

GPS- and VLBI-derived Subdaily Estimates of Earth's Rotation and Their Impact on Global Solutions



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Introduction

- Subdaily variations of Earth's rotation are usually accounted for with the model recommended by the IERS Conventions 2003
- Studies of subdaily Earth rotation variations with GPS and VLBI have been carried out since more than a decade
- Study the impact of introducing GPS- and VLBI-derived subdaily ERP models in global solutions

Outline

- Estimation and comparison of subdaily ERP models from GPS and VLBI time series
- Impact of sideband constraints and a priori models
- Impact of different a priori subdaily ERP models on global GPS and VLBI solutions

Subdaily GPS and VLBI Solutions

GPS

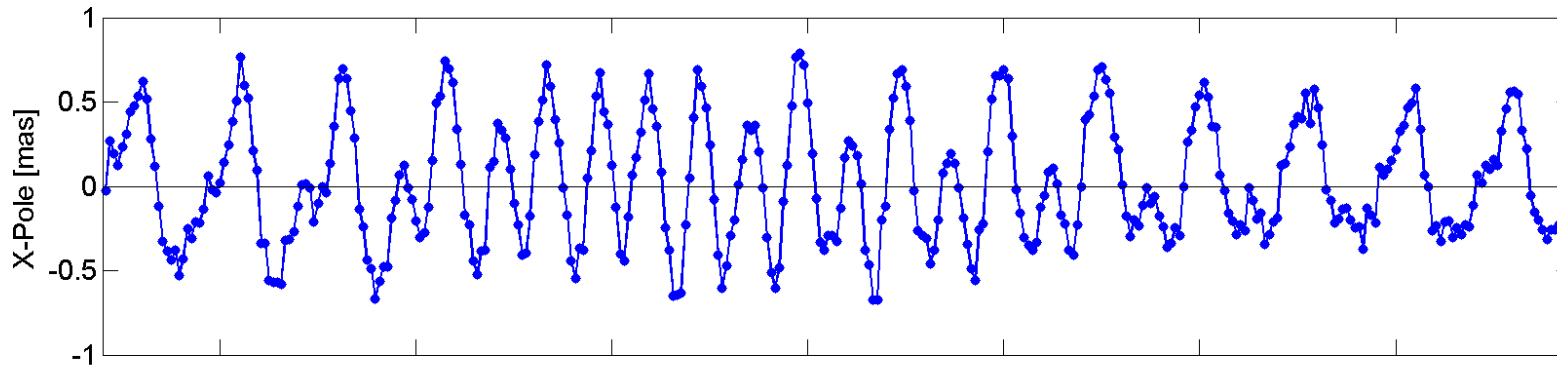
- Bernese GPS Software
- 3-day orbital arcs
- diurnal retrograde polar motion blocked

VLBI

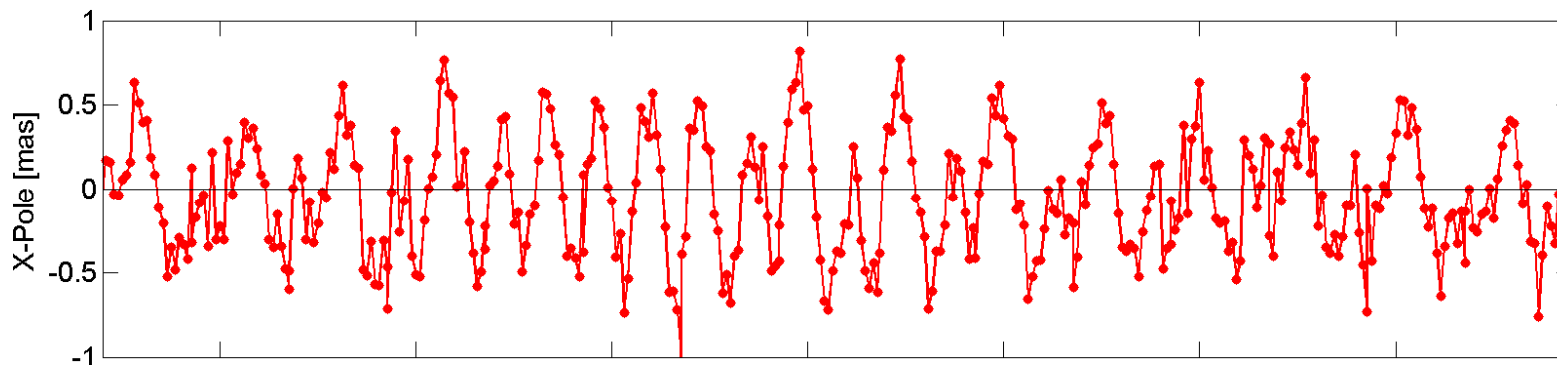
- CALC/SOLVE
- nutation fixed to IVS quarterly solution IVS09q2e

Solution	Technique	Resolution	Time period
TUM08	GPS	2h	Jan 1994 – Dec 2007
COD09	GPS	1h	Jan 1994 – Dec 2008
IGG09	VLBI	1h	Mar 1984 – Dec 2008
TUM08C	GPS/VLBI	2h/1h	Apr 1980 – Dec 2007

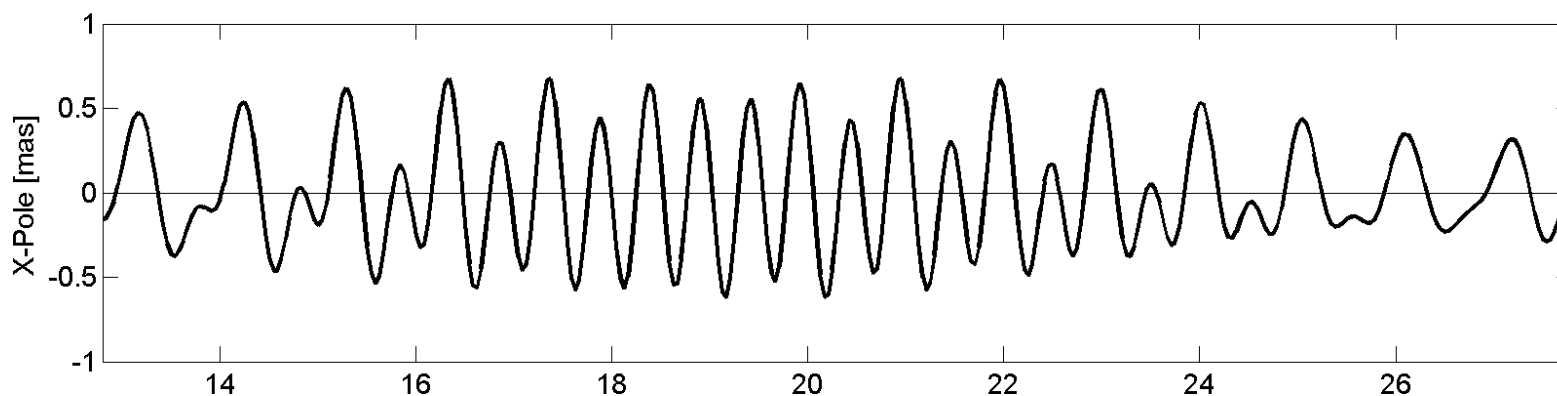
Subdaily GPS and VLBI Solutions: CONT05



**GPS
COD09**



**VLBI
IGG09**

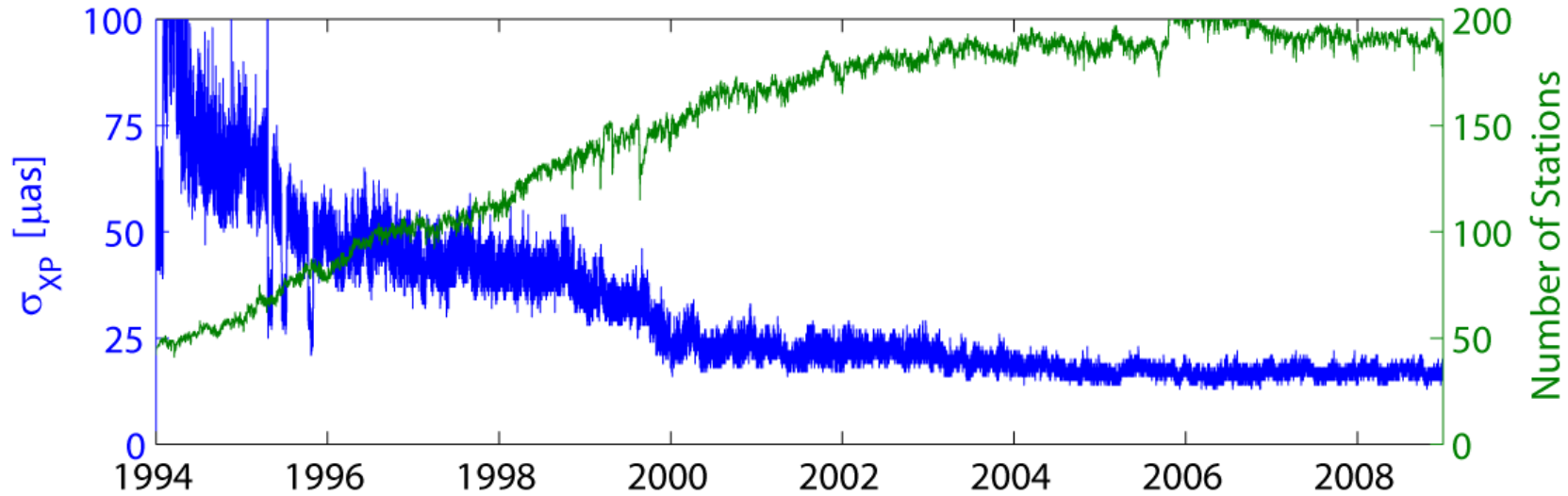


IERS2003

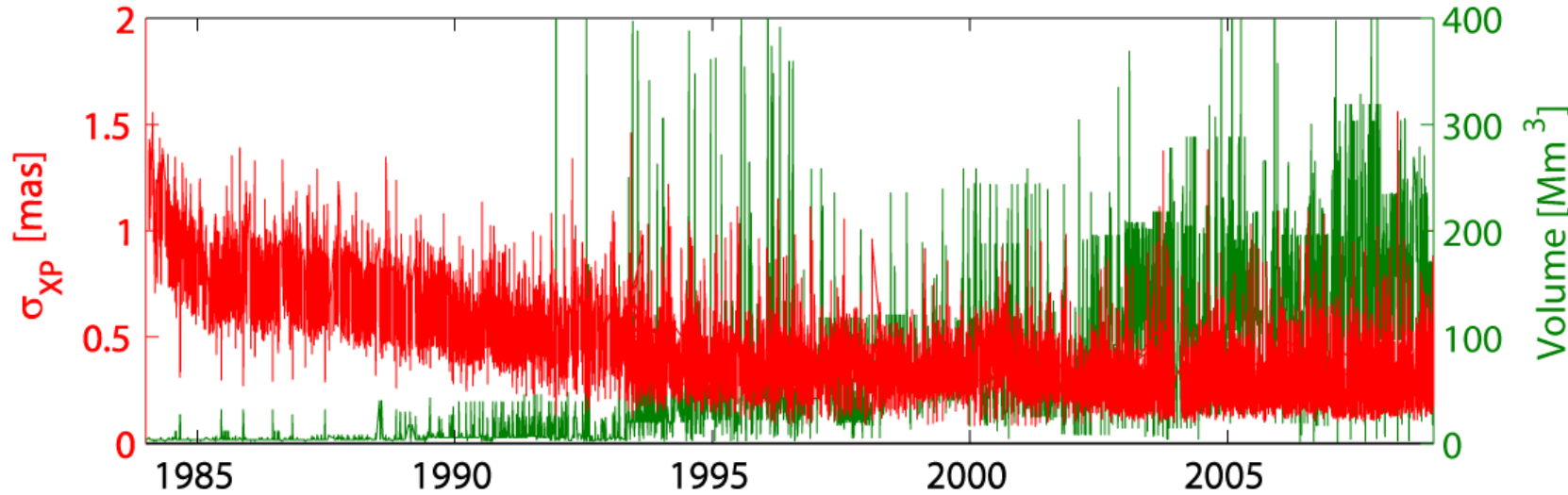
September 2005

Formal Errors X-Pole

GPS
 $\sigma=30 \mu\text{as}$



VBLI
 $\sigma=0.37 \text{ mas}$



Estimation of Subdaily ERP Models

- Estimation of **57 polar motion** and **41 UT1** ocean tidal amplitudes in a weighted least squares adjustment

$$\Delta X(t) = \sum_{j=1}^n \left[-p_j^c \cos \psi_j(t) + p_j^s \sin \psi_j(t) \right]$$

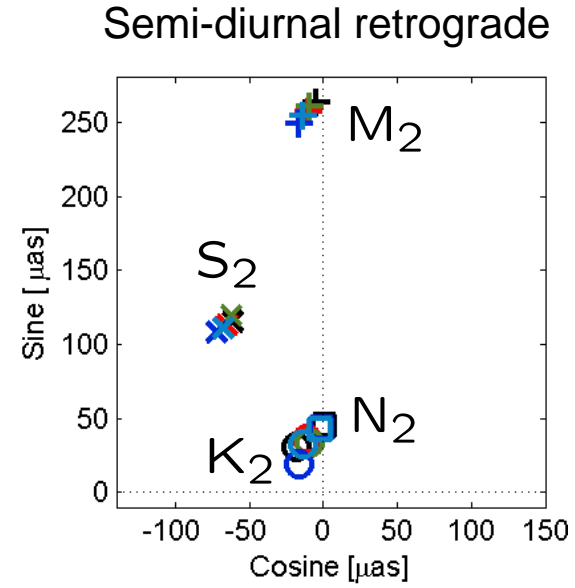
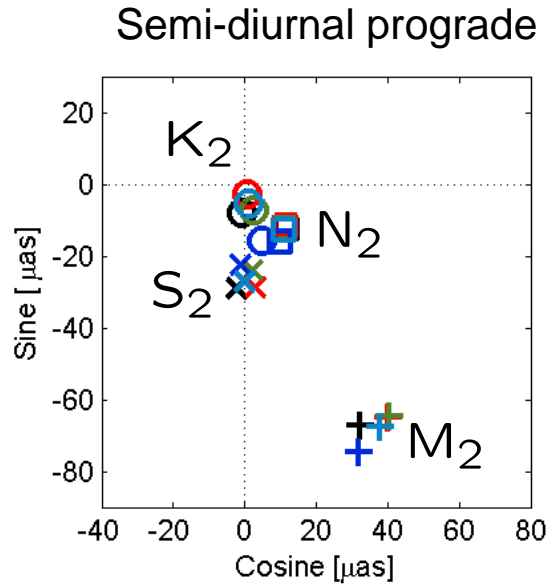
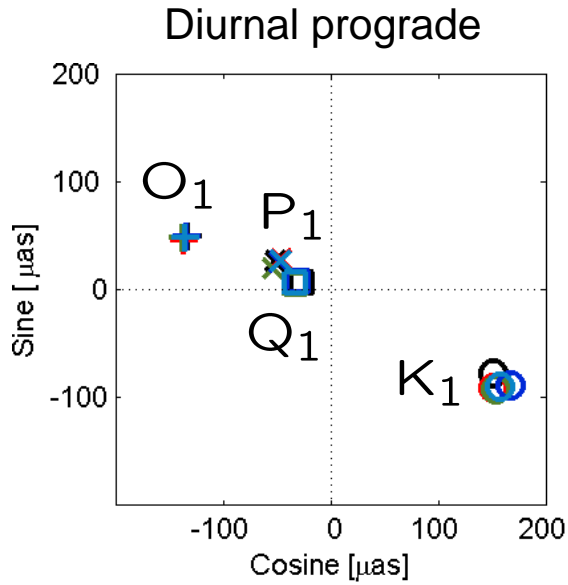
$$\Delta Y(t) = \sum_{j=1}^n \left[p_j^c \sin \psi_j(t) + p_j^s \cos \psi_j(t) \right]$$

$$\Delta UT1(t) = \sum_{j=1}^n \left[u_j^c \cos \psi_j(t) + u_j^s \sin \psi_j(t) \right]$$

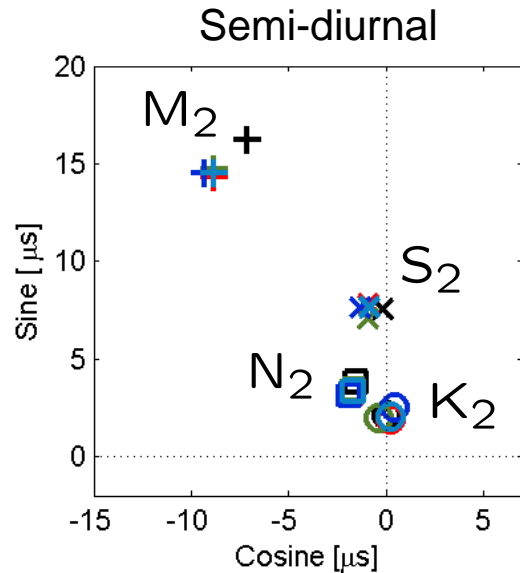
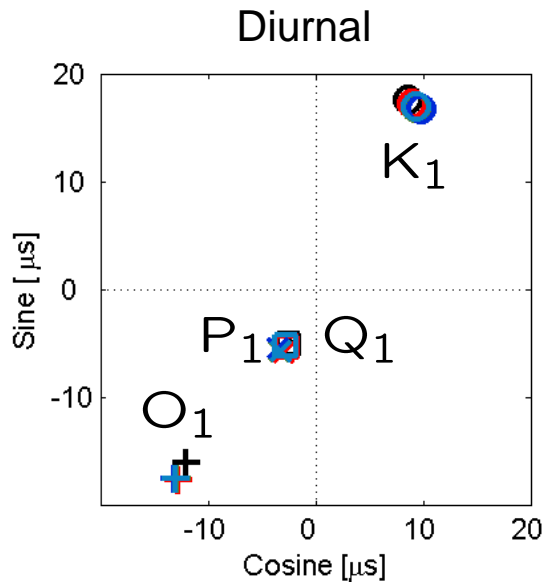
- Pseudo-observations:
 - GPS: **polar motion rates, length of day**
 - VLBI: **polar motion, UT1**
- **Constraints** for sidebands that cannot be solved for

Major Tidal Constituents

Polar Motion



UT1



TUM08

COD09

IGG09

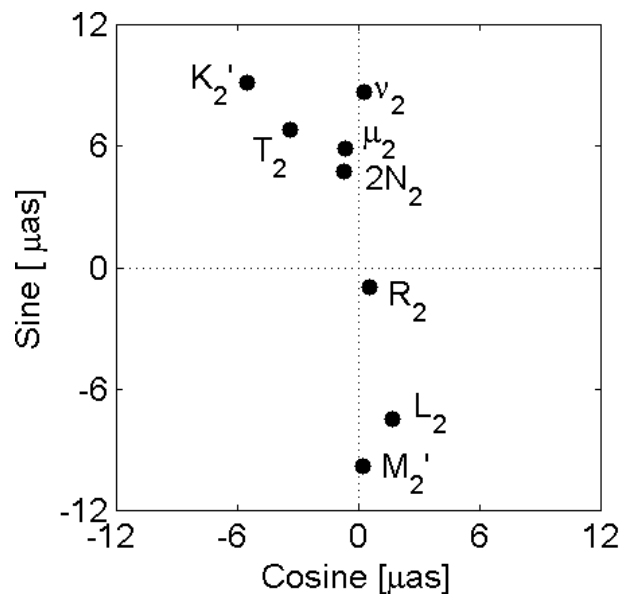
TUM08C

IERS2003

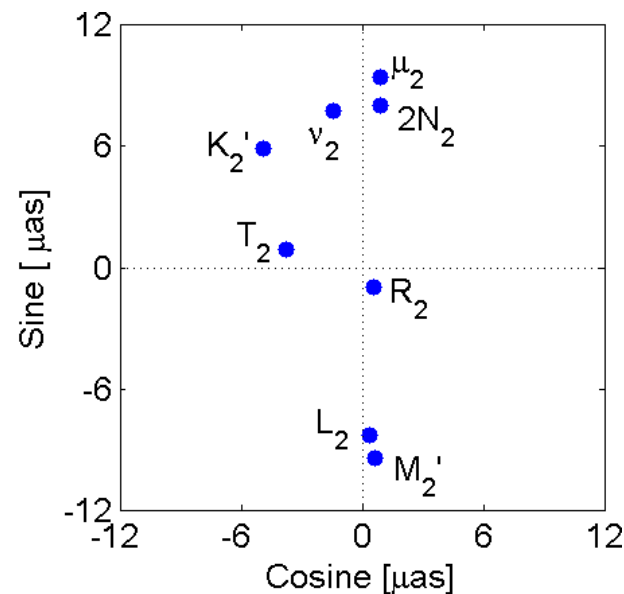


Small Tidal Constituents: Retrograde Polar Motion

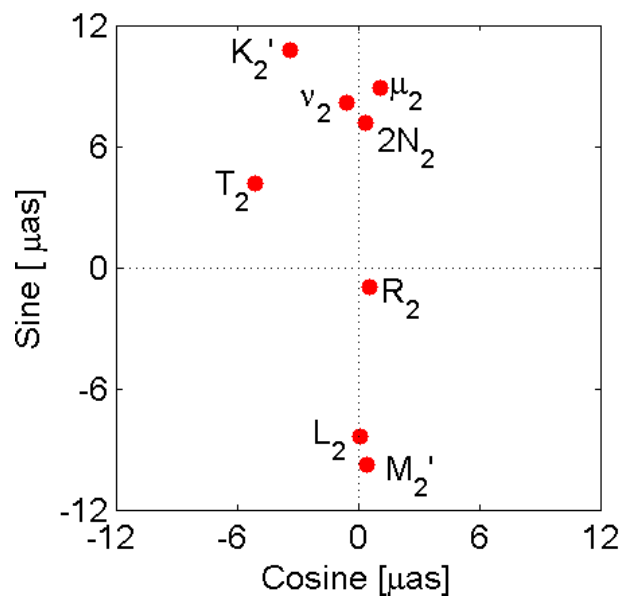
IERS2003



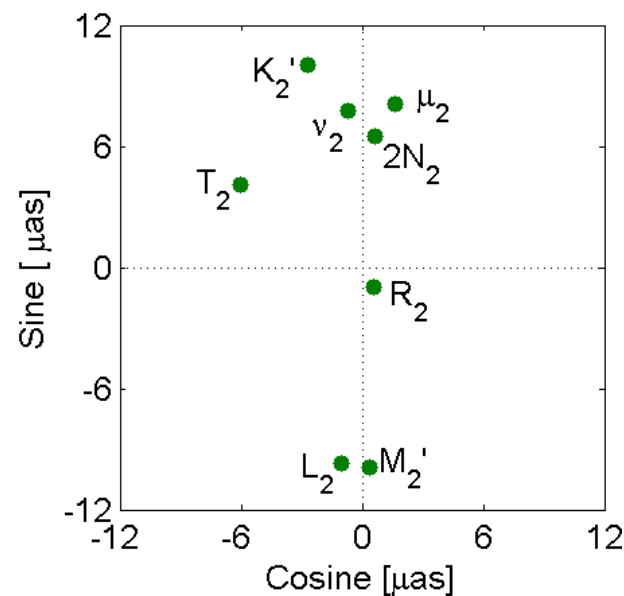
IGG09



TUM08

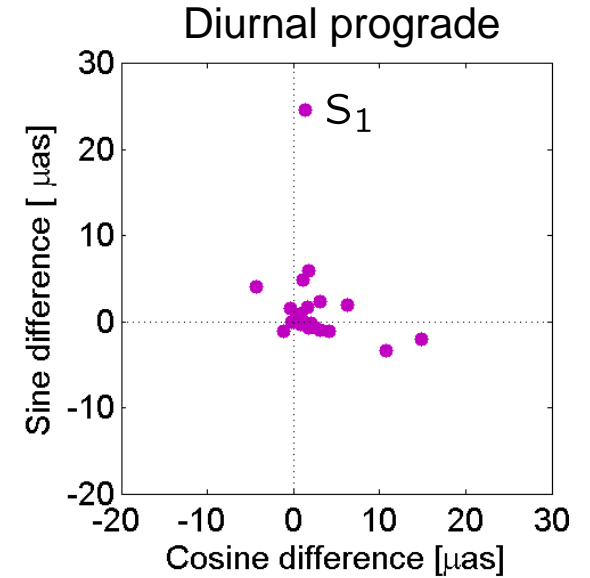
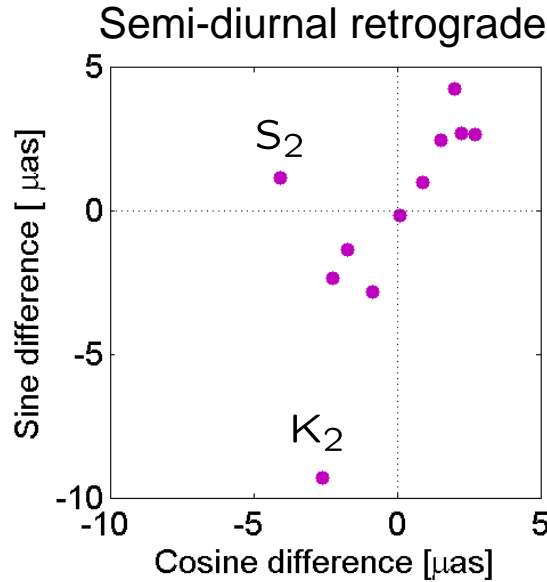
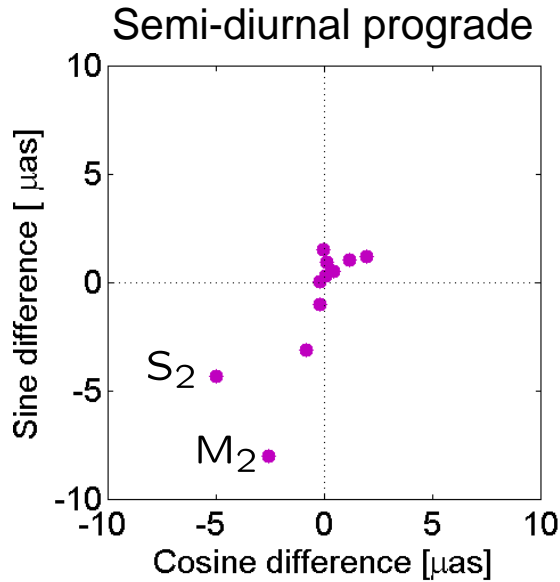


COD09

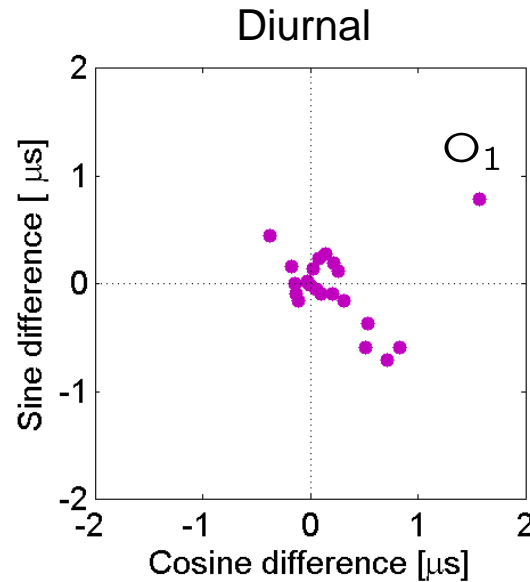
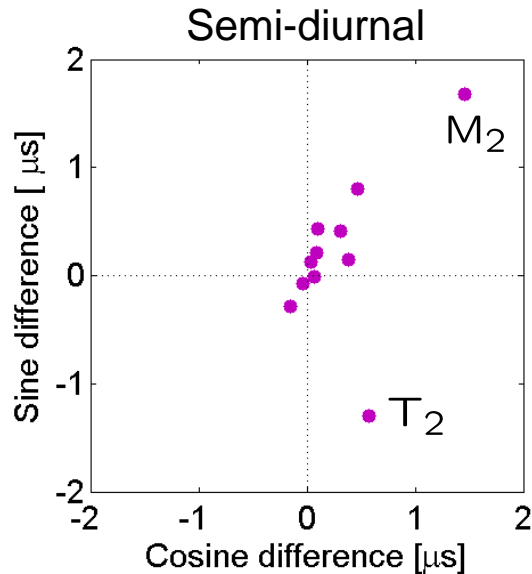


Differences of COD09 w.r.t. IERS2003

Polar Motion



UT1



Comparison of All Estimated Tidal Constituents

Mean **RMS** differences of estimated amplitudes

PM in μas	COD09	IGG09	TUM08C	IERS2003
TUM08	4.2	4.1	1.5	3.3
COD09		4.9	4.4	4.1
IGG09			2.9	4.3
TUM08C				3.2

UT1 in μs	COD09	IGG09	TUM08C	IERS2003
TUM08	0.28	0.30	0.14	0.48
COD09		0.35	0.28	0.49
IGG09			0.20	0.59
TUM08C				0.49

Sideband Constraints

A time series of at least 18.6 years is needed to properly solve for the sidebands of the tidal constituents

Constraints for the sideband amplitudes:

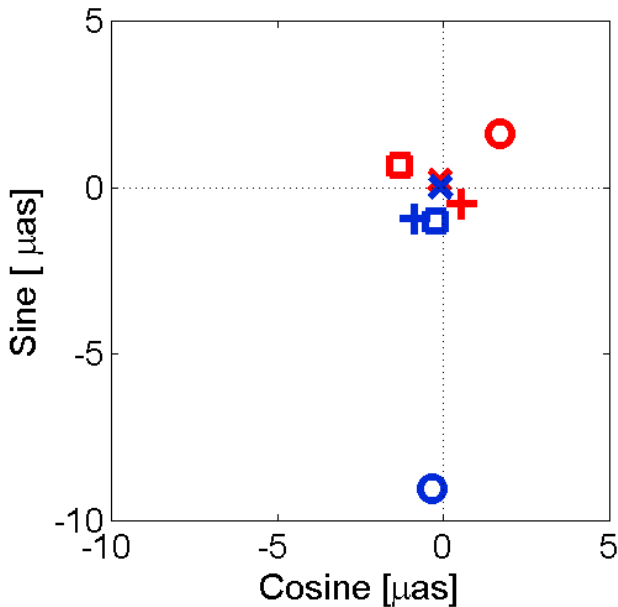
$$\frac{a_{j'}}{a_j} = \frac{h_{j'}}{h_j}$$

- a estimated subdaily ERP model coefficients
- h tide generating potential
- j tidal constituent
- j' corresponding sideband constituent

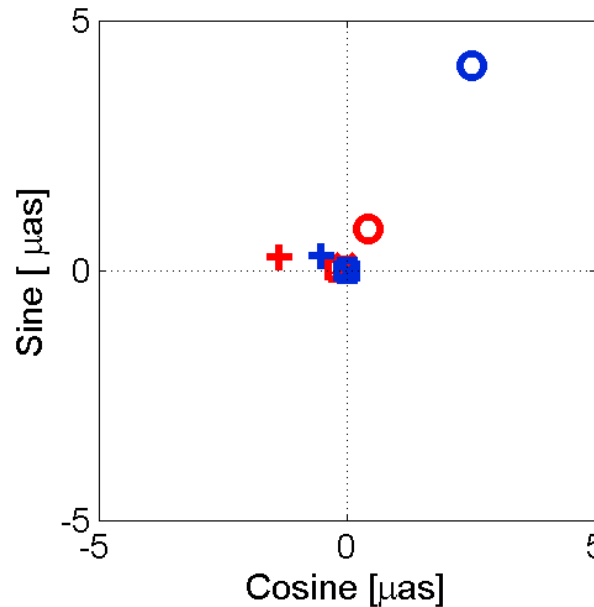
Impact of Sideband Constraints

Polar motion differences of **GPS** and **VLBI** models **with** and **without** sideband constraints

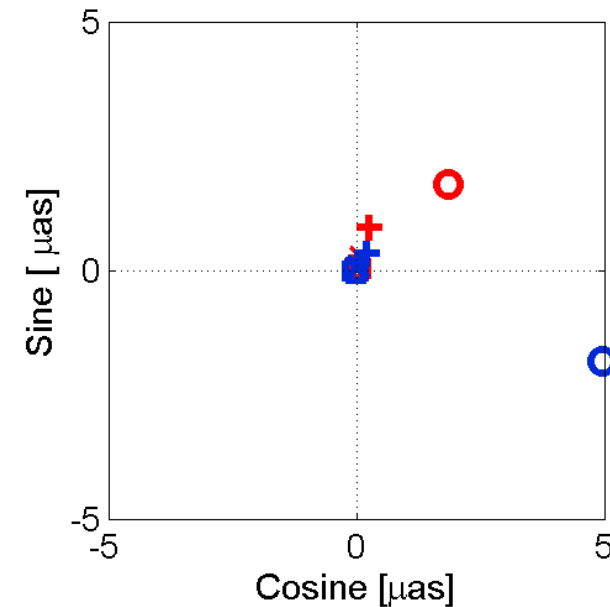
diurnal prograde



semidiurnal prograde



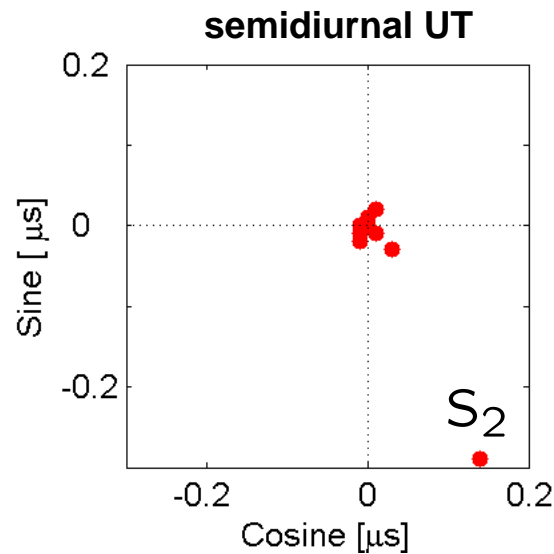
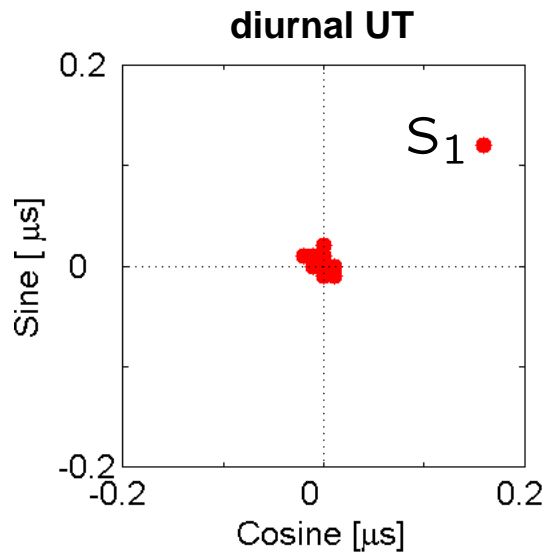
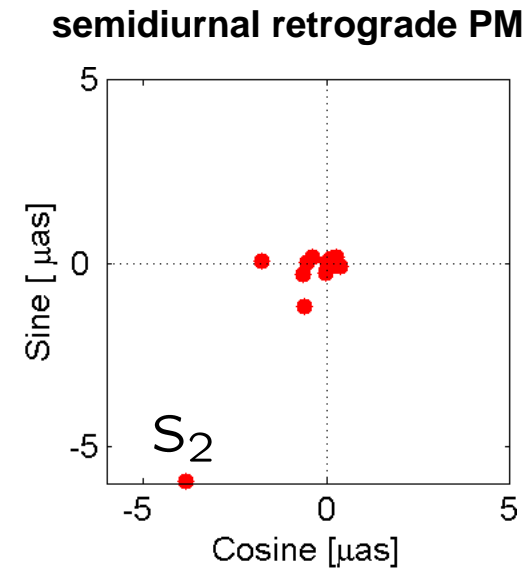
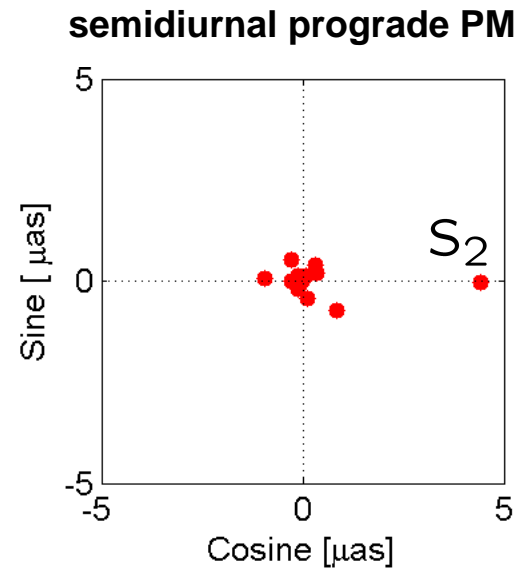
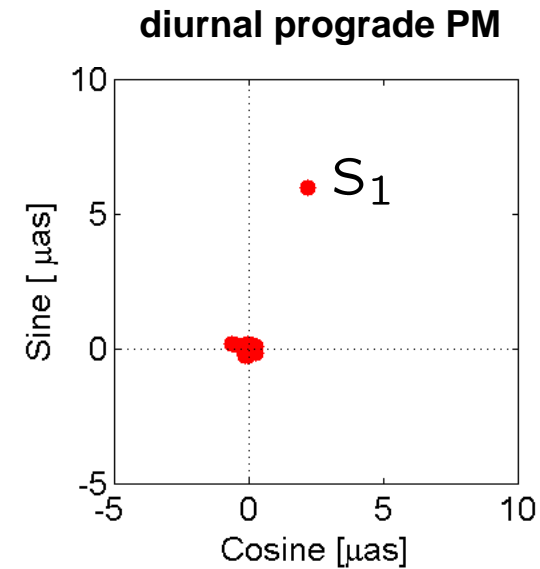
semidiurnal retrograde



\circ K_1 \times P_1 $+$ O_1 \square Q_1

\circ K_2 \times S_2 $+$ M_2 \square N_2

Impact of a Priori Models



Differences of
VLBI models
with IERS2003 and
GSFC hf1102a
a priori model

Impact on Global Solutions

Aliasing effects:

- 24 hours batches (GPS and VLBI)
- Orbit repeat period (GPS)

Global GPS and VLBI solutions with different subdaily a priori ERP models

GPS: Jan 2000 – Dec 2008

IERS2003	Reference solution
TUM08	GPS, 2h
COD09	GPS, 1h
IGG09	VLBI, 1h
TUM08C	GPS/VLBI, 2h/1h

VLBI: Mar 1984 – Dec 2008

IERS2003	Reference solution
IGG09	VLBI, 1h
hf1102a	GSFC model for CALC/SOLVE

Aliasing Effects

$$T_{\text{alias},j} = \frac{2\pi T}{|\Delta\phi_{\text{tide},j}|} \quad \Delta\phi_{\text{tide},j} = 2\pi \left[\frac{T}{T_{\text{tide},j}} - \text{NINT} \frac{T}{T_{\text{tide},j}} \right]$$

$T_{\text{alias},j}$ Alias period of tidal constituent j

$T_{\text{tide},j}$ Period of tidal constituent j

T 24^h or orbit repeat period of 23^h 56^m

24^h processing batches

Orbit repeat period

Tide j	$T_{\text{tide},j}$	$T_{\text{alias},j}$
M ₂	12.42 h	14.8 d
J ₁	23.10 h	25.6 d
P ₁	24.07 h	364.6 d

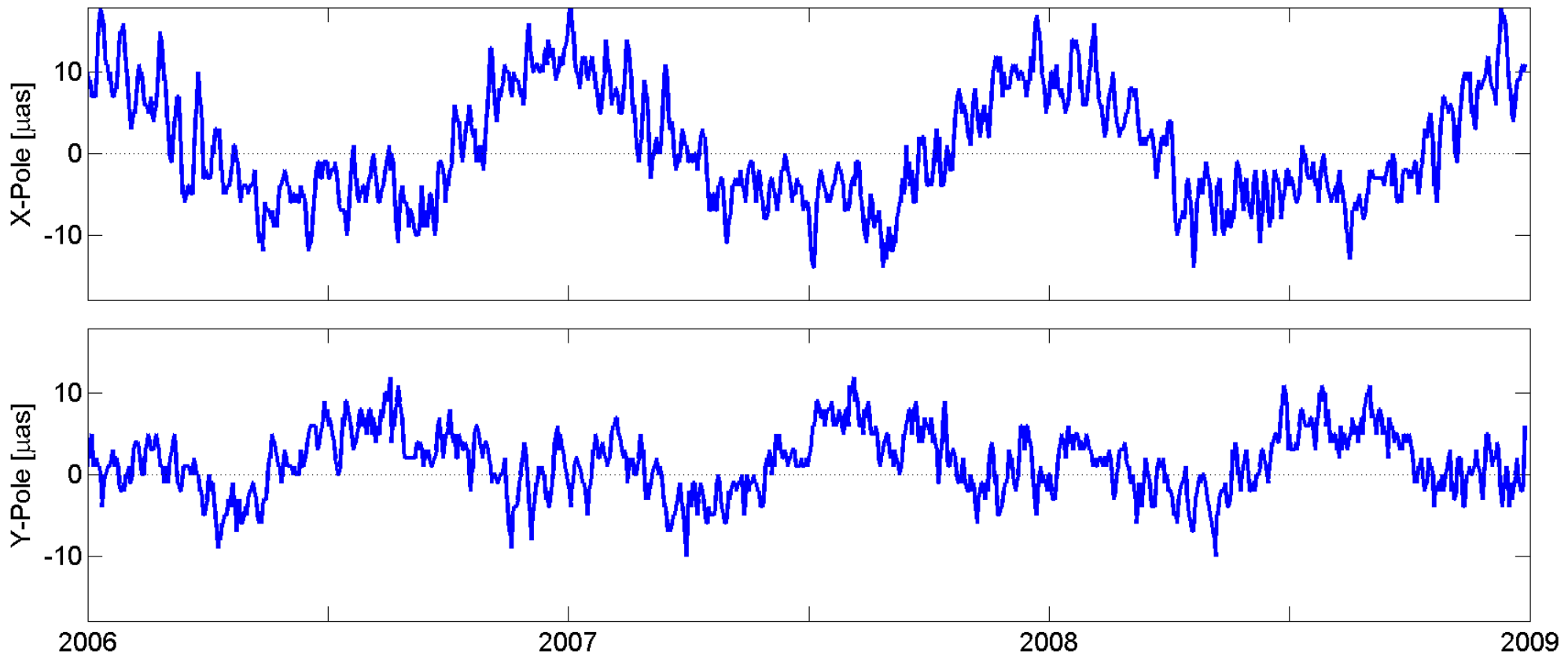
Tide j	$T_{\text{tide},j}$	$T_{\text{alias},j}$
M ₂	12.42 h	13.6 d
J ₁	23.10 h	27.6 d
P ₁	24.07 h	180.9 d

GPS Earth Rotation Parameters: IERS2003/COD09 (1)

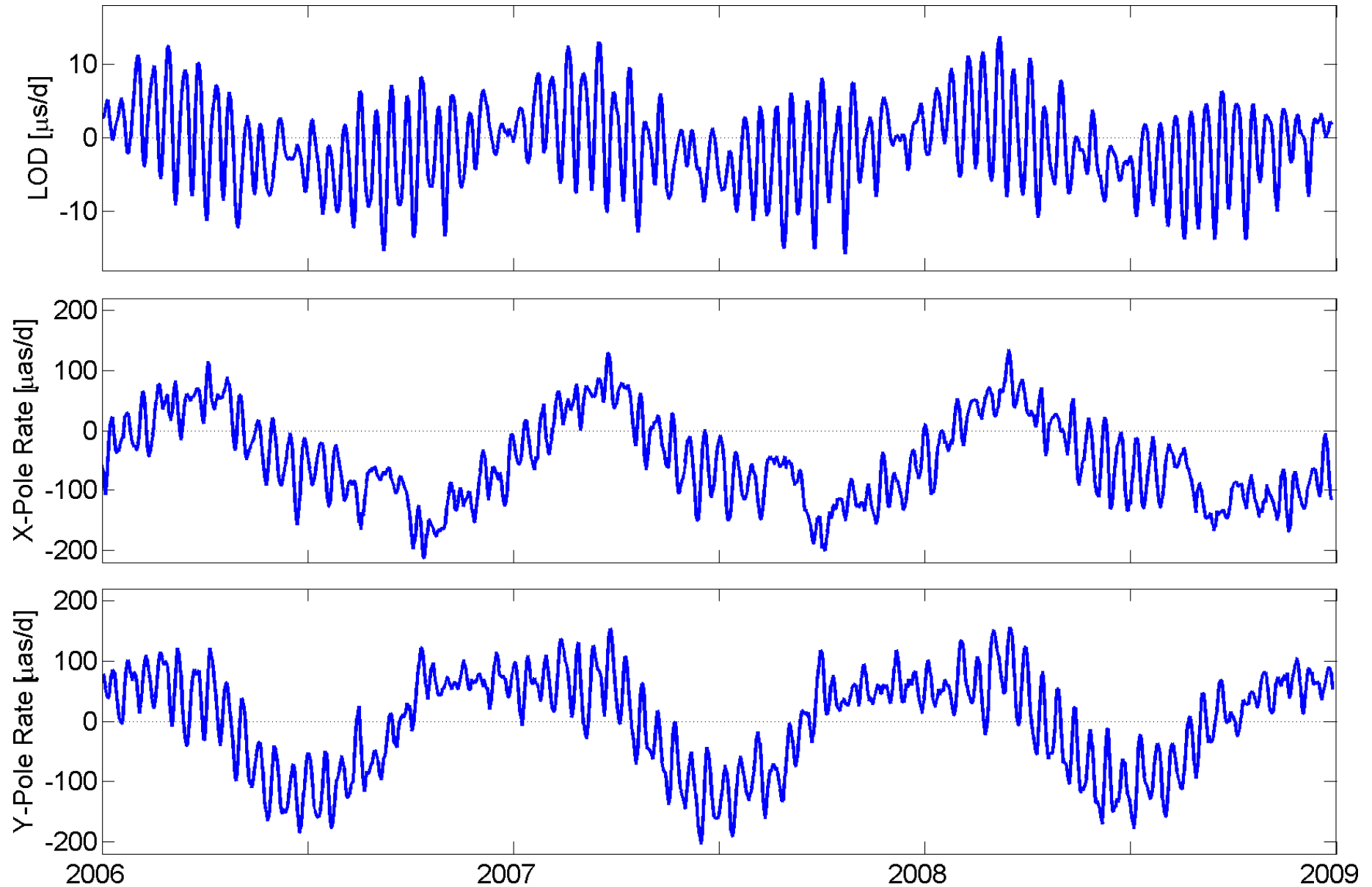
ERP difference time series of the GPS solutions IERS2003 and COD09

Estimated parameters per daily solution:

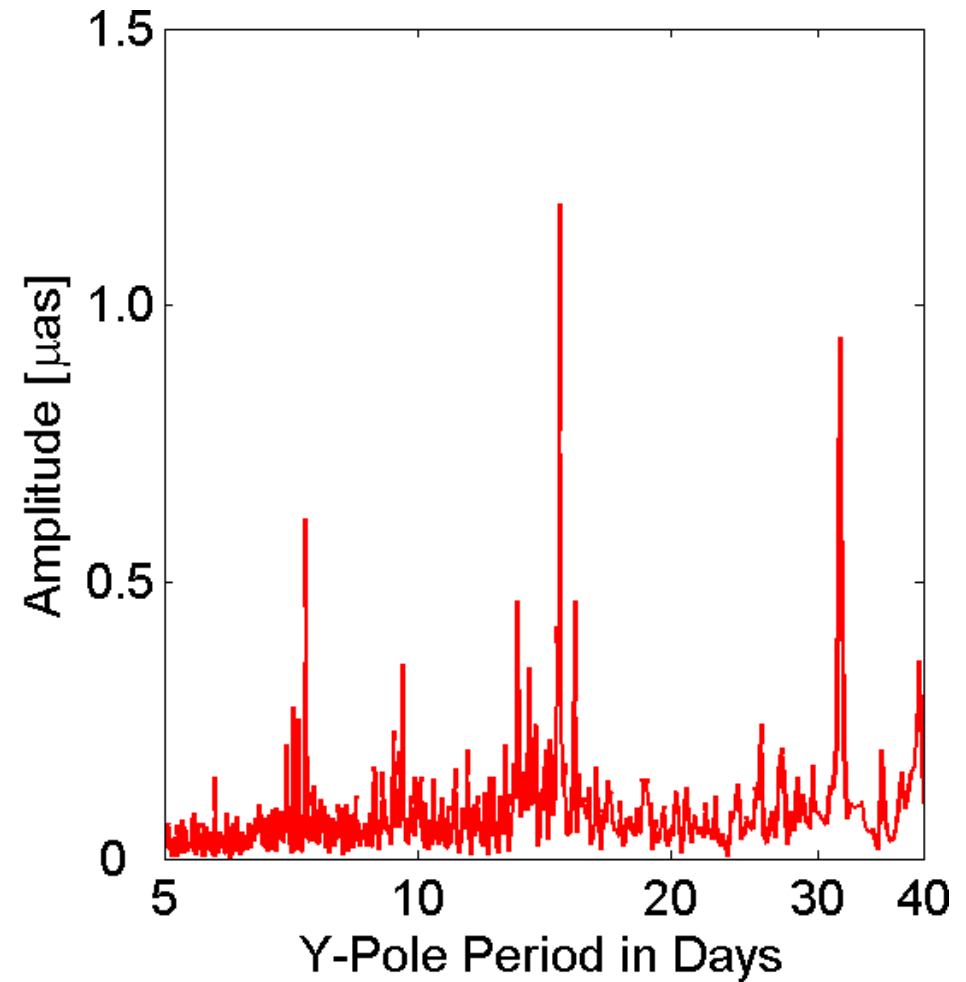
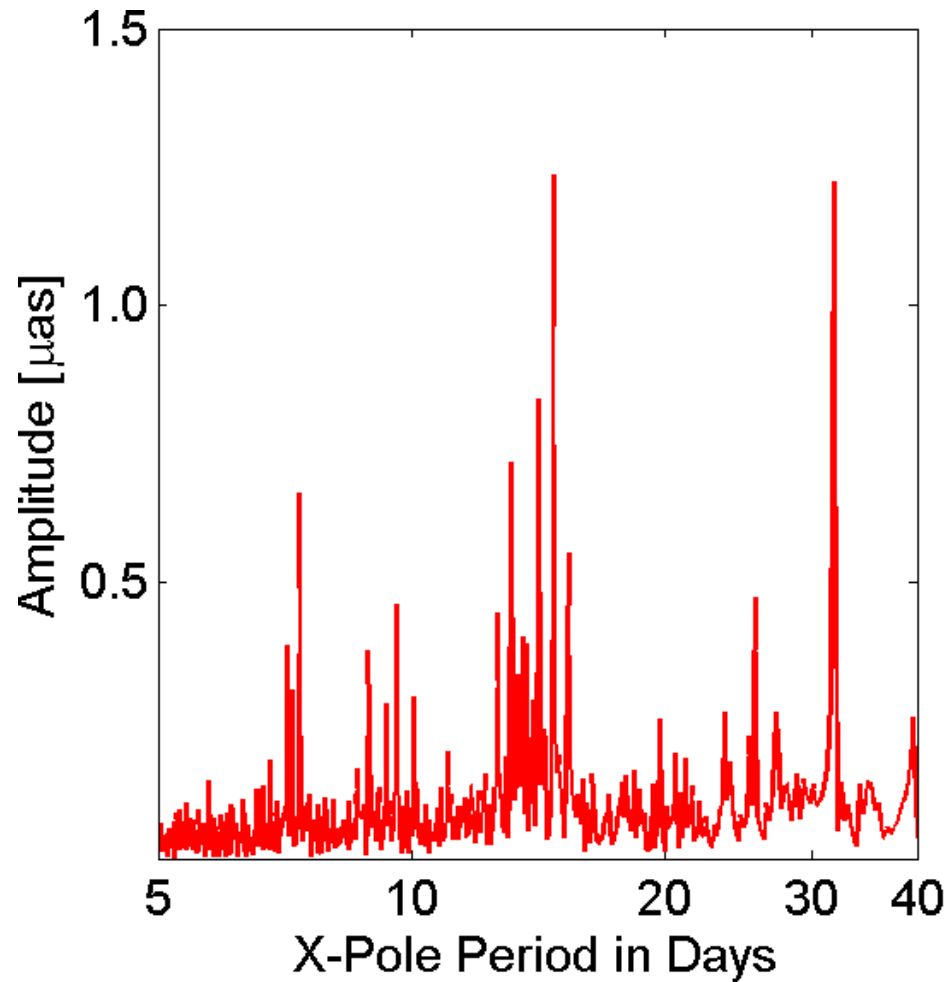
- Offset and rate for polar motion
- Rate for UT1 (= -LOD)



GPS Earth Rotation Parameters: IERS2003/COD09 (2)

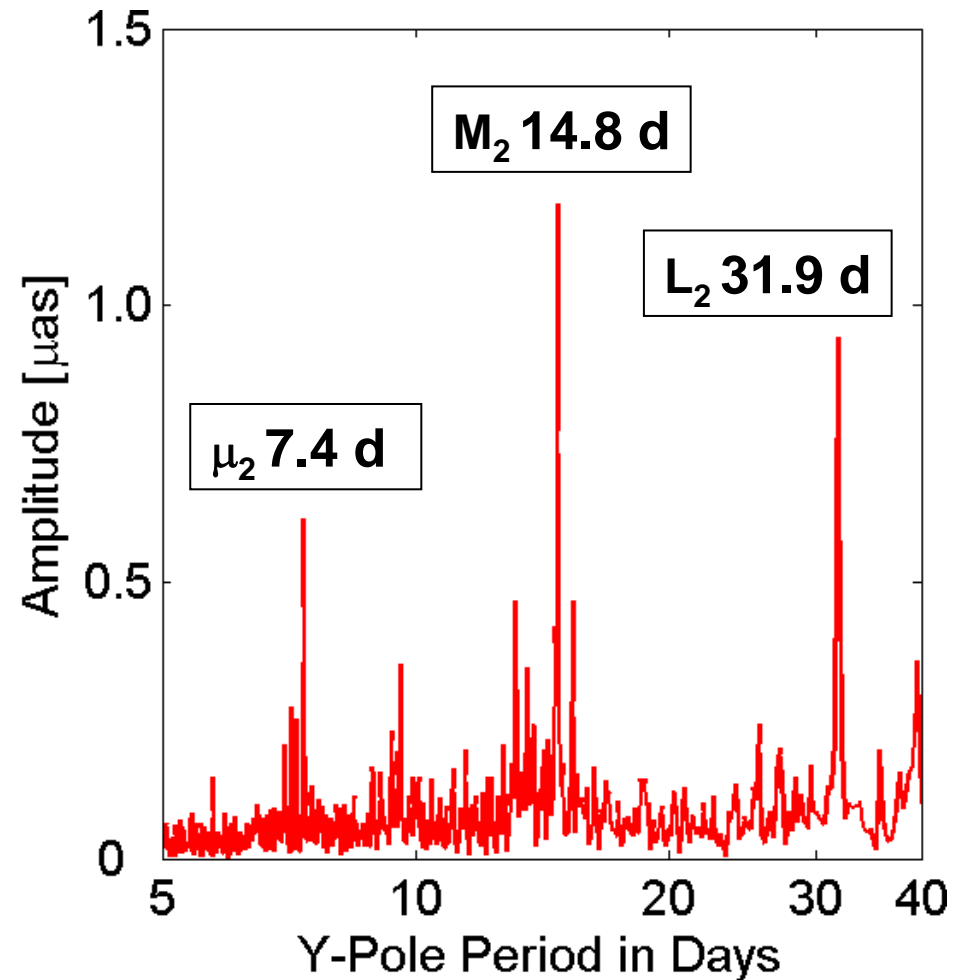
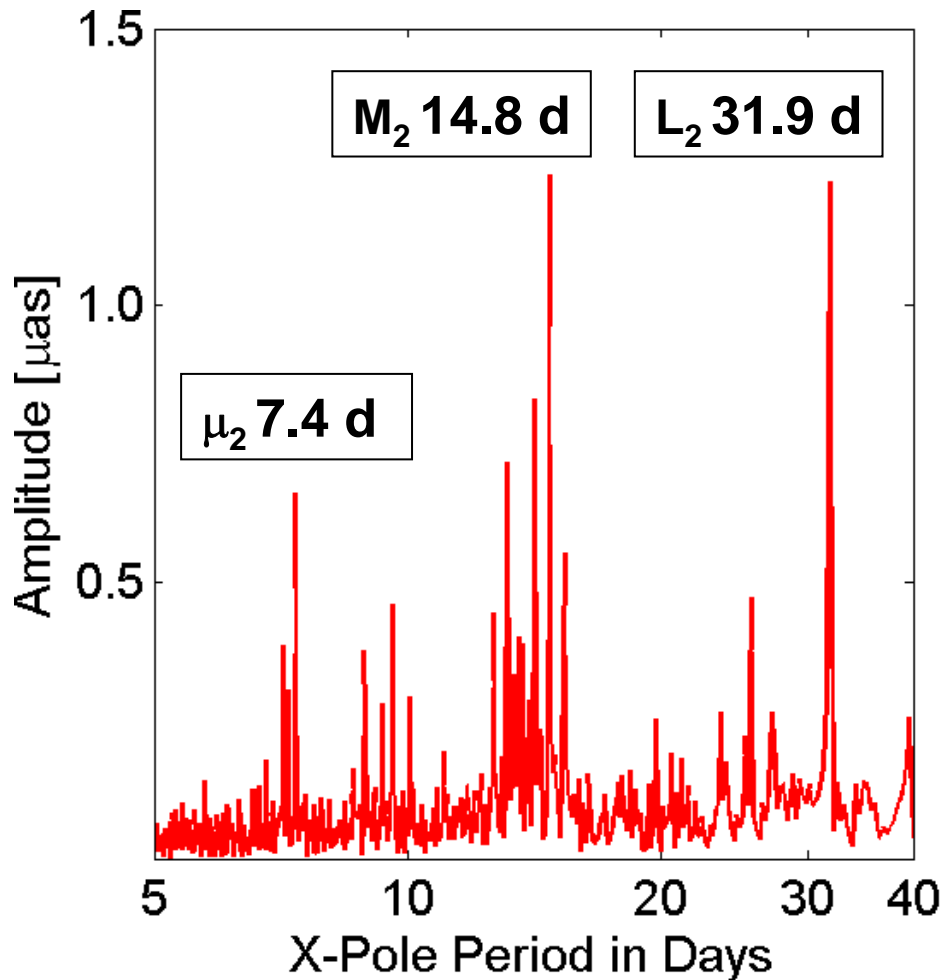


Spectra ERP Differences: IERS2003/COD09



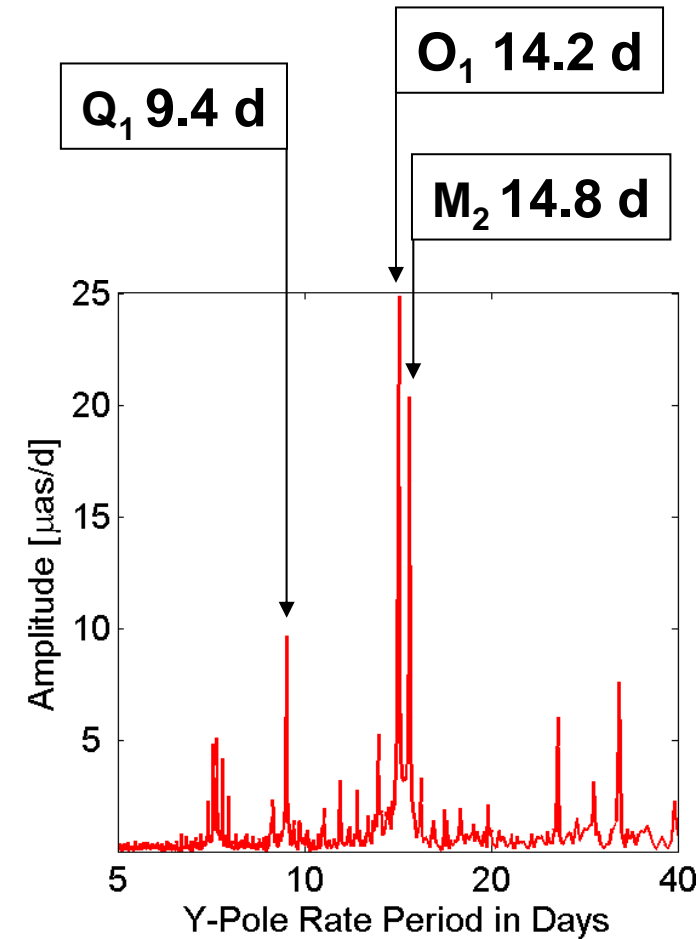
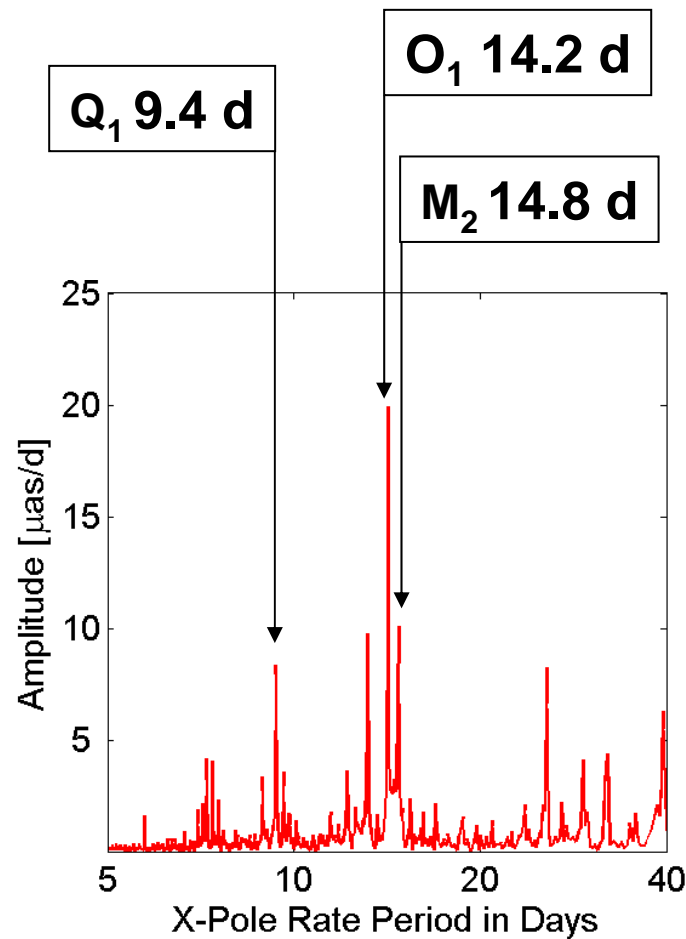
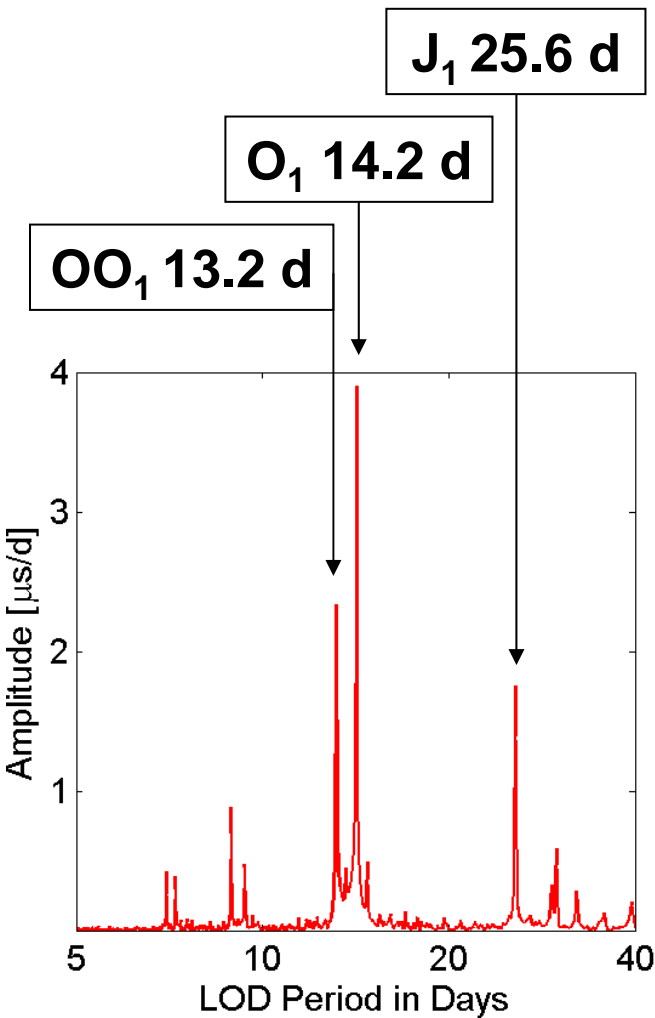
Spectra ERP Differences: IERS2003/COD09

Aliasing effects between 24 hours and ...

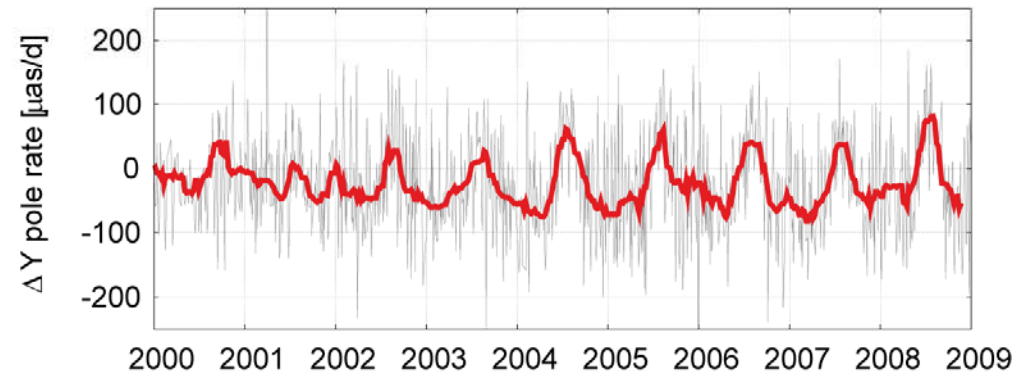
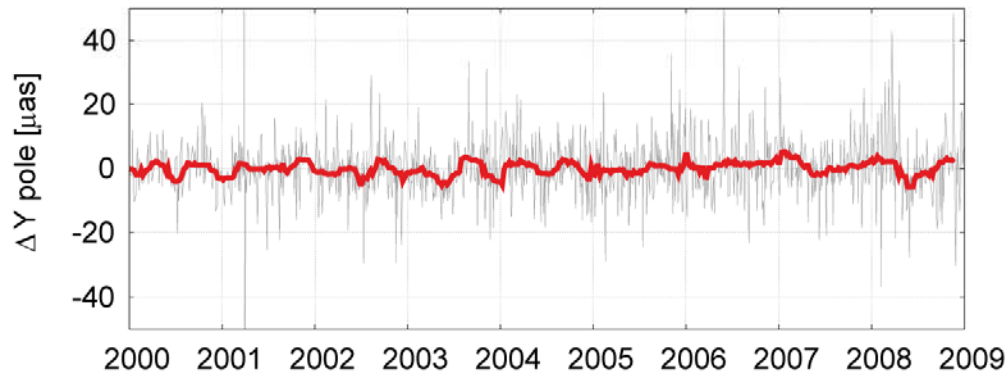
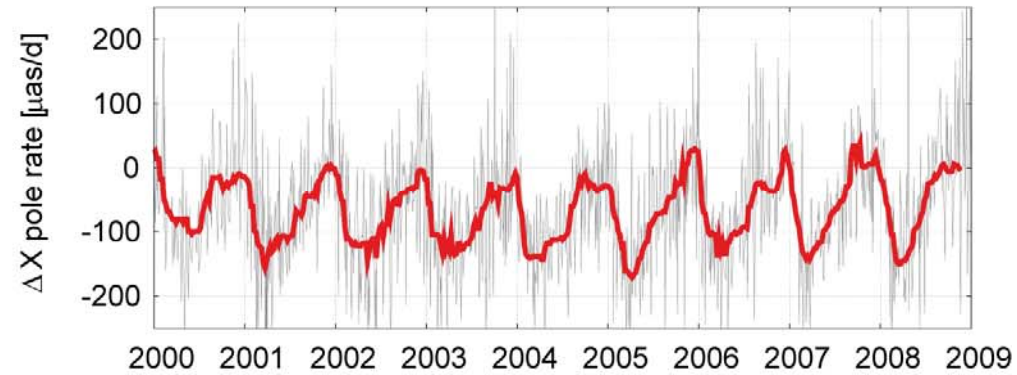
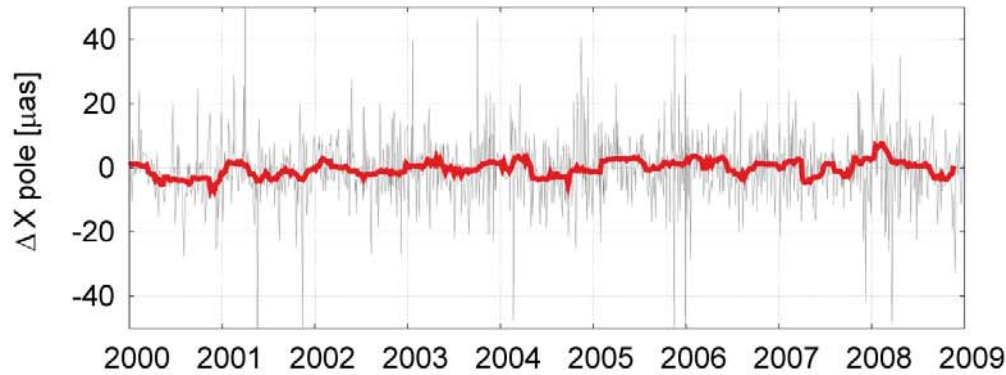
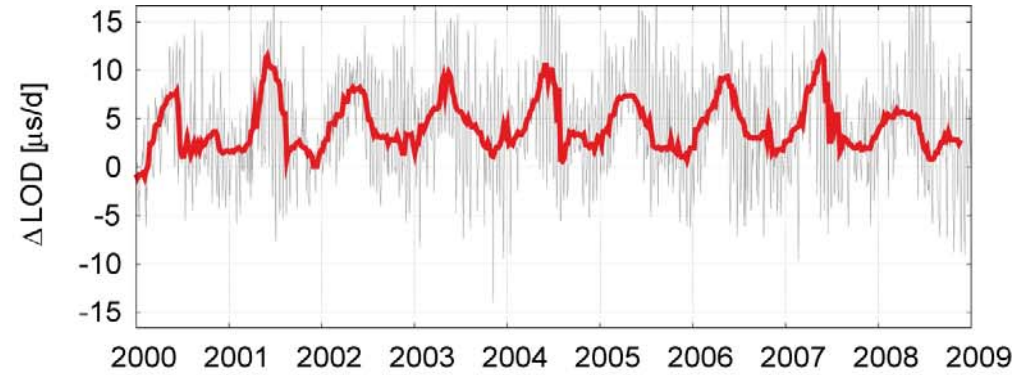
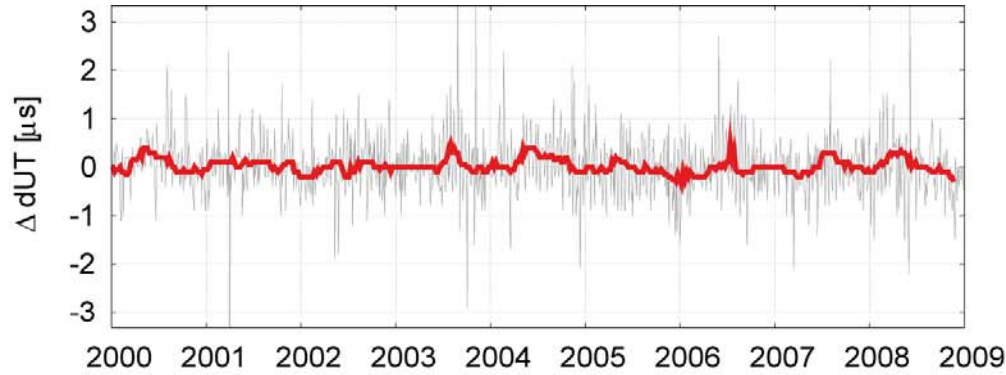


Spectra ERP Differences: IERS2003/COD09

Aliasing effects between 24 hours and ...

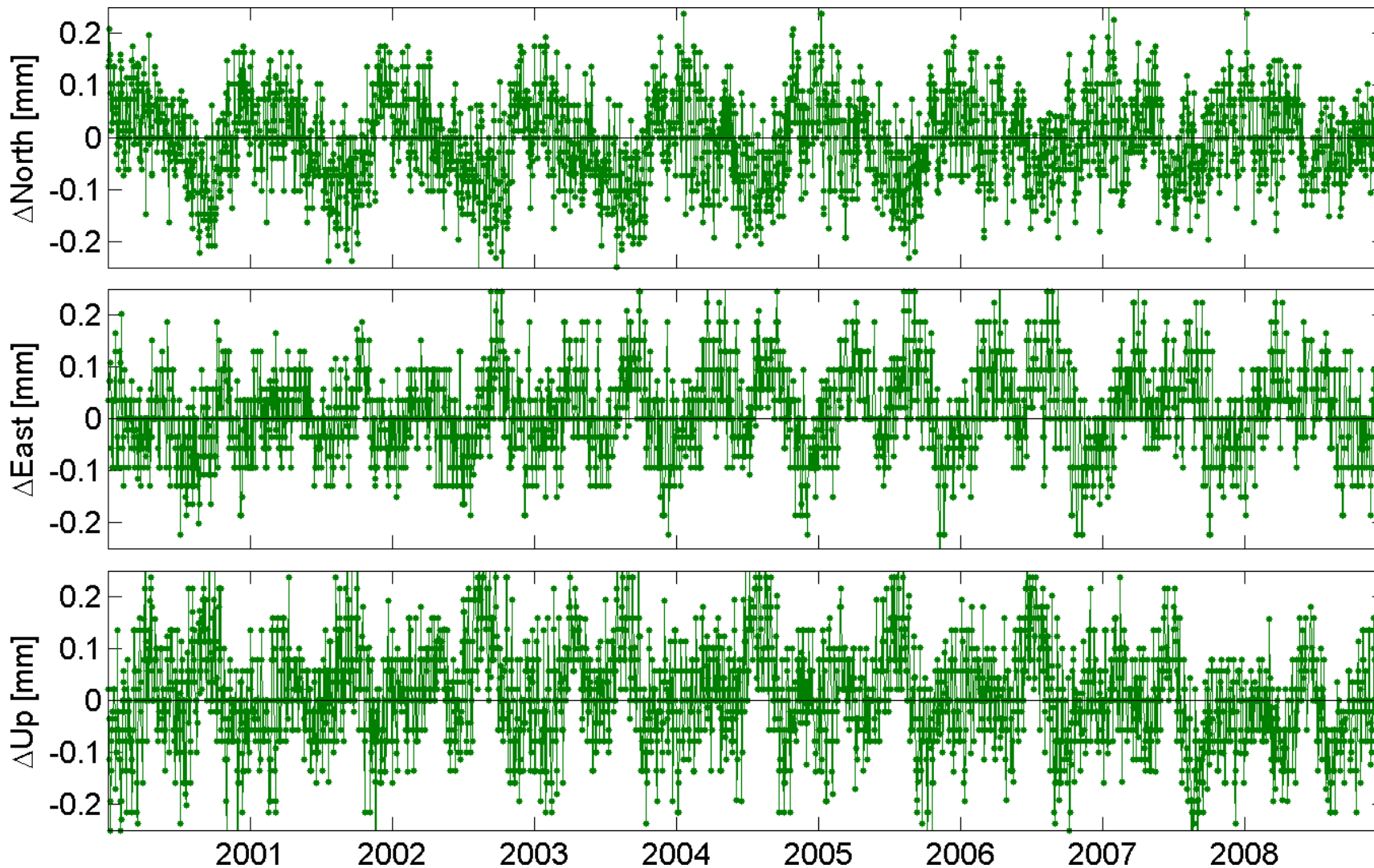


VLBI Earth Rotation Parameters: IERS2003/IGG09



GPS Station Coordinates: IERS2003/COD09

BOR1, Borowiec, Poland



STD_N
0.08 mm

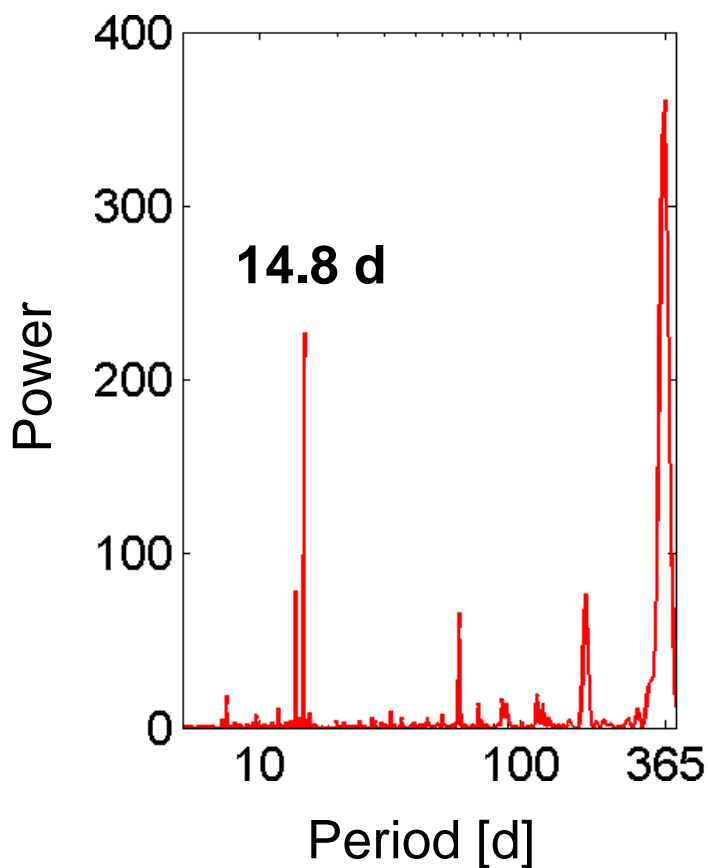
STD_E
0.08 mm

STD_U
0.10 mm

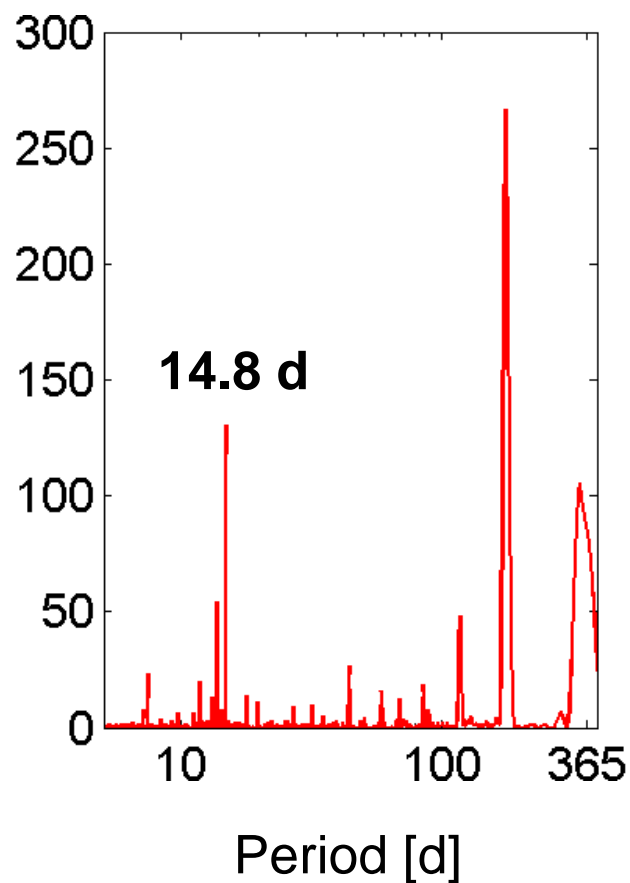
Spectra Coordinates Differences: IERS2003/COD09

BOR1, Borowiec, Poland

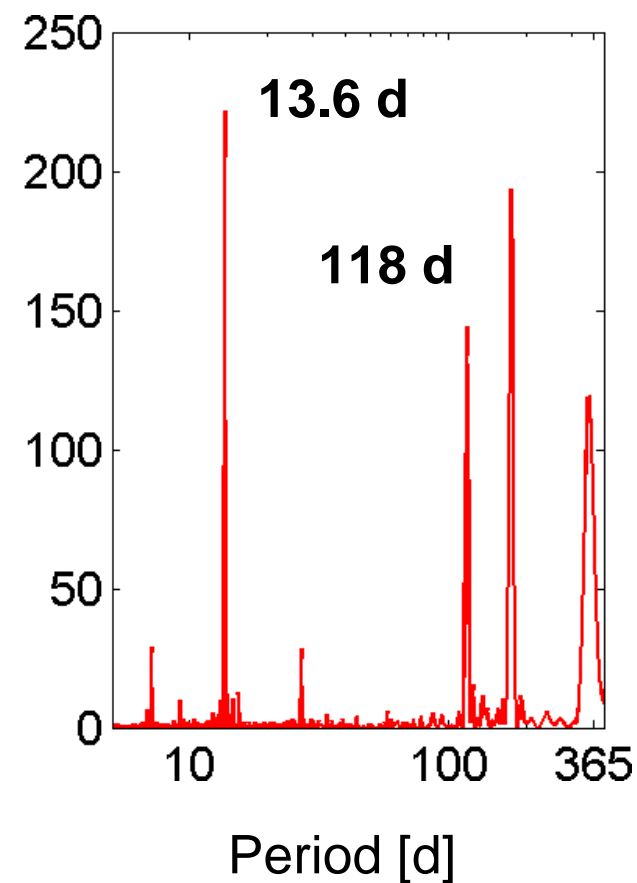
Δ North



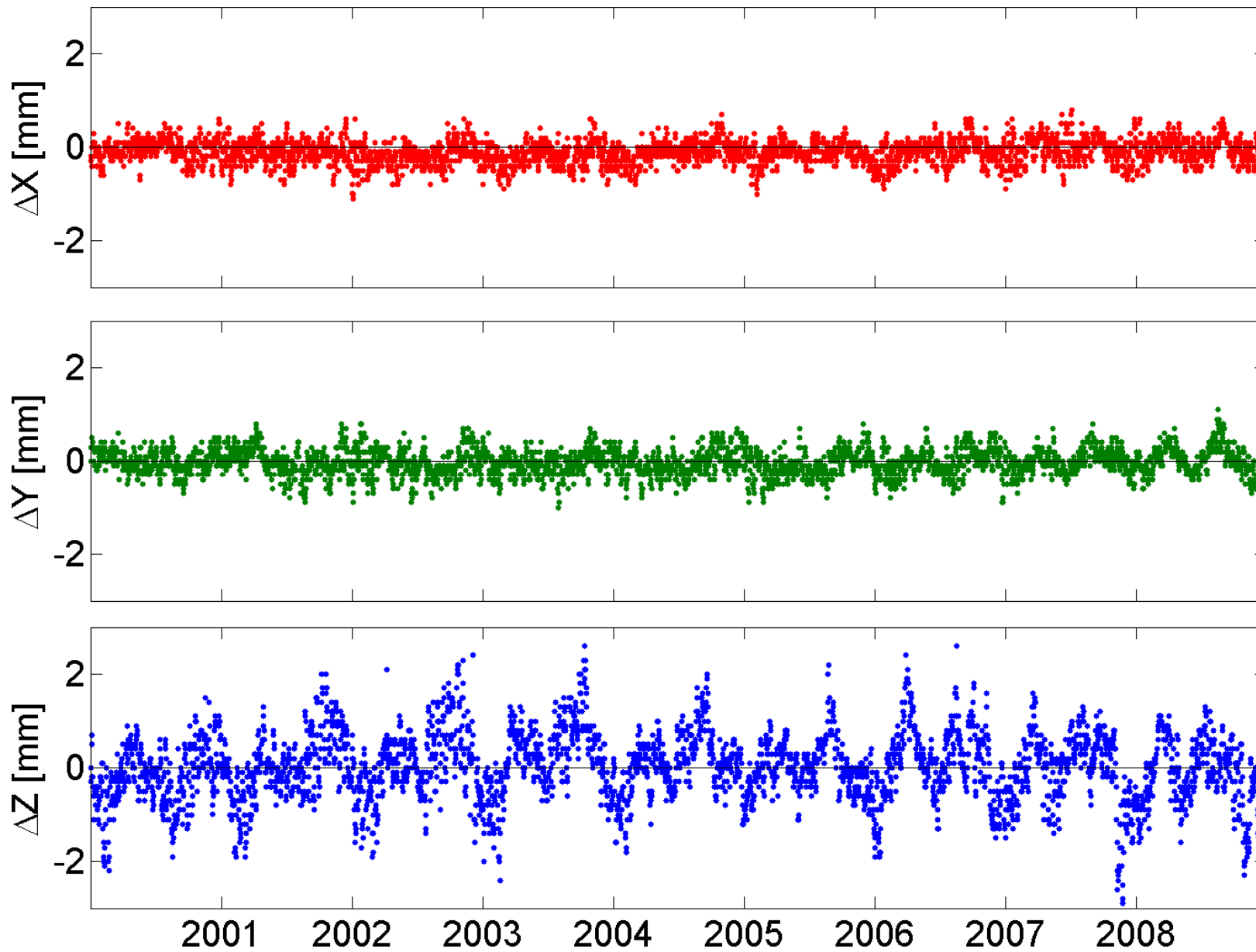
Δ East



Δ Up



GPS Geocenter: IERS2003/COD09

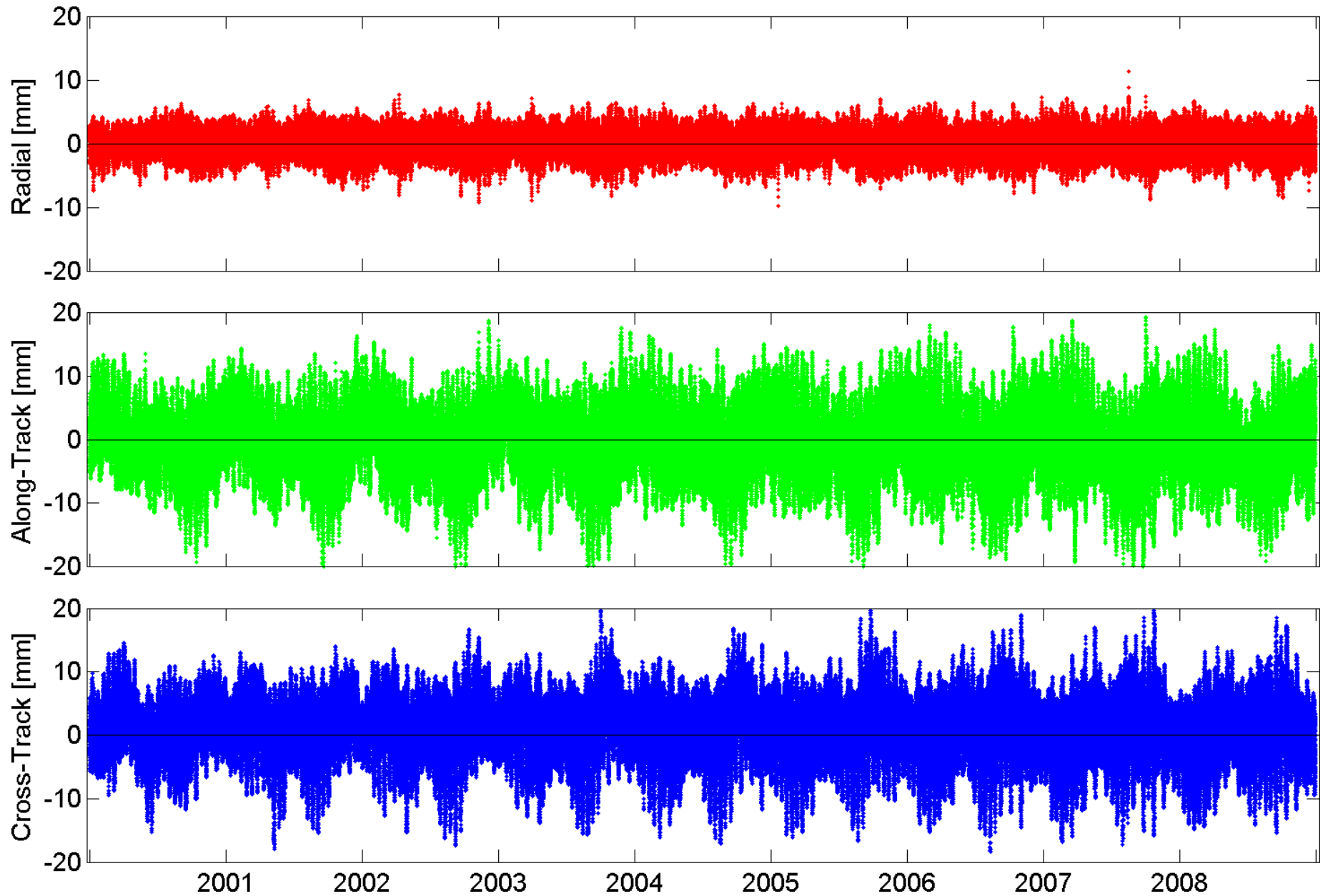


STD_X
0.26 mm

STD_Y
0.28 mm

STD_Z
0.73 mm

Orbit Residuals: IERS2003/COD09



Conclusions

- GPS- and VLBI-derived subdaily ERP estimates agree on the **5 μs level for polar motion** and **0.3 μs level for UT1**
- Impact of different subdaily ERP models on global solutions visible in different parameter types:
 - Earth rotation parameters:
 - $\pm 15 \mu\text{s}$ for polar motion
 - $\pm 100 \mu\text{s/d}$ for polar motion rates
 - $\pm 10 \mu\text{s/d}$ for LOD
 - Coordinate time series: few 1/10 mm level
 - Geocenter: below 1 mm for X and Y, up to 2 mm for Z
 - Satellite orbits: up to 2 cm
 - Several **aliasing periods** clearly visible, more pronounced for GPS compared to VLBI