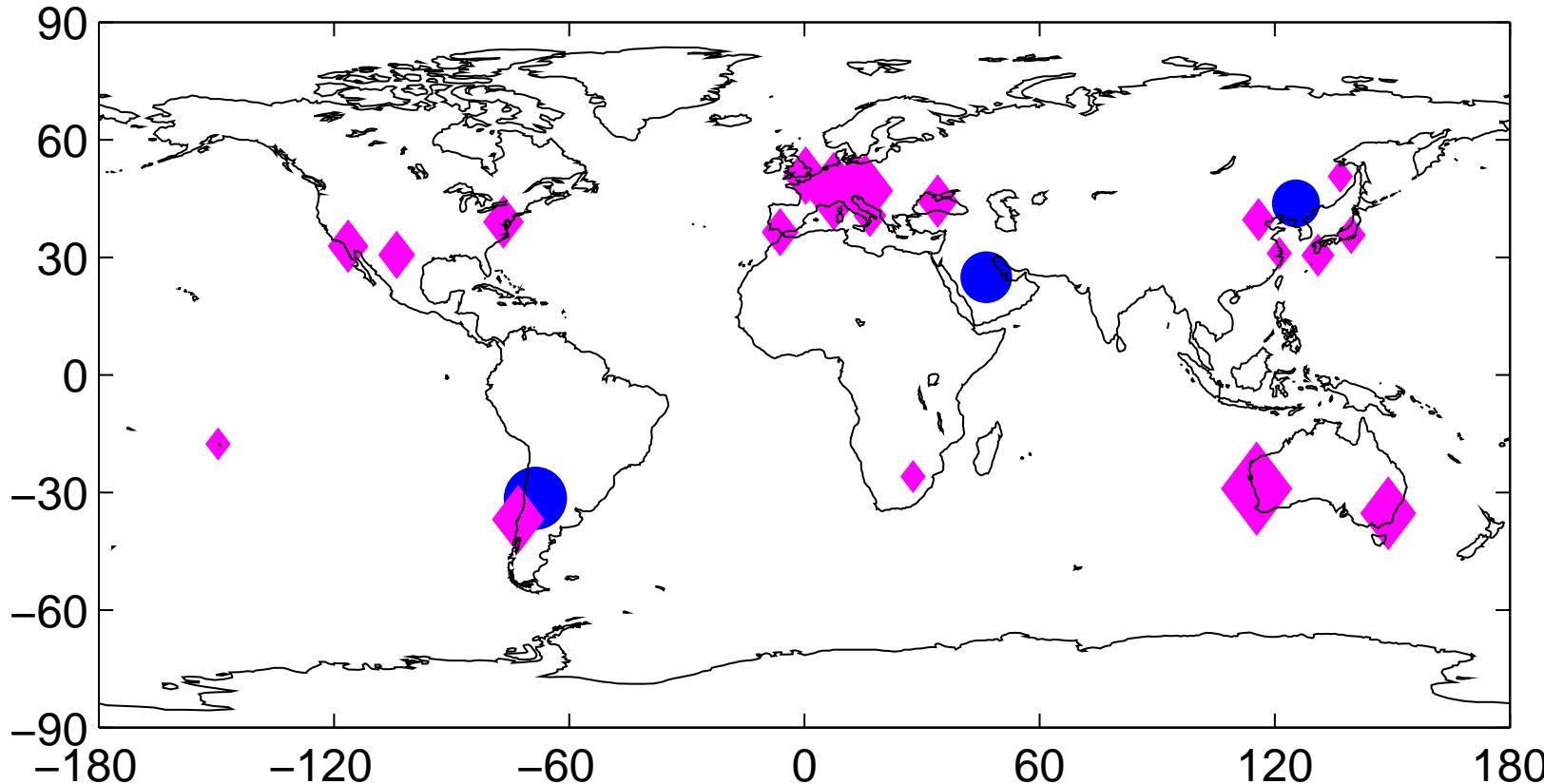
→ SLR tracking for selected GNSS satellites:

**2 GPS** → 2009: 1

**3 GLONASS** → 2010: 6



# SLR tracking of GNSS satellites



**Satellites tracked in 2008:**

**GPS:** G05  
G06

**GLONASS:**  
R15  
R24  
R07  
R11

Altogether (2008):

**25** SLR sites

**31855** normal points (NP)

**8 sites with > 1000 NP**

**5 sites with > 500 NP**

6 sites with > 100 NP

6 sites with < 100 NP

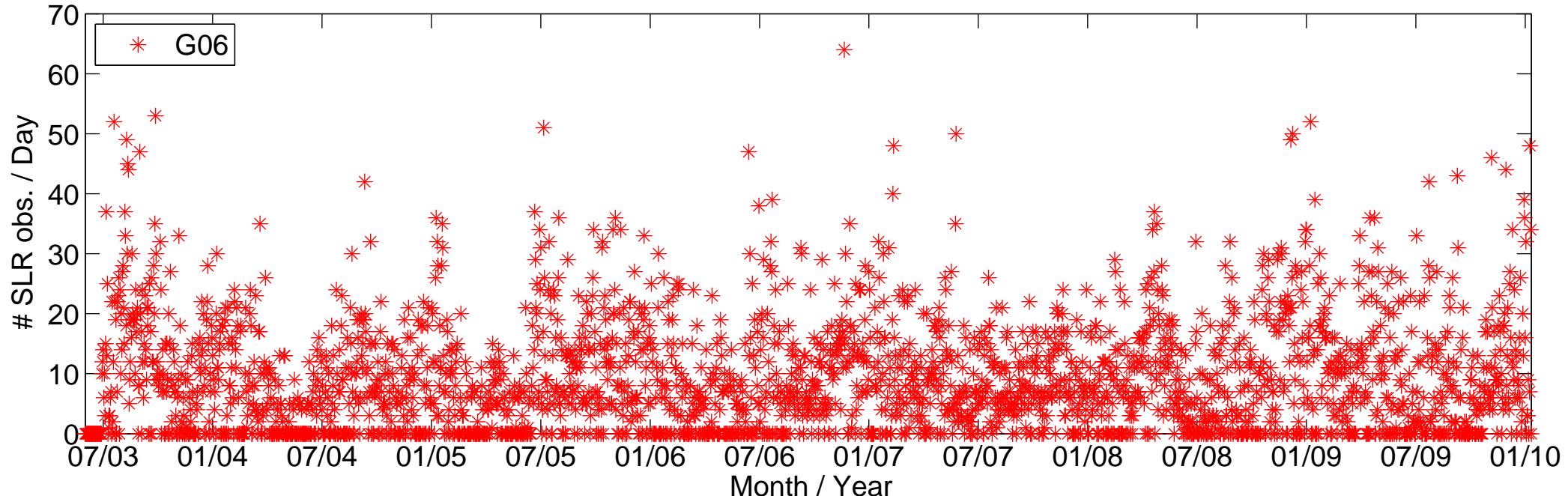
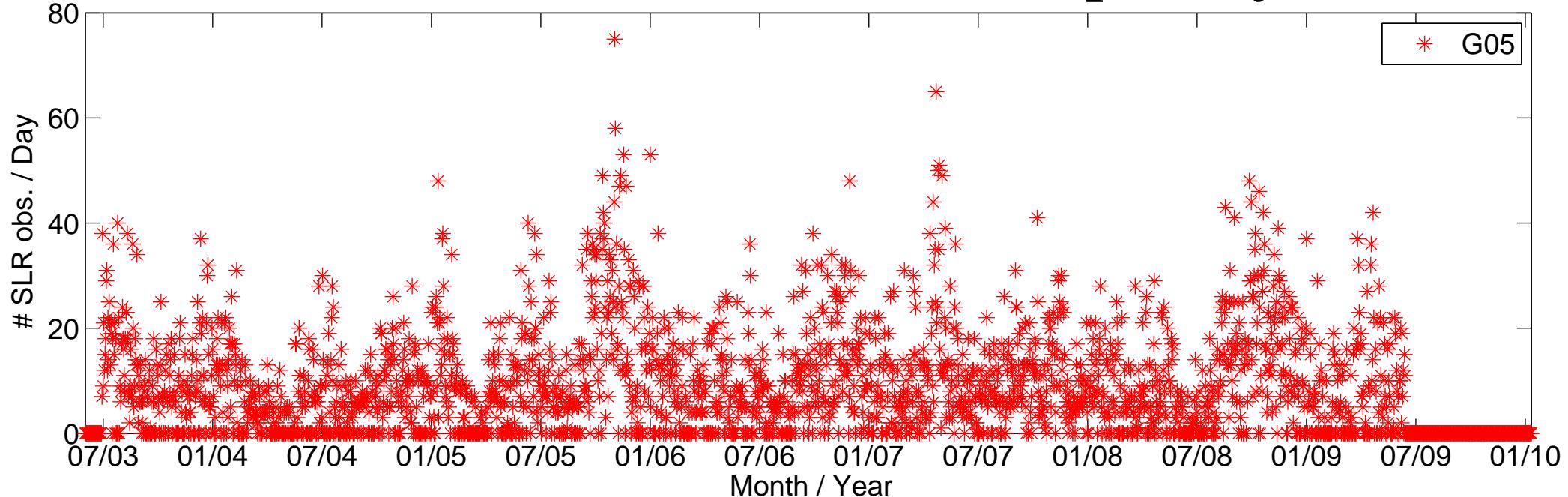
**Northern hemisphere:**

16804 NP

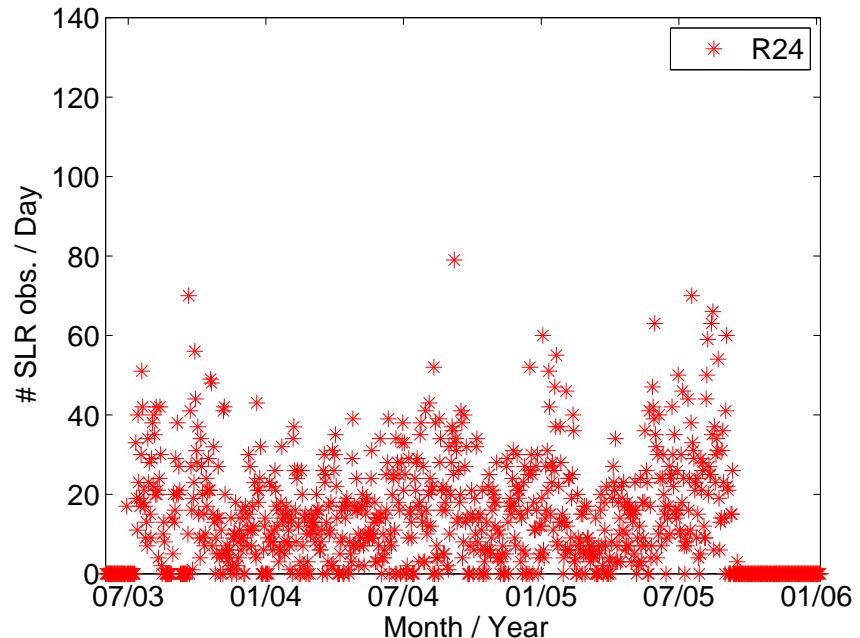
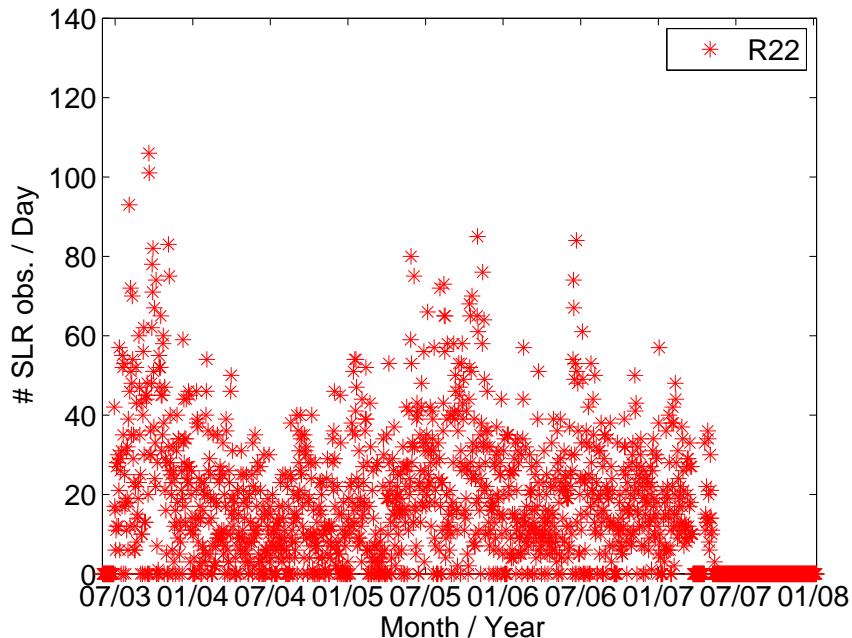
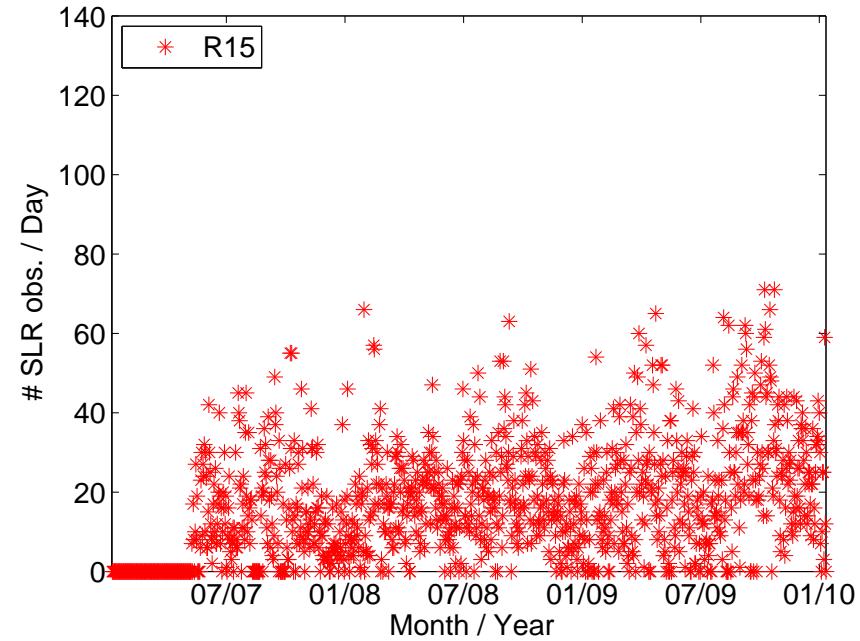
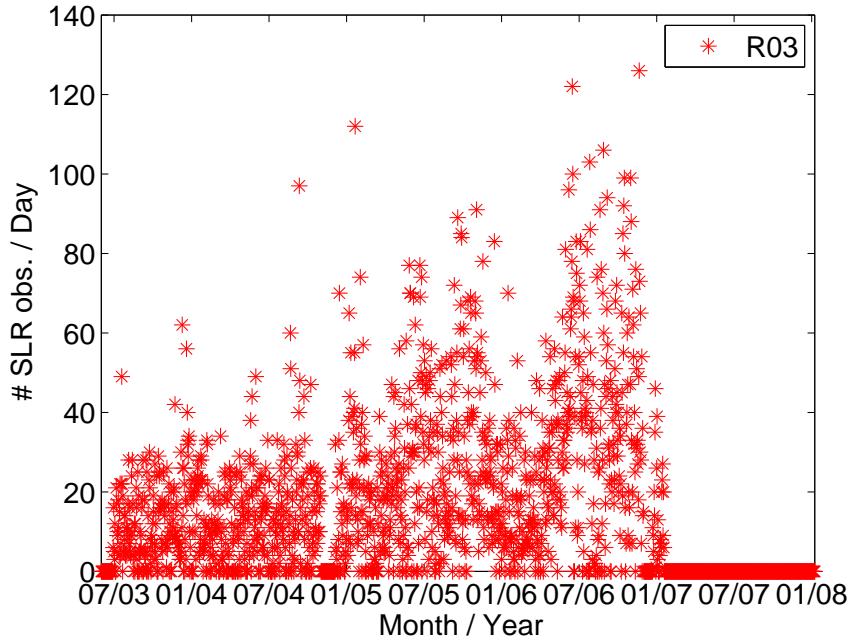
**Southern hemisphere:**

15051 NP

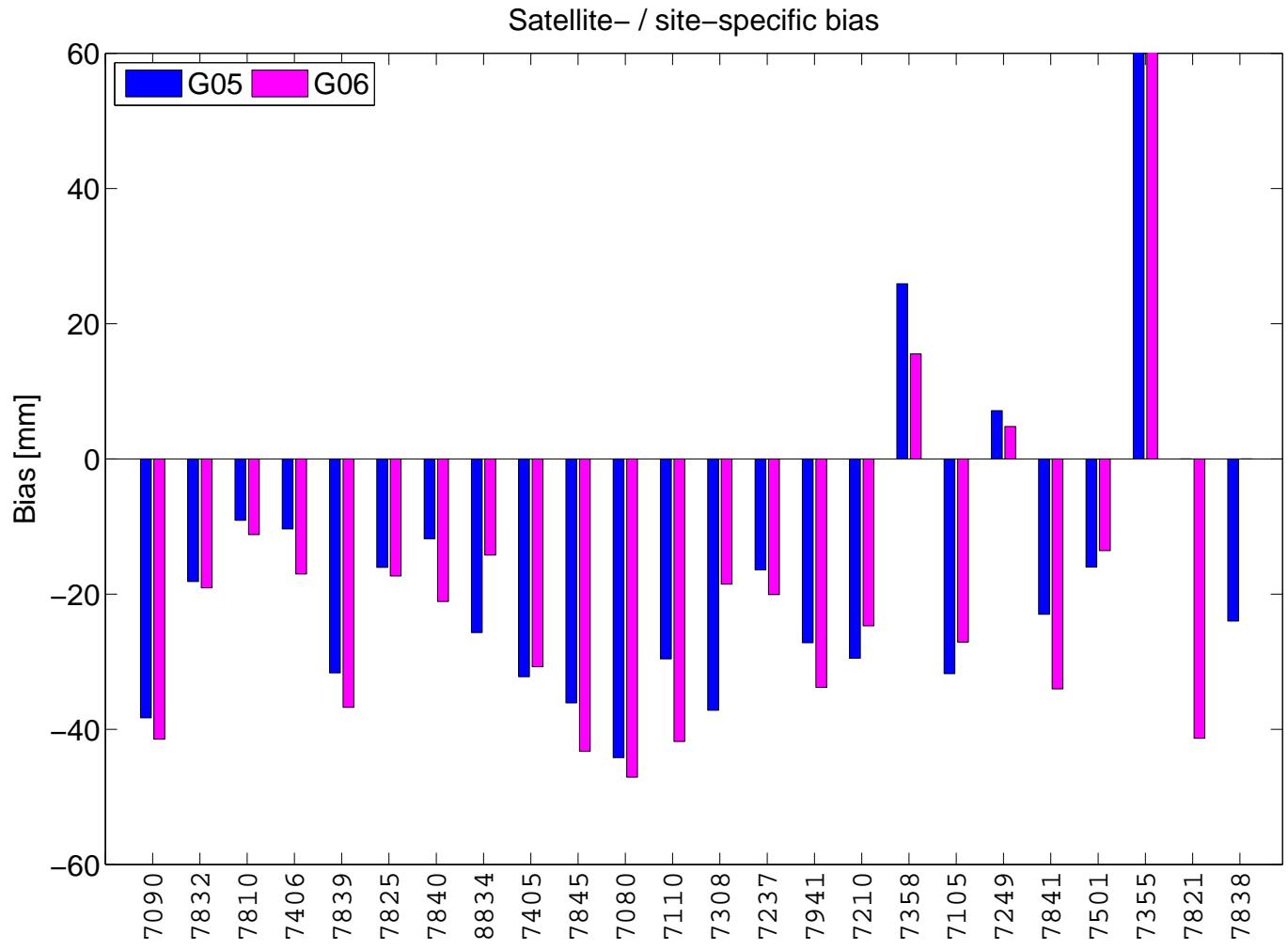
# Number of SLR observations per day



# Number of SLR observations per day



# SLR residuals: Mean bias



Mean bias for all stations  
for 2003 – 2009 [mm]:

| G05   | G06   |
|-------|-------|
| -24.0 | -26.4 |

| R03   | R07  | R11   | R15  | R22   | R24a  | R24b  |
|-------|------|-------|------|-------|-------|-------|
| -13.5 | -8.6 | -19.5 | -2.6 | -14.1 | -17.9 | -16.0 |

# Combined analysis of GNSS and SLR

## *Problems and Questions:*

Only **few SLR observations** to GNSS satellites (10 – 20 per day)

- Weak estimation of parameters
- Daily solutions not possible

**Correlations** between parameters (**offsets**, **range biases**) and **scale**

- Common estimation possible?

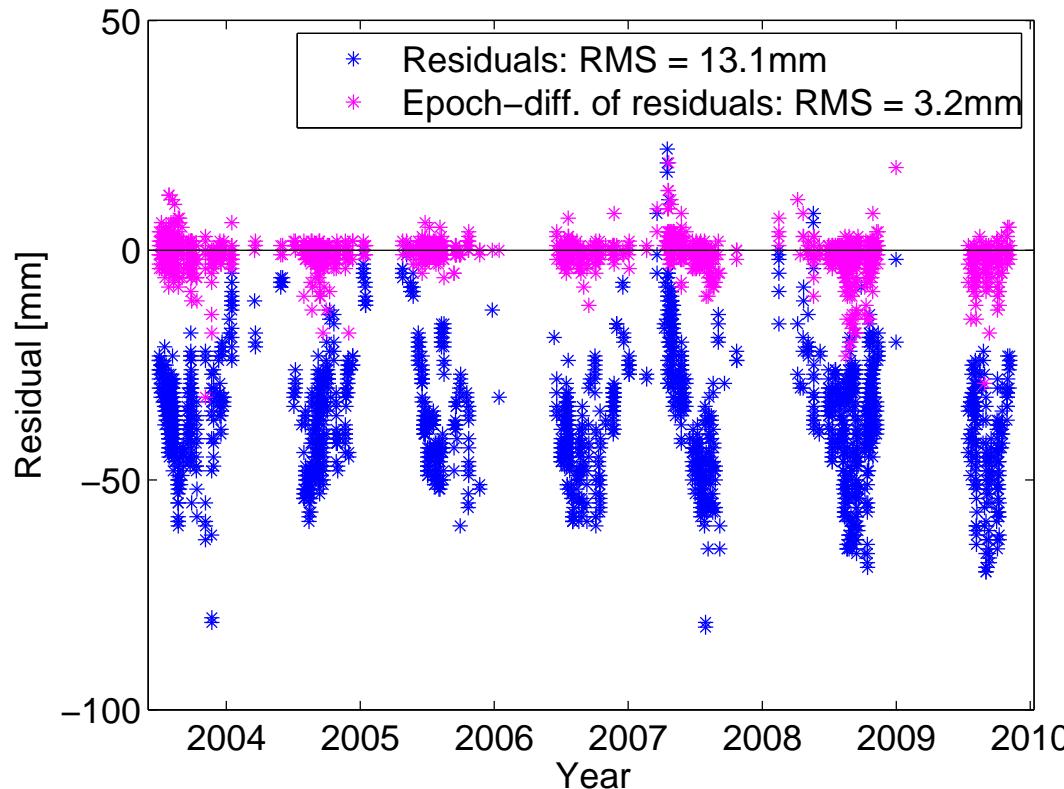
Are satellite co-locations (**space ties**) strong enough or are co-locations on ground (**local ties**) needed additionally?

**Biases between GNSS and SLR** are seen in SLR range residuals to given microwave-based orbits

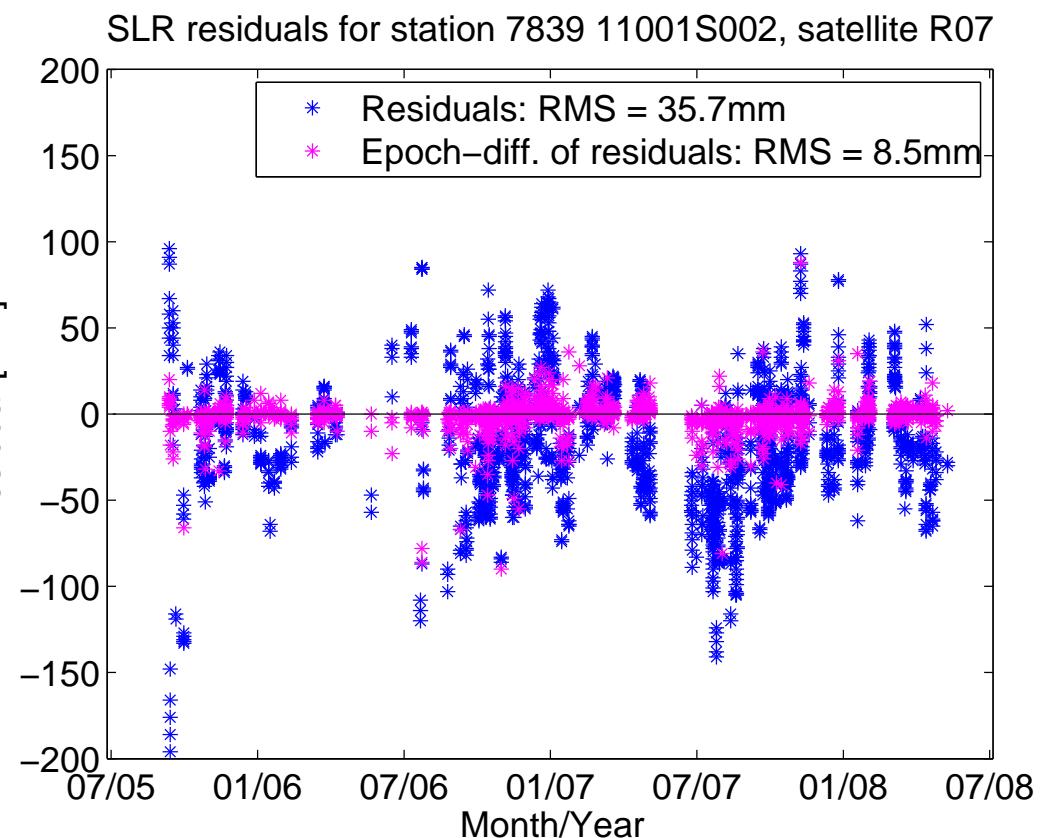
- Several possible error sources ...

# Systematic effects between SLR and GNSS

SLR residuals for station 7839 11001S002, satellite G06



- 1) Biases in SLR range residuals (cm-level)
  - 2) Epoch-differences of SLR range residuals have a much smaller RMS
- ⇒ systematic effects



# Systematic effects between SLR and GNSS

**Possible reasons for systematic effects in SLR range residuals:**

SLR station coordinates (fixed to SLRF2005)

TRF (scale, geocenter)

Offset for GNSS satellite antenna (SAO from igs05.atx)

Offset for laser reflector array (LRA from ILRS web site)

SLR range biases (unknown for GNSS satellites)

GNSS orbit modelling (solar radiation pressure)

⇒ **Must be handled in combined solution:**

- use known / better values
- **Estimation**

# Combined analysis of GNSS and SLR

SLR station coordinates

→ estimate + inclusion of LAGEOS

TRF scale (and geocenter)

→ use from SLR

Offset for GNSS satellite antenna (SAO from igs05.atx)

→ estimate

Offset for laser reflector array (LRA from ILRS web site)

→ estimate

SLR range biases (unknown for GNSS satellites)

→ estimate + inclusion of LAGEOS

GNSS has rank-deficiency w.r.t. scale if SAO are estimated

Estimation of 1 bias parameter per station / per GNSS satellite

⇒ GNSS-microwave + SLR@GNSS + SLR@LAGEOS for 2006-2009

# Combined analysis of GNSS and SLR

→ ***GNSS-only NEQs (daily):***

- Combined GPS+GLONASS analysis performed at CODE
- Re-analysis for 2003 – 2008, routine IGS analysis for 2009

→ ***SLR-only NEQs for SLR@GNSS (daily):***

- SLR data to GPS and GLONASS satellites
- Parameterization identical to GNSS analysis (orbits, ERP, geocenter)
- Range biases for all sites

→ ***Combination of daily NEQs***

→ ***SLR-NEQs for Lageos (weekly):***

- Range biases only for selected sites

→ ***Combination of NEQs and accumulation to long-term solution:***

- Use of “Space ties” only; Local ties are not applied!

# SLR station coordinates

## SLR station network

- Not included in the datum definition (no-net-rotation, no-net-translation)
- No local ties applied
- Only appended via the „space ties“ (common orbit parameters)

## Validation of SLR station coordinates: Helmert transformation

| RMS |                | SLRF2005     | Lageos-only |      |
|-----|----------------|--------------|-------------|------|
|     | Comb: SLR@GNSS | <b>54.40</b> | 54.22       | [mm] |
|     | Comb: + Lageos | <b>6.70</b>  | 2.95        | [mm] |
|     | Lageos-only    | <b>7.49</b>  |             | [mm] |

- Agreement is at the **cm-level** if only SLR@GNSS is used
- **Inclusion of Lageos** improves the coordinate estimates
- Connection by using space ties only is feasible

# SLR station coordinates

## SLR station network:

- Not included in the datum definition (no-net-rotation, no-net-translation)
  - No local ties applied
- Only appended via the „space ties“ (common orbit parameters)

## Validation of SLR station coordinates: Helmert transformation

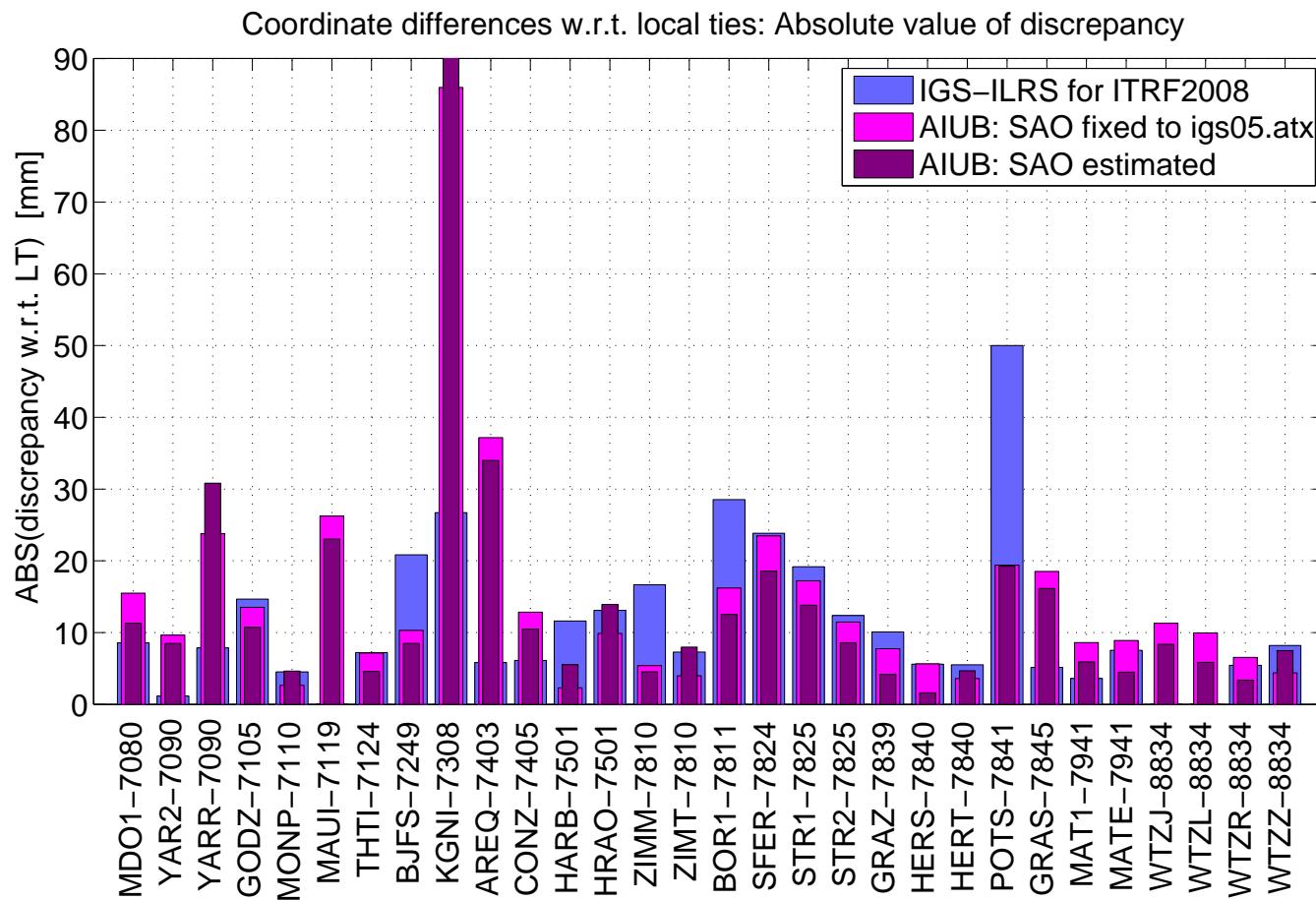
| Scale          | SLRF2005            | Lageos-only  |       |
|----------------|---------------------|--------------|-------|
| Comb: SLR@GNSS | <b>1.06 +- 2.76</b> | 2.34 +- 2.75 | [ppb] |
| Comb: + Lageos | <b>1.02 +- 0.34</b> | 0.25 +- 0.15 | [ppb] |
| Lageos-only    | <b>1.28 +- 0.38</b> |              | [ppb] |

→ Scale of SLR is defined well

→ **Inclusion of Lageos** improves the coordinate estimates

# Comparison with co-located GNSS sites

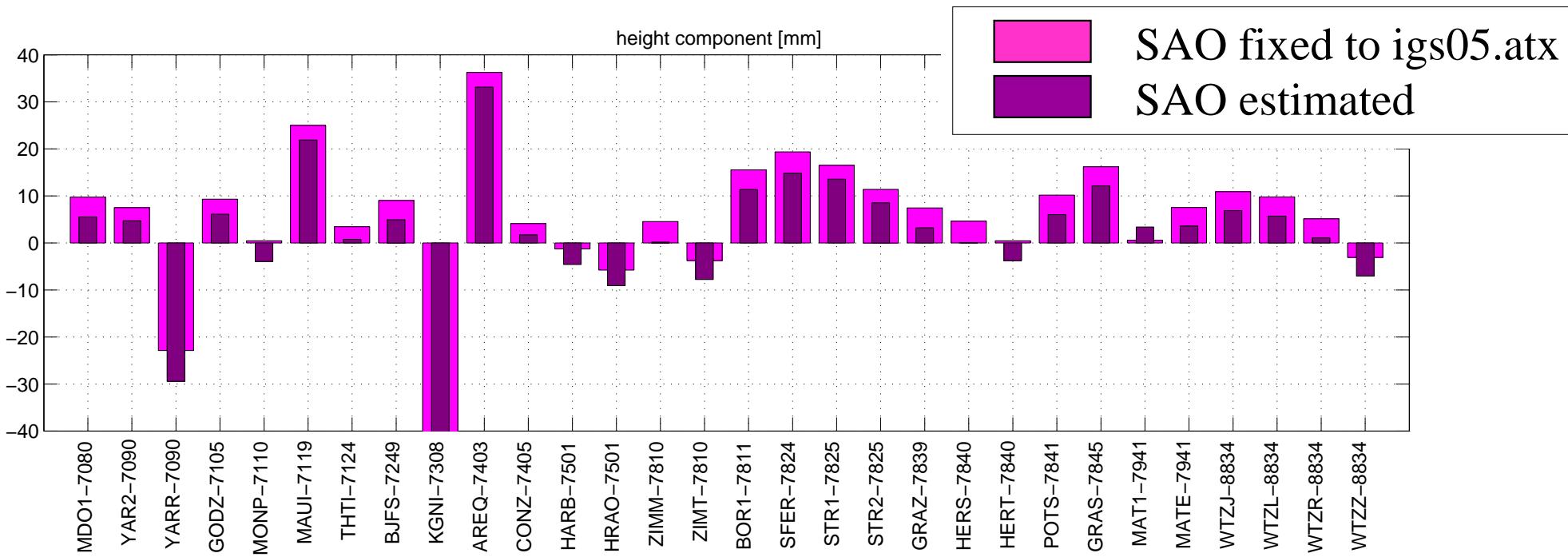
1. Estimated SLR and GNSS station coordinates  $\Rightarrow \Delta\text{CRD\_estimate}$
  2. Local tie between SLR and GNSS reference points:  $\Delta\text{CRD\_LT}$
- $\Rightarrow \Delta\text{CRD\_estimate} - \Delta\text{CRD\_LT}$



from ITRF2008-D solution (provided by M. Seitz, DGFI)

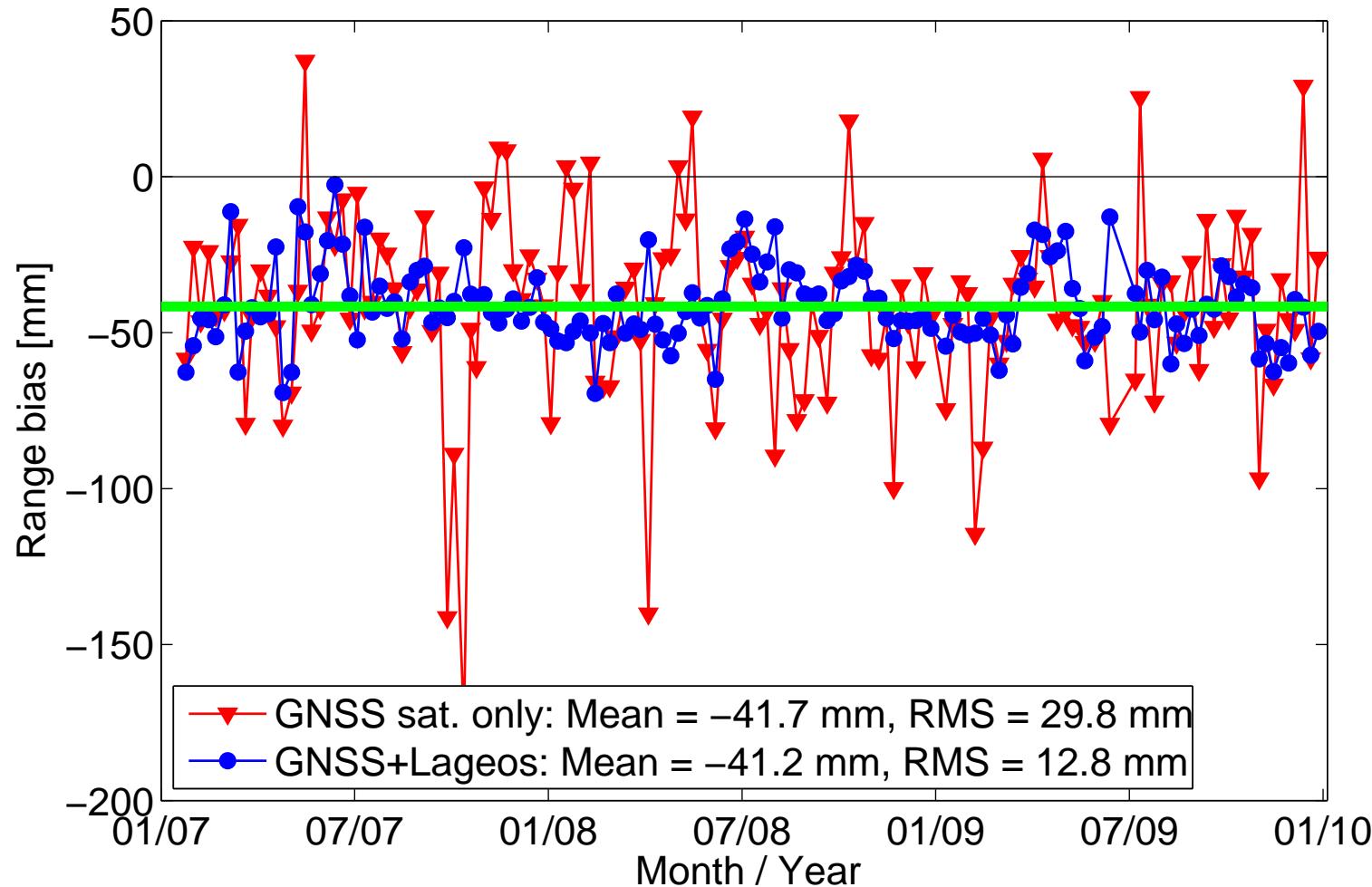
# Comparison with local ties

1. Estimated SLR and GNSS station coordinates  $\Rightarrow \Delta\text{CRD\_estimate}$
  2. Local tie between SLR and GNSS reference points:  $\Delta\text{CRD\_LT}$
- $\Rightarrow \Delta\text{CRD\_estimate} - \Delta\text{CRD\_LT}$ : Height component
- $\Rightarrow$  Agreement between GNSS and SLR sites better if GNSS SAO are estimated  
(i.e. using the SLR scale)



# SLR-GNSS biases

SLR range biases from weekly solutions: Station 7090



- **Weekly** estimation from **SLR@GNSS** data only: not possible
- Inclusion of **Lageos** data improves weekly solutions
- **Yearly (or multi-year)** solutions needed for reliable values

# SLR-GNSS biases and GNSS SAO

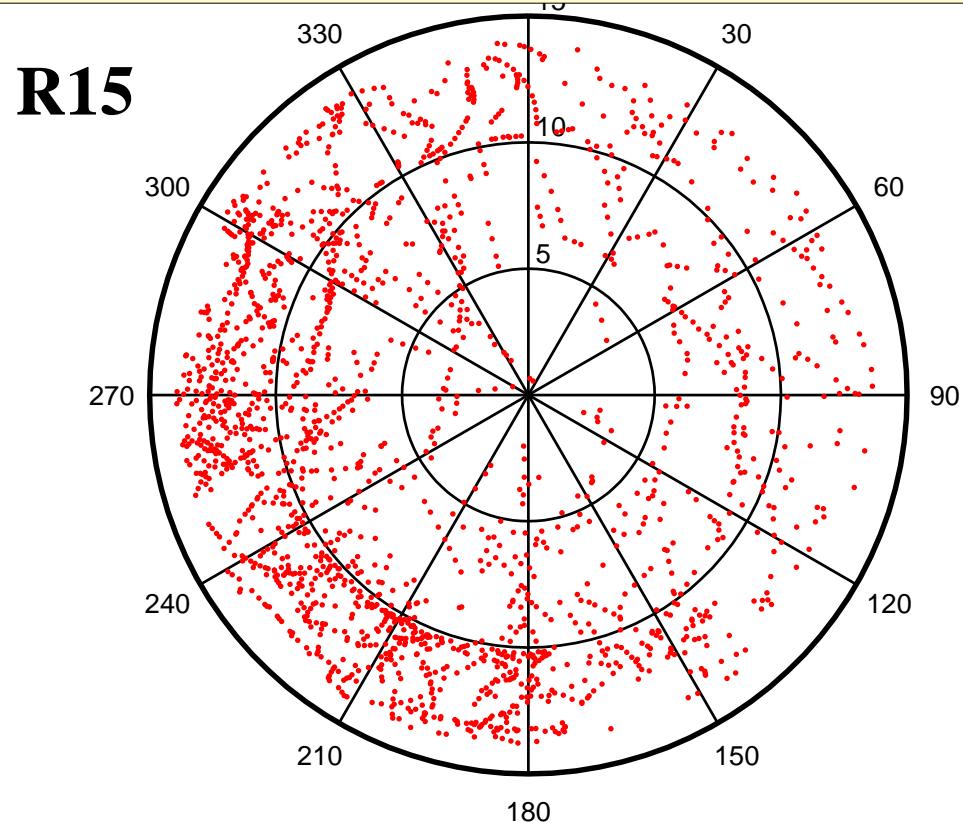
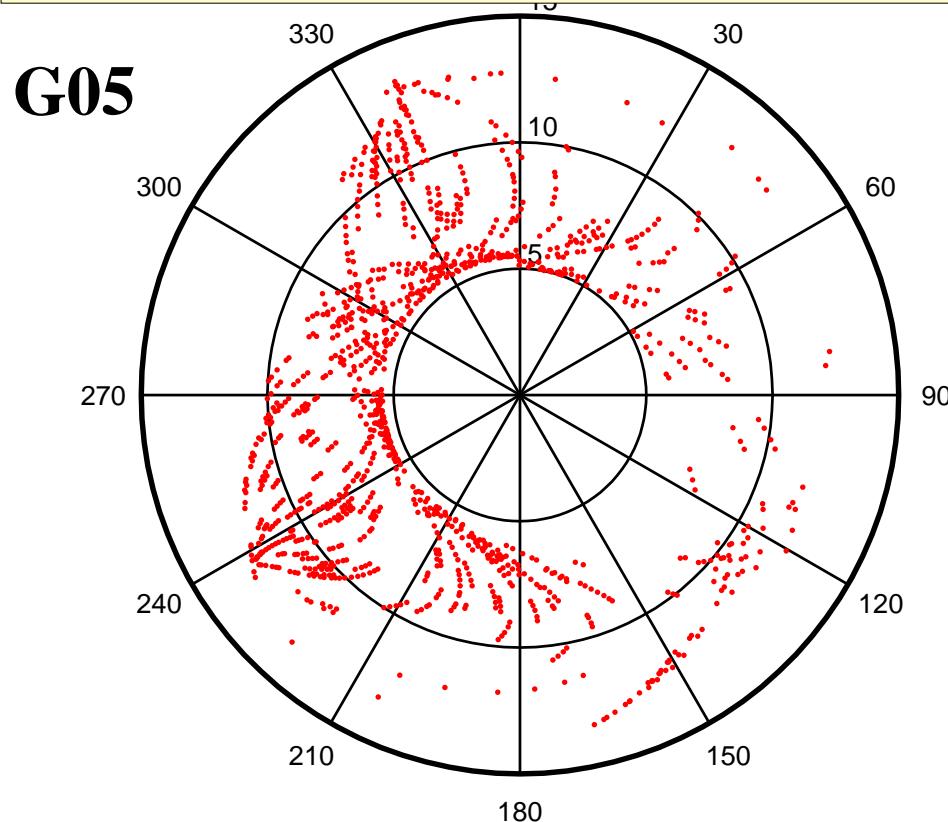
Effect of range bias:

identical effect for all directions of the observation

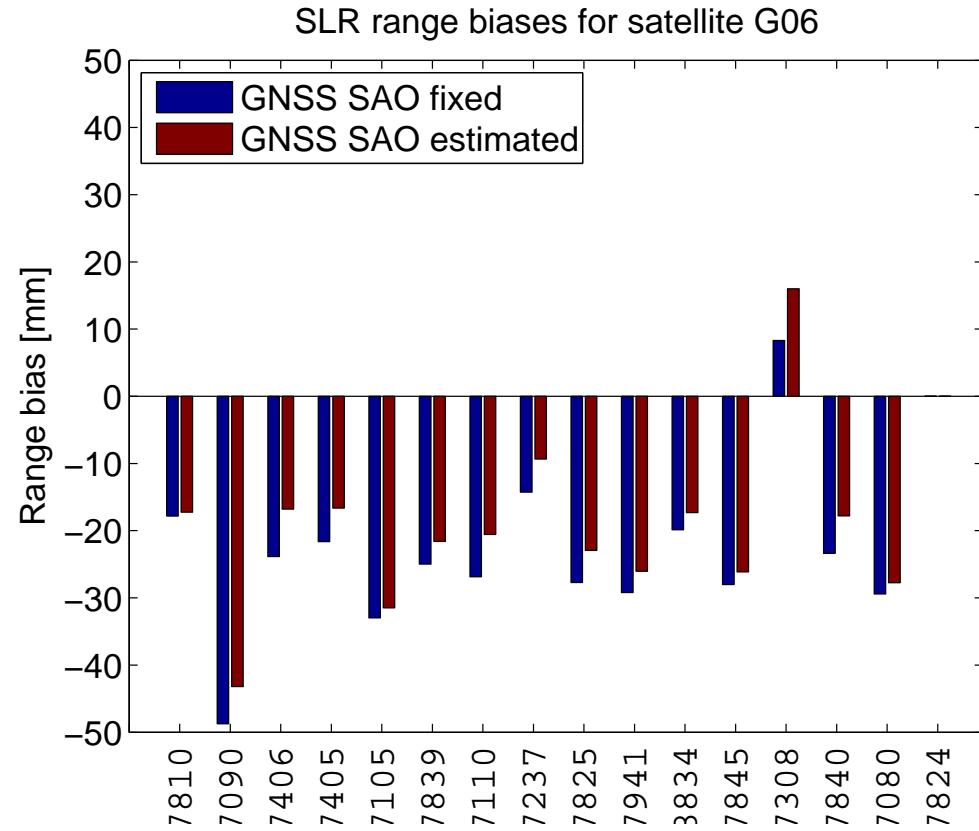
Effect of SAO:

different size for different directions of the observation

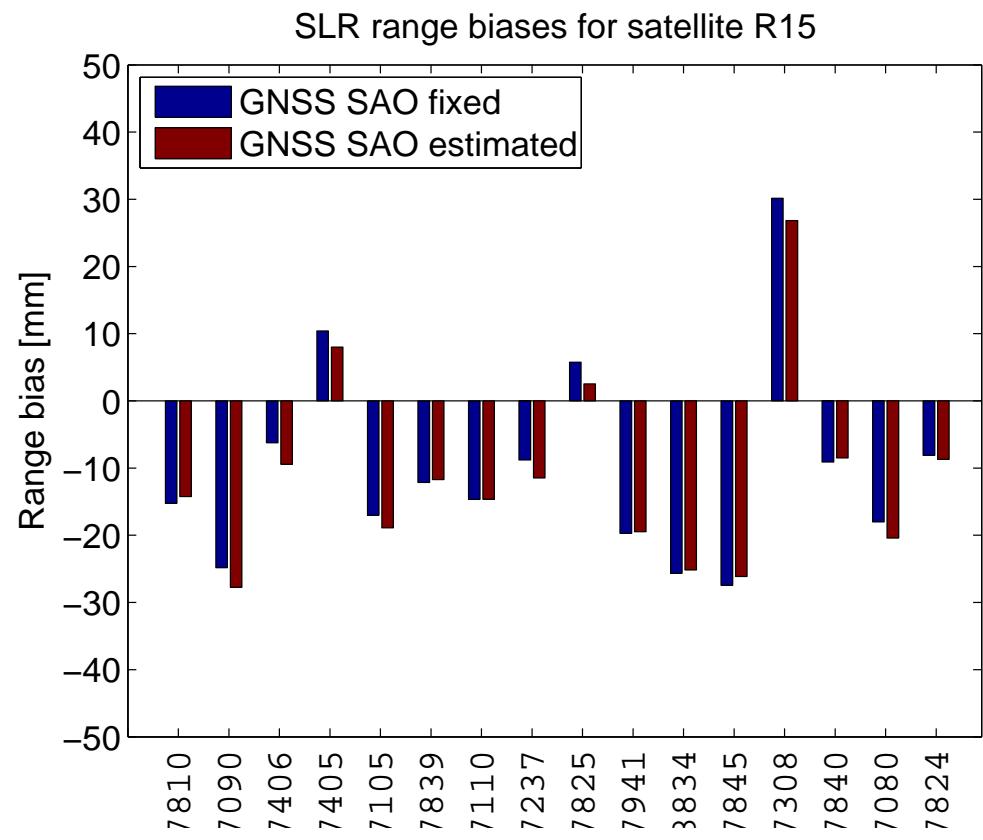
⇒ Correlation can be reduced by homogeneous distribution of observations  
(regarding nadir / azimuth angle at the satellite)



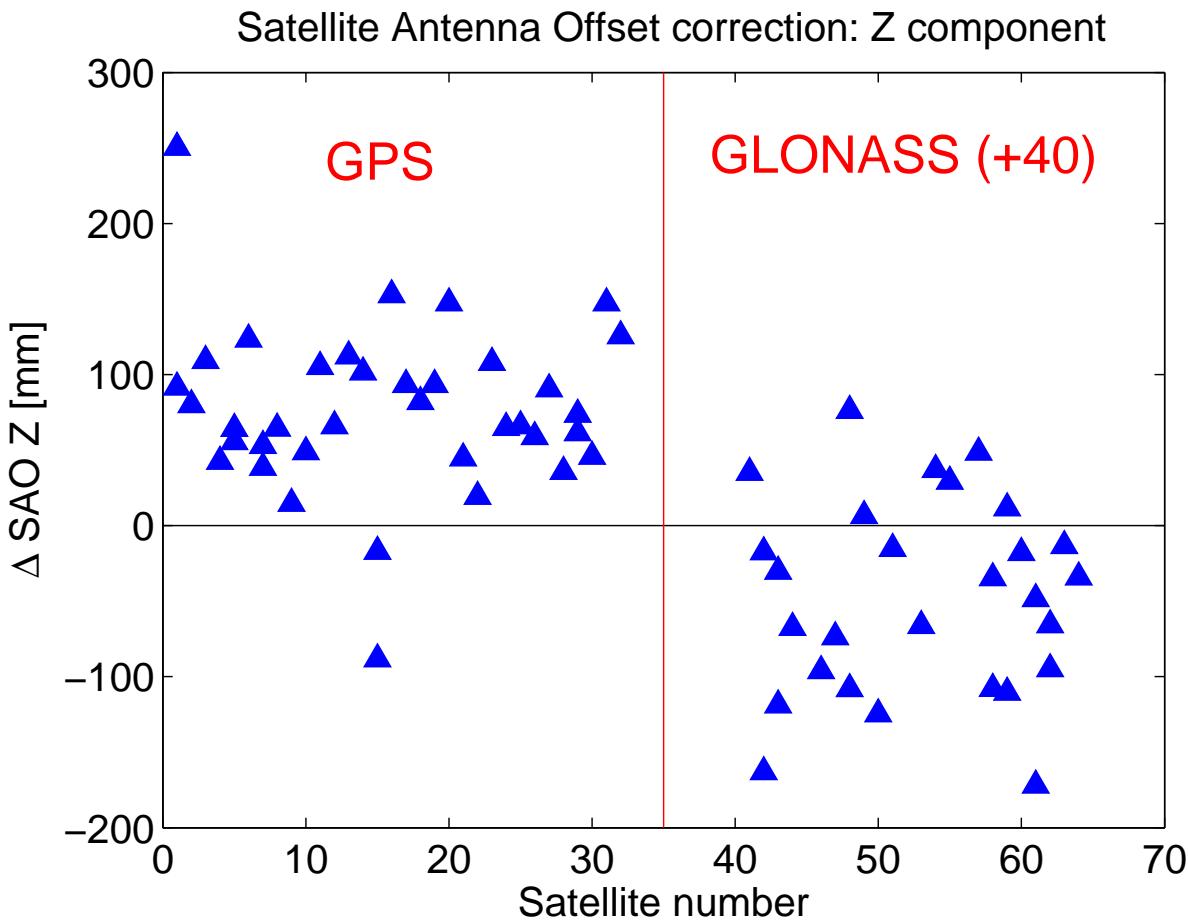
# SLR-GNSS biases and GNSS SAO



Impact of GNSS-SAO estimation  
on SLR-GNSS „range“ biases:  
 $\wedge 5$  mm



# SLR-GNSS biases and GNSS SAO

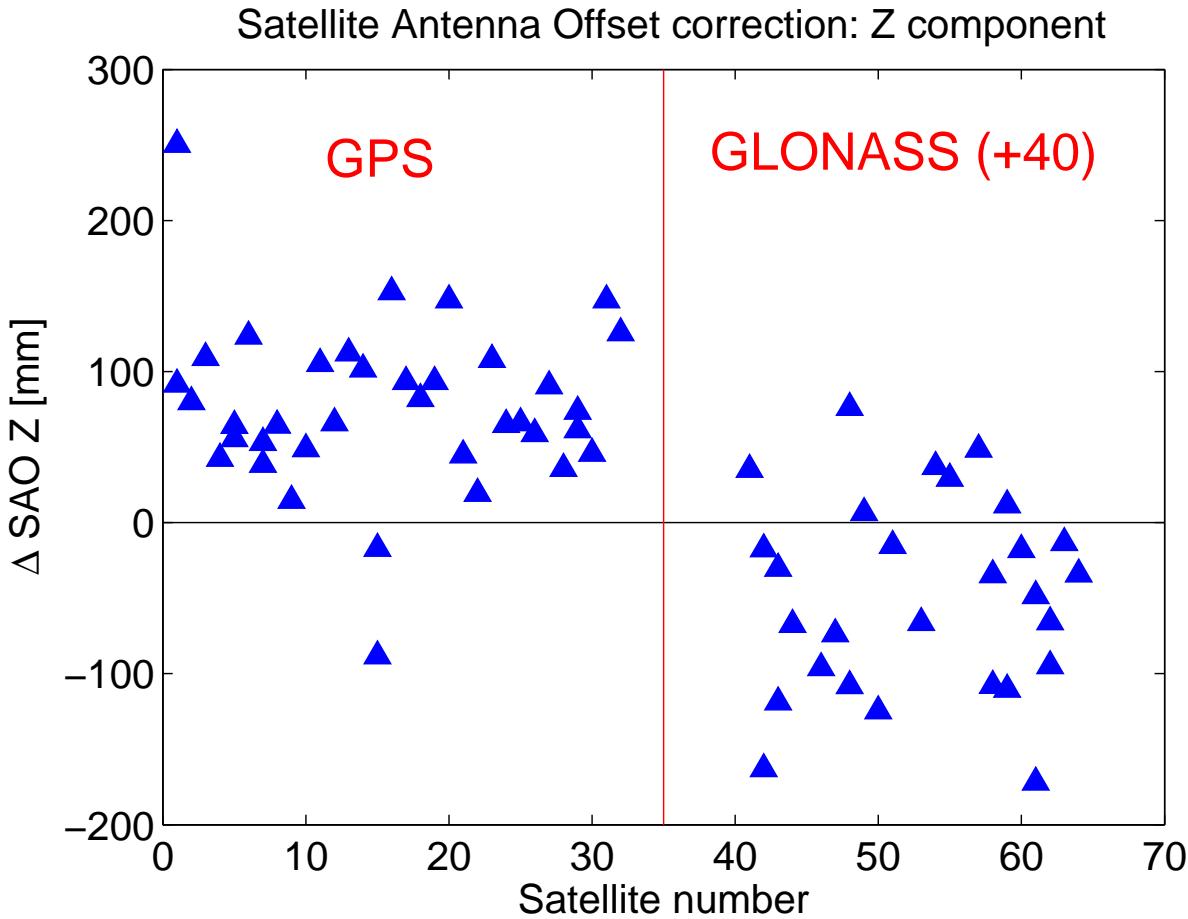


Mean  $\Delta Z$  for GPS:  
**76.4 mm**

Mean  $\Delta Z$  for GLONASS:  
**-47.7 mm**

No general shift of SAO estimates  
⇒ Scale of SLR is transferred properly  
to GNSS

# SLR-GNSS biases and GNSS SAO



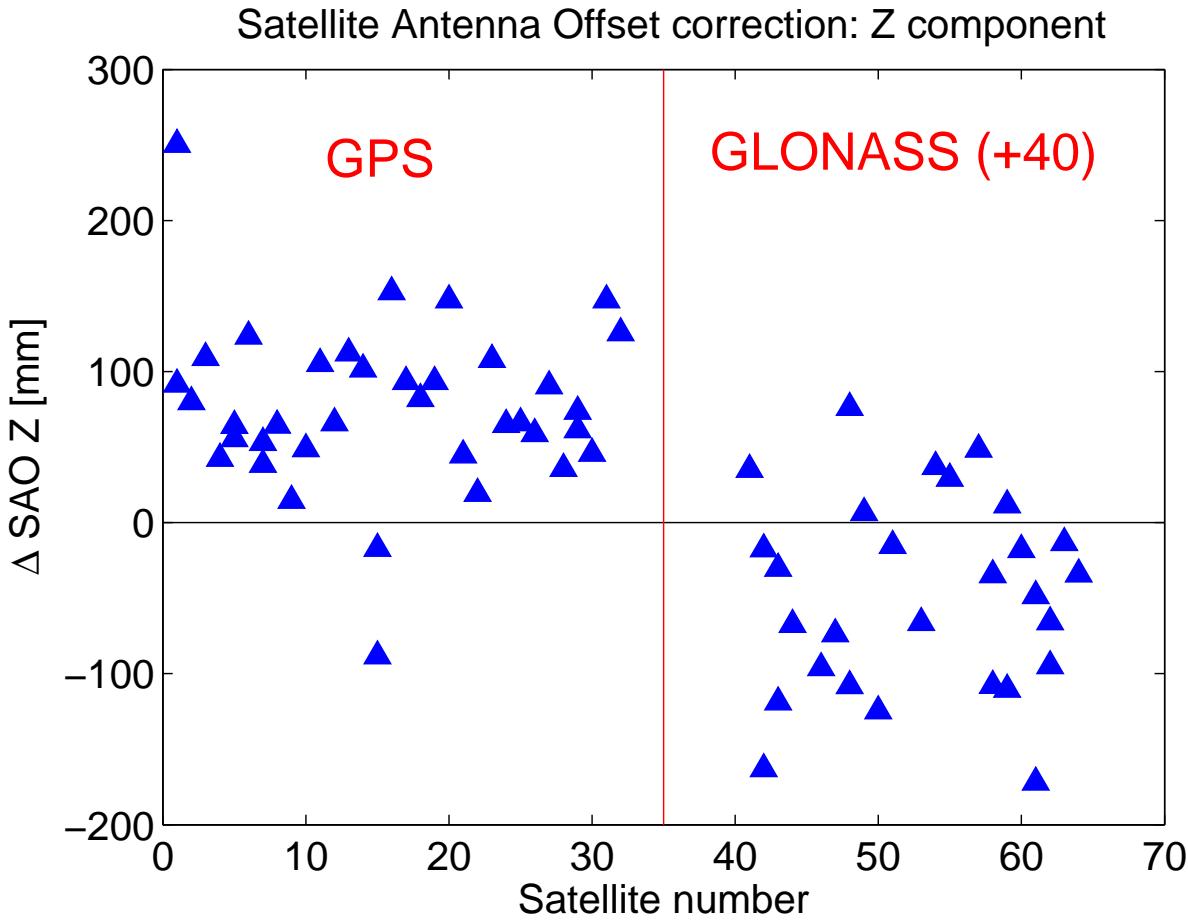
Mean  $\Delta Z$  for GPS:  
**76.4 mm**  
 $\approx 0.59 \text{ ppb}$

Mean  $\Delta Z$  for GLONASS:  
**-47.7 mm**

$$\Delta \text{scale}_{[\text{ppb}]} \approx -7.8 \bullet \Delta \text{SAO}_{[\text{m}]}$$

No general shift of SAO estimates  
⇒ Scale of SLR is transferred properly  
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# SLR-GNSS biases and GNSS SAO



No general shift of SAO estimates  
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Mean  $\Delta Z$  for GPS:  
**76.4 mm**  
 $\approx 0.59 \text{ ppb}$

Mean  $\Delta Z$  for GLONASS:  
**-47.7 mm**

$$\Delta \text{scale}_{[\text{ppb}]} \approx -7.8 \bullet \Delta \text{SAO}_{[\text{m}]}$$

$\Delta \text{Scale}$  for GNSS network:  
**0.59 ppb**

$\Delta \text{Scale}$  for SLR network:  
**0.00 ppb**

# Zusammenfassung und Ausblick -1-

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- **LAGEOS**-Prozessierung mit BSW ist auf einem guten Stand
- In Zusammenarbeit mit **BKG** werden täglich Lösungen an den **ILRS** geliefert (seit Juli 2010)
- **Re-Prozessierung** am AIUB bisher für **2006 – 2010**
- Weitergehende Re-Prozessierung im Rahmen eines gemeinsamen Projektes zusammen mit ETH Zürich, TU München und TU Dresden
- Erweiterung für **ETALON** ist momentan in der Testphase
- Verbesserung der **Orbitmodellierung** (Albedo-Modell)
- Weitere Parameter, z.B. **Schwerefeld**

## Zusammenfassung und Ausblick -2-

- Gemeinsame Auswertung von **SLR**- und **Mikrowellen**-Beobachtungen zu **GNSS-Satelliten** erfolgreich
- **LAGEOS** Beobachtungen stabilisieren die kombinierte Lösung
- **SLR-Massstab** wird über Satelliten-Kolokationen direkt ins GNSS-Netz übertragen  
→ ermöglicht Schätzung der **GNSS SAO** ohne Fixieren des apriori Massstabs
- GNSS SAO aus ***igs05.atx*** und **SLR Massstab** sind inkonsistent (0.59 ppb)
- SLR-GNSS-Kombination via „**Space Ties**“ ist möglich (ohne Local Ties)  
→ **Genaue Ties** als Voraussetzung (Stationen und Satelliten)
- **Trennung** von SLR Range Biases und **LRA Offsets** noch nötig

**AIUB**

Rolf Dach, Krzysztof Sosnica, Gerhard Beutler

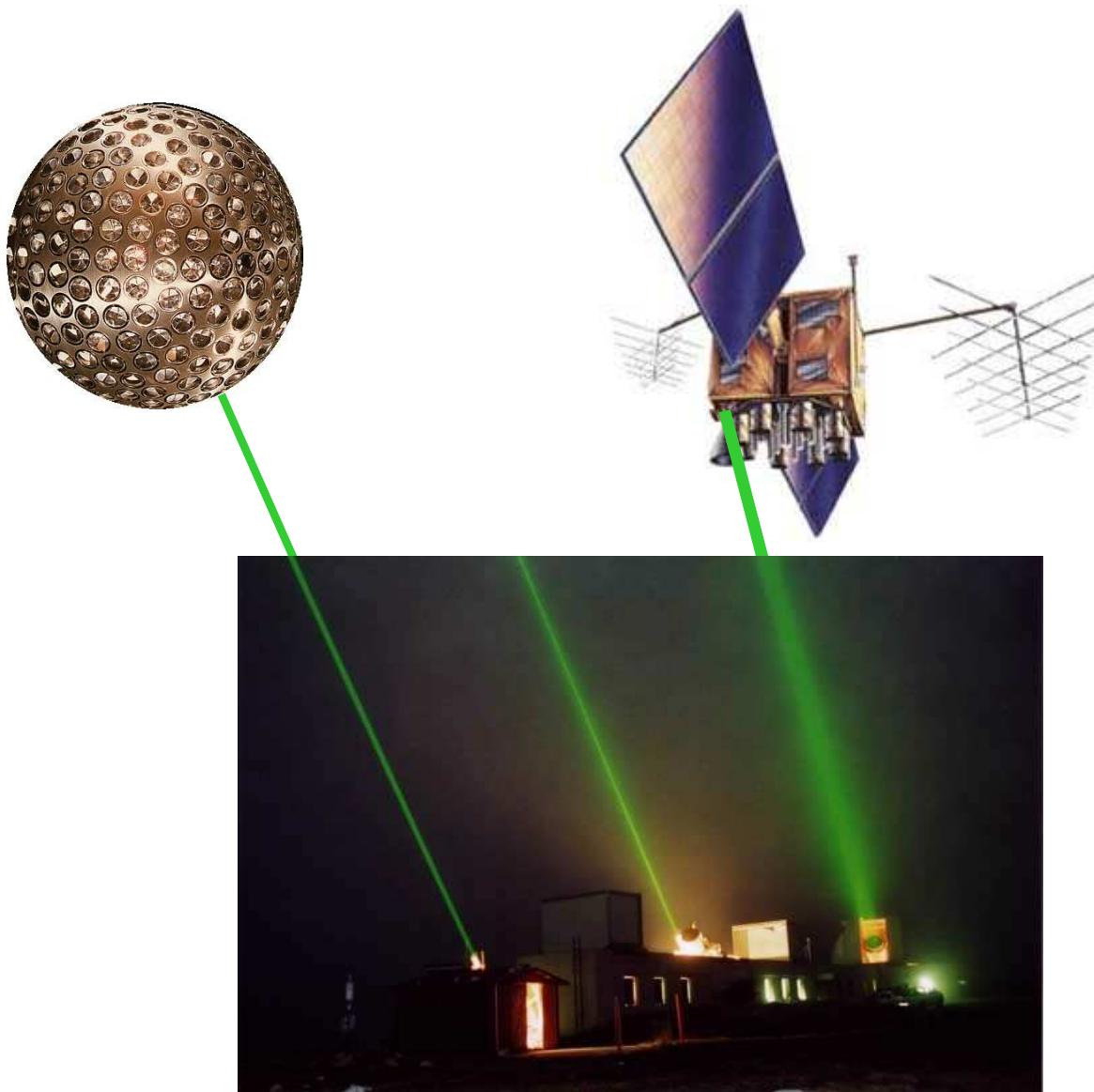
**BKG**

Maria Mareyen, Bernd Richter

**DGFI**

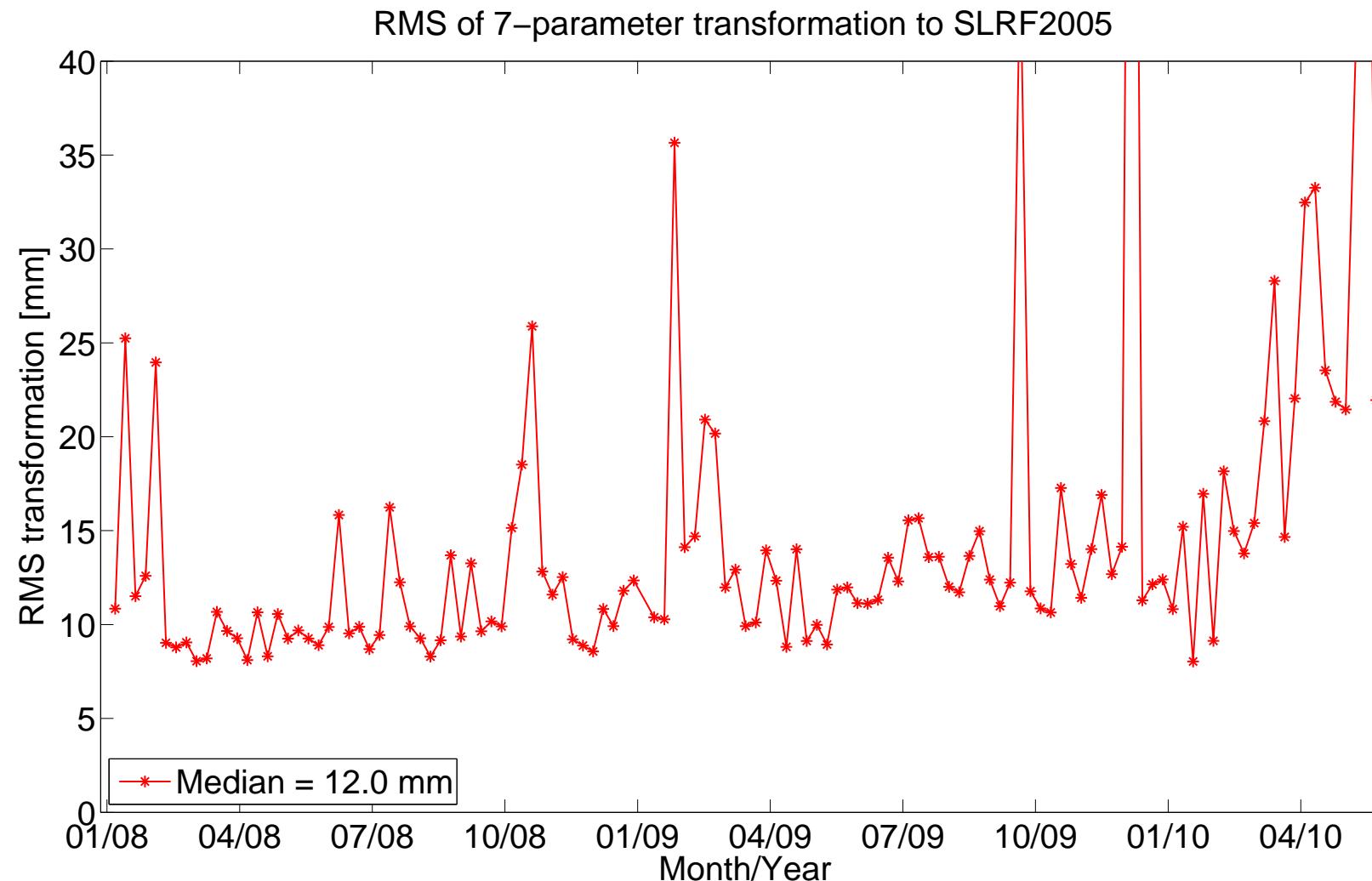
Manuela Seitz

# Danke für die Aufmerksamkeit !



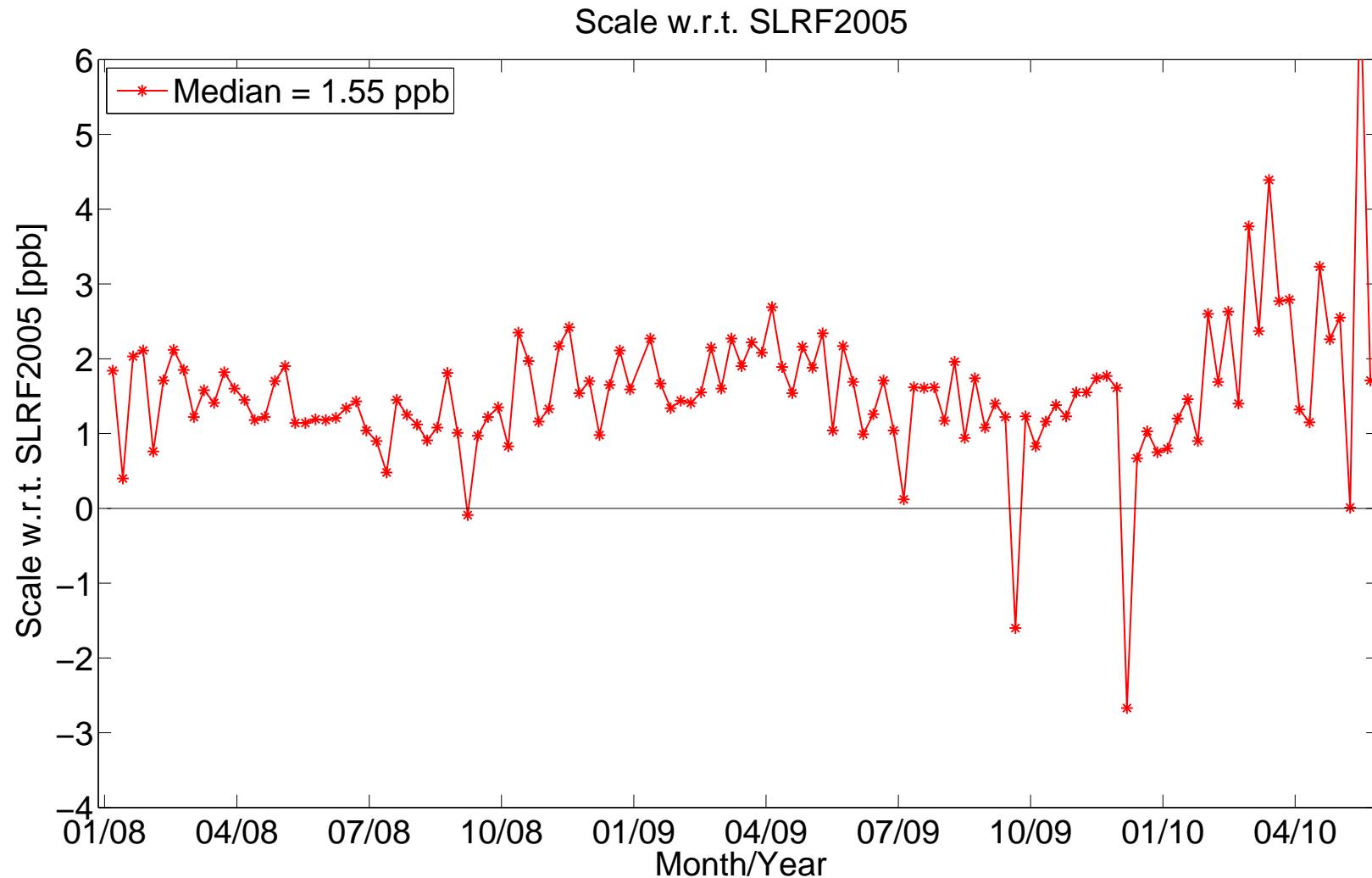
# Weekly LAGEOS solutions

Station coordinates: 7-parameter **Helmert transformation** w.r.t. SLRF2005  
**RMS** of transformation (weighting not considered!)



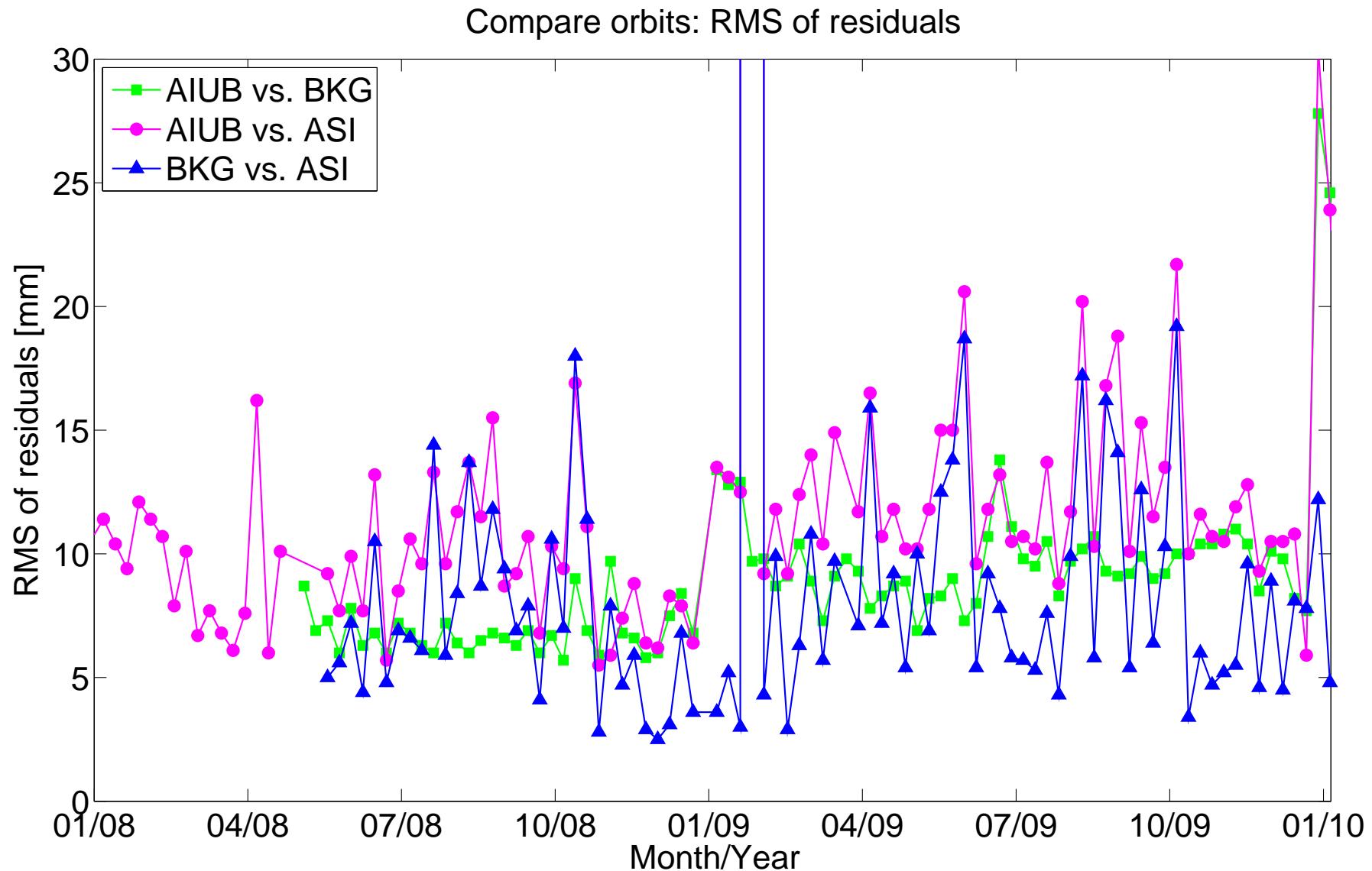
# Weekly LAGEOS solutions

Station coordinates: 7-parameter **Helmert transformation** w.r.t. SLRF2005



# Weekly LAGEOS solutions

Orbit comparison with other ILRS analysis centers



# Kombination von GNSS und SLR

## GNSS

$$L_A^S = \left| \begin{array}{cc} \mathbf{R}_{\text{EOP}} \cdot \mathbf{r}_A(t_A) & -\mathbf{r}^S(t_A - \tau_A^S) \end{array} \right| + \delta\rho_{trop(MW),A} + \delta\rho_{ion,A} + c \cdot \delta t_A + \delta\rho_{rel} - c \cdot \delta t^S + \lambda \cdot N_A^S \\ + \delta\rho_{phas} \\ + \delta\rho_{mult} \\ + \mathcal{E}_A^S \end{math>$$

## SLR

$$\frac{1}{2} \cdot c \cdot \tau_A^S = \left| \begin{array}{cc} \mathbf{R}_{\text{EOP}} \cdot \mathbf{r}_A(t^S) & -\mathbf{r}^S(t^S) \end{array} \right| + \delta\rho_{trop(opt)} + \delta\rho_{rel} + \delta\rho_{bias} + \delta\rho_{CoM} + \mathcal{E}_A^S$$

# Kombination von GNSS und SLR

GNSS

$$L_A^S = \left| \mathbf{R}_{\text{EOP}} \cdot \mathbf{r}_A(t_A) - \mathbf{r}^S(t_A - \tau_A^S) \right| + \delta\rho_{trop(MW),A} + \delta\rho_{ion,A} + c \cdot \delta t_A + \delta\rho_{rel} - c \cdot \delta t^S + \lambda \cdot N_A^S + \delta\rho_{phas} + \delta\rho_{mult} + \mathcal{E}_A^S$$

SLR

$$\frac{1}{2} \cdot c \cdot \tau_A^S = \left| \mathbf{R}_{\text{EOP}} \cdot \mathbf{r}_A(t^S) - \mathbf{r}^S(t^S) \right| + \delta\rho_{trop(opt)} + \delta\rho_{rel} + \delta\rho_{bias} + \delta\rho_{CoM} + \mathcal{E}_A^S$$

EOP:  
Pol, UT, Nutation

TRF

Satellite orbit